

# BESIII粲物理进展

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# 粲物理实验主要目标

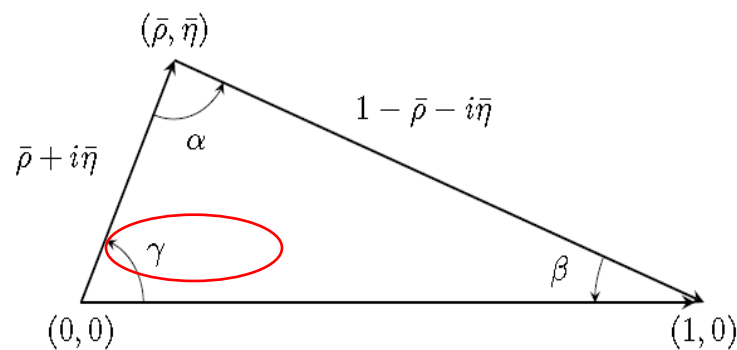
## ➤ (Semi-)leptonic $D_{(s)}$ decays

1.  $f_{D(s)+}, f_{K(\pi)+}^{K(\pi)}$ : better calibrate LQCD
2.  $|V_{cs(d)}|$ : better test on CKM matrix unitarity
3. LFU test and search of rare SL decays

$$U = \begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix}$$

## ➤ Hadronic $D_{(s)}$ decays

1.  $D^0\bar{D}^0$  mixing parameters and CPV
2. Strong phase difference in  $D^0$  decays:  
Constrain  $\gamma/\phi_3$  measurement in B decays
3. SU(3) symmetry and break effect



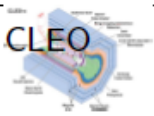





## ➤ Absolute BFs of $\Lambda_c^+$ decays

No absolute BF measurements of  $\Lambda_c^+$  using near threshold data before BESIII

# 主要内容

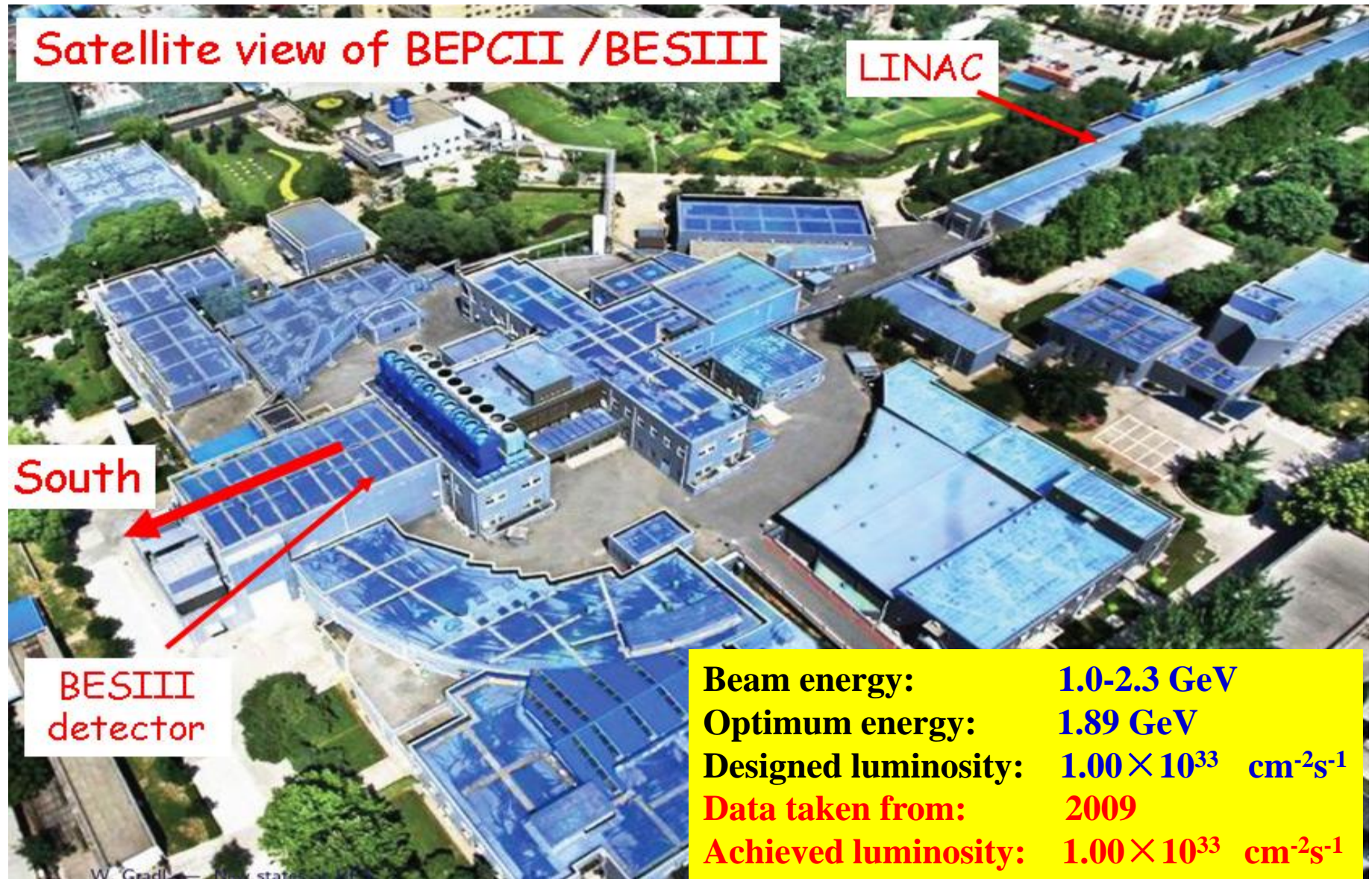
- Charm samples at BESIII
- (Semi-)leptonic  $D_{(s)}$  decays
- Hadronic  $D_{(s)}$  decays
- $\Lambda_c^+$  decays
- Summary

# 近十年来的粲物理实验

Experiment	Machine	C.M	Lumin.	N(D)	efficiency	advantage/disadvantage
	CESR ( $e^+e^-$ )	3.77 GeV	0.8 fb $^{-1}$	$2.9 \times 10^6$	~10-30%	☺ extremely clean enviroment
		4.17 GeV	0.6 fb $^{-1}$	$2.3 \times 10^6(D^\pm)$		☺ pure D-beam, almost no bkg
	BEPC-II ( $e^+e^-$ )	3.77 GeV	2.92 fb $^{-1}$	$0.6 \times 10^6$		☺ quantum coherence
		4.18 GeV	3 fb $^{-1}$	$10.5 \times 10^6$ $8.4 \times 10^6$ $D^{0(+)}$ $3 \times 10^6$ $D_s^+$		☹ no CM boost, no T-dep analyses
				★	★★★★	
 	KEKB ( $e^+e^-$ )	10.58 GeV	1 ab $^{-1}$	$1.3 \times 10^9$	~5-10%	☺ clear event environment
	PEP-II ( $e^+e^-$ )	10.58 GeV	0.5 ab $^{-1}$	$6.5 \times 10^8$		☺ high trigger efficiency
				★★	★★	☺ high-efficiency detection of neutrals
 	Tevatron ( $p\bar{p}$ )	1.96 TeV	9.6 fb $^{-1}$	$1.3 \times 10^{11}$	<0.5%	☺ many high-statistics control samples
	LHC ( $pp$ )	7 TeV	1.0 fb $^{-1}$	$5.0 \times 10^{12}$		☺ time-dependent analysis
		8 TeV	2.0 fb $^{-1}$			☹ smaller cross-section than pp colliders
				★★★★	★	☺ large production cross-section
						☺ large boost: excellent time resolution
						☹ dedicated trigger required
						☹ hard to do neutrals and neutrinos



# BEPCII加速器

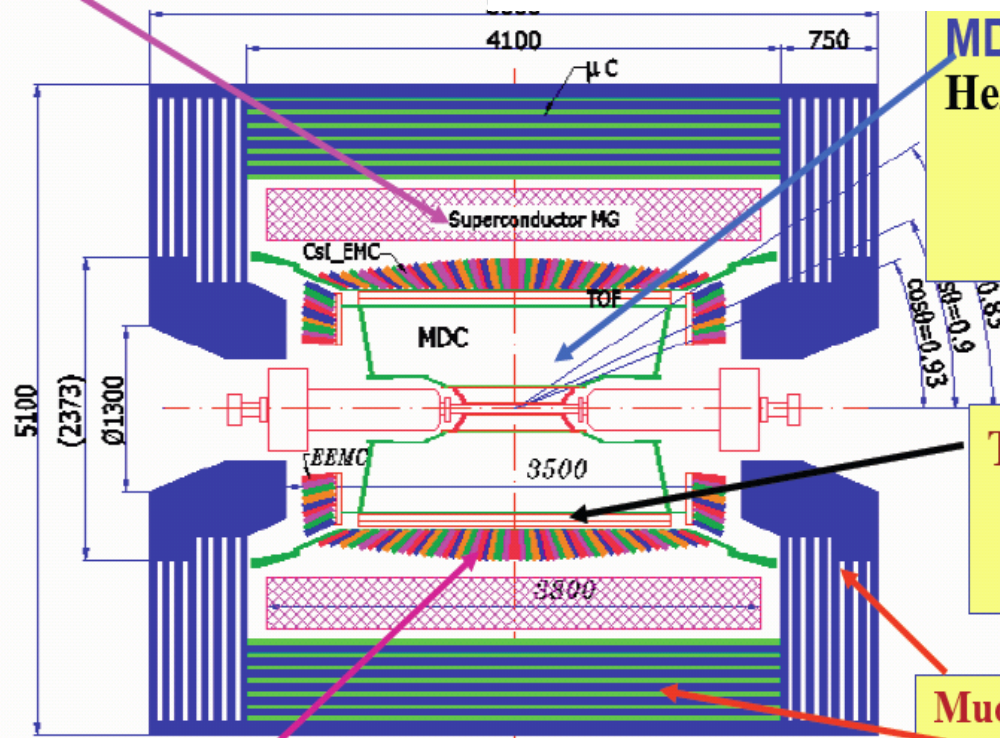


Beam energy:	1.0-2.3 GeV
Optimum energy:	1.89 GeV
Designed luminosity:	$1.00 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$
Data taken from:	2009
Achieved luminosity:	$1.00 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$

# BESIII探测器

Magnet: 1 T Super conducting

Nucl. Instr. Meth. A614, 345 (2010)



MDC: small cell & Gas:  
He/C<sub>3</sub>H<sub>8</sub> (60/40), 43 layers  
 $\sigma_{xy} = 130 \mu\text{m}$   
 $\sigma_p/p = 0.5\% @ 1\text{GeV}$   
 $dE/dx = 6\%$

TOF:  
 $\sigma_T = 100 \text{ ps}$  Barrel  
110 ps Endcap

Muon ID: 9 layers RPC  
8 layers for endcap

EMC: CsI crystal, 28 cm  
 $\Delta E/E = 2.5\% @ 1 \text{ GeV}$   
 $\sigma_z = 0.6 \text{ cm}/\sqrt{E}$

Data Acquisition:  
Event rate = 4 kHz  
Total data volume  $\sim 50 \text{ MB/s}$

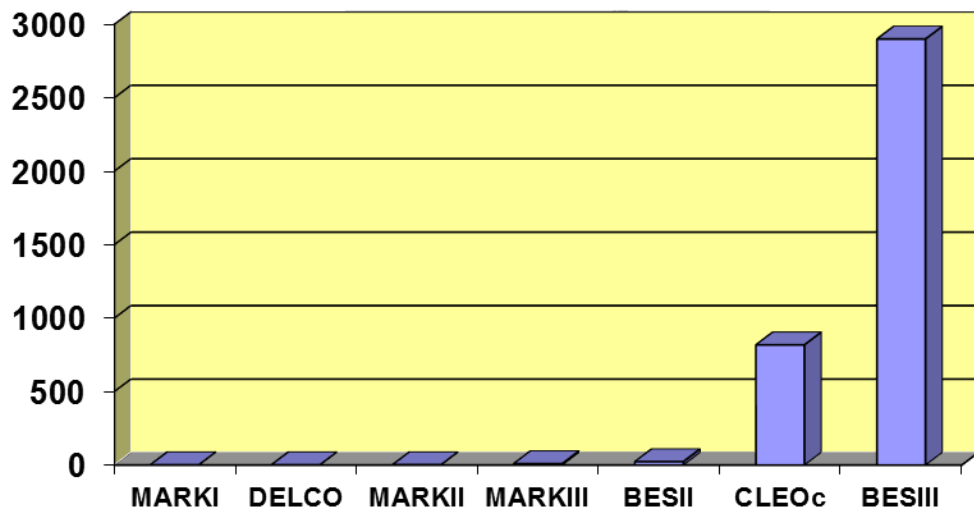
2015年ETOF升级改造后,  
分辨好于60 ps



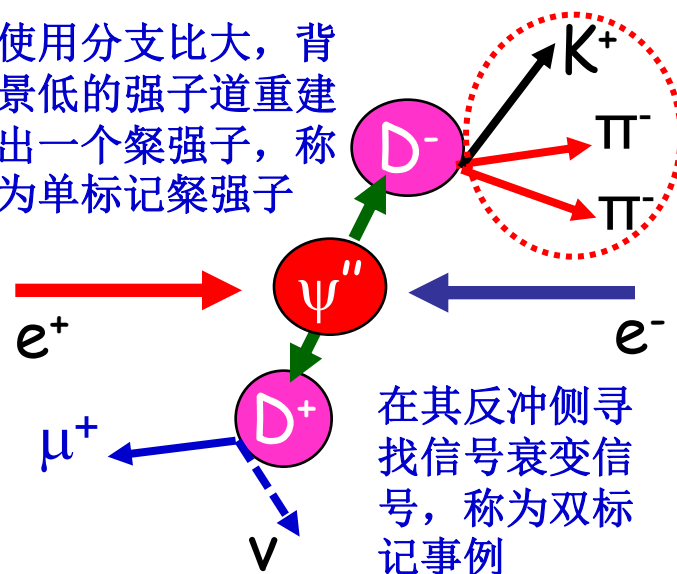
# BESIII $D^{0(+)}$ , $D_s^+$ 和 $\Lambda_c^+$ 样本

## ➤ $D^{0(+)}$ 样本 @ $\psi(3770)$

2010-2011  
3.773 GeV



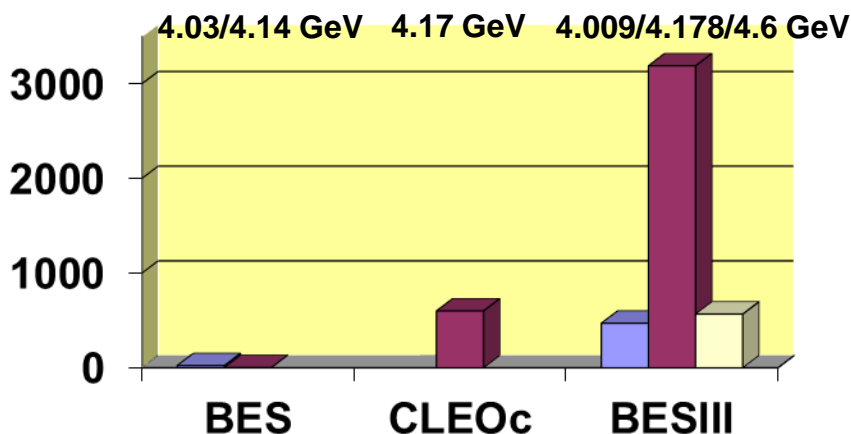
使用分支比大，背景低的强子道重建出一个粲强子，称为单标记粲强子



联合单、双标记粲强子，测定绝对分支比，研究动力学机制

## ➤ $D_s^+/\bar{D}_s^+/\Lambda_c^+$ 样本

2011/2016/2014



$$N_{ST}^i = 2 \times N_{D\bar{D}} \times B_{ST}^i \times \epsilon_{ST}^i$$

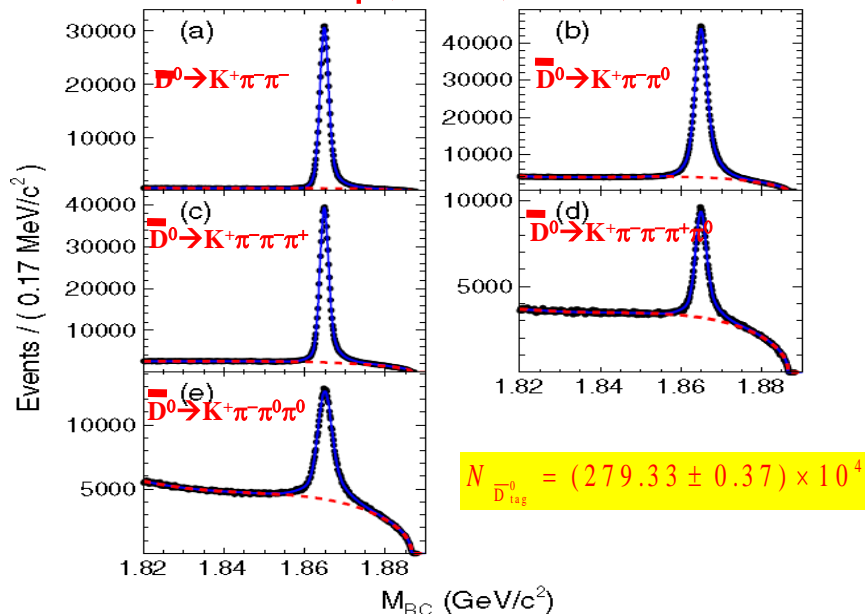
$$N_{DT}^i = 2 \times N_{D\bar{D}} \times B_{ST}^i \times B_{sig} \times \epsilon_{ST \text{ vs. sig}}^i$$

$$B_{sig} = \frac{N_{DT}^{tot}}{N_{ST}^{tot} \times \bar{\epsilon}_{sig}}$$

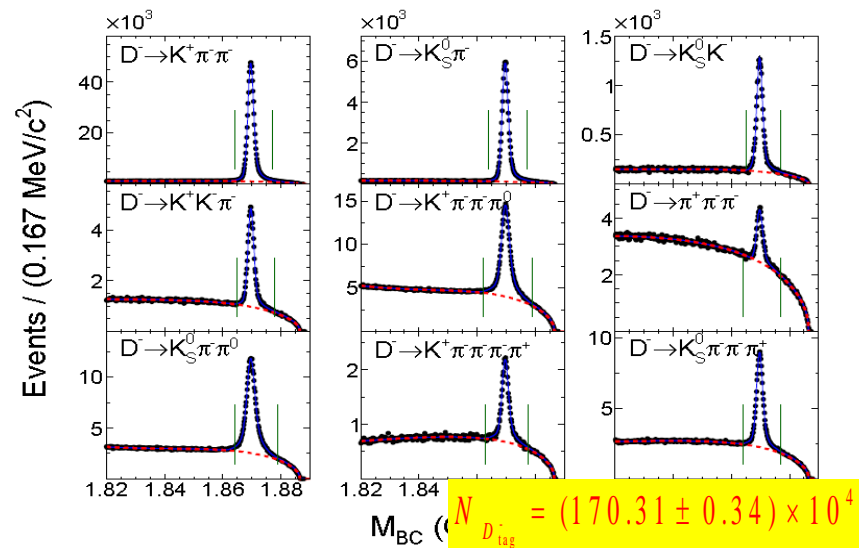
$$\bar{\epsilon}_{sig} = \sum_{i=1}^N (N_{ST}^i \times \epsilon_{ST \text{ vs. sig}}^i / \epsilon_{ST}^i) / \sum_{i=1}^N N_{ST}^i$$

# 单标记粲强子样本

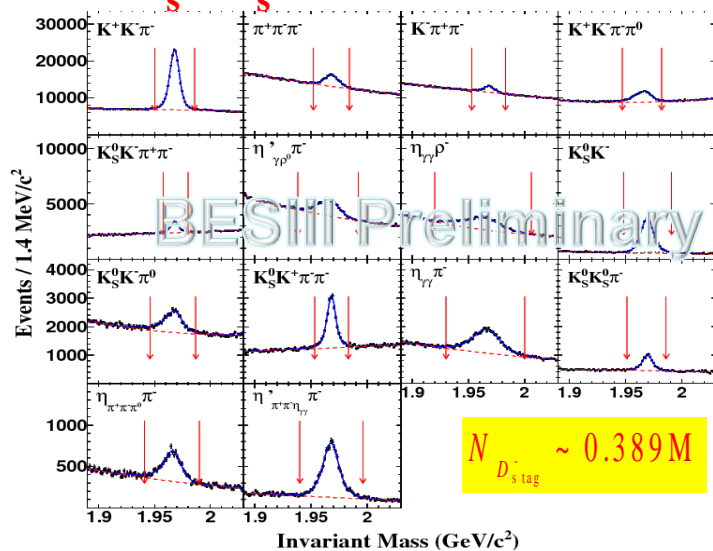
$$e^+e^- \rightarrow \psi(3770) \rightarrow D^0 \bar{D}^0$$



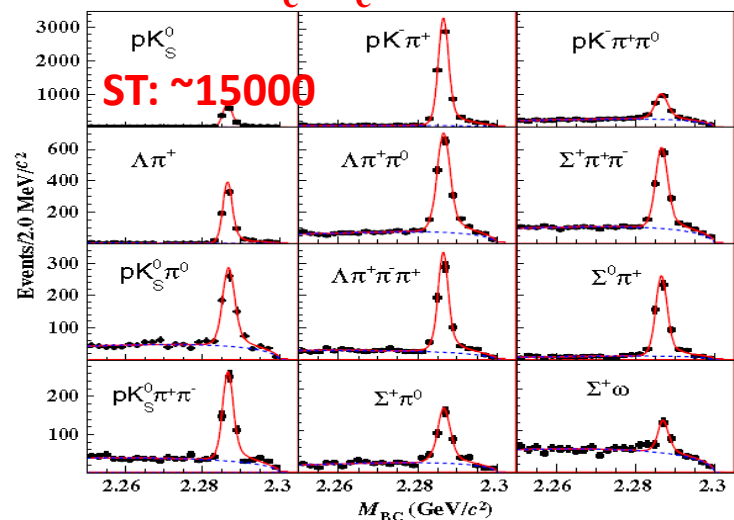
$$e^+e^- \rightarrow \psi(3770) \rightarrow D^+ D^-$$



$$e^+e^- \rightarrow D_s^{*+} D_s^- + \text{c.c.}$$



$$e^+e^- \rightarrow \Lambda_c^+ \bar{\Lambda}_c^- + \text{c.c.}$$

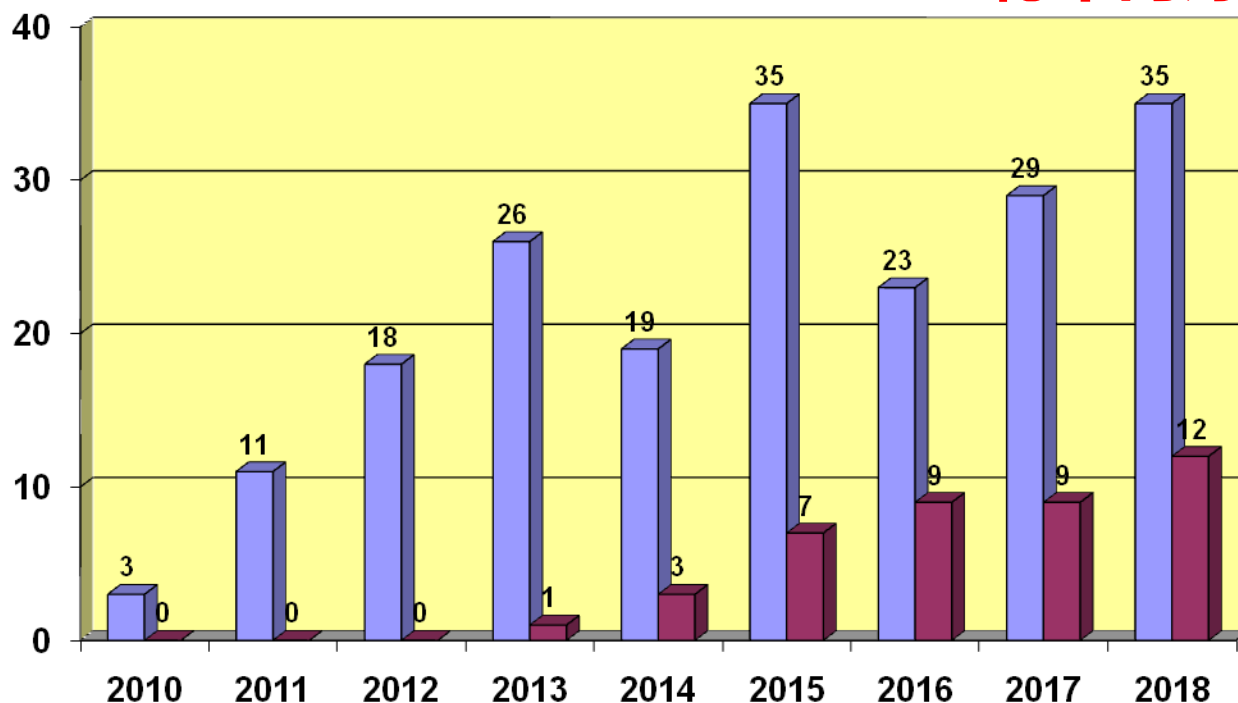


# BESIII粲物理研究进展概况

- 4年来，粲物理文章数量、质量大幅提高：4→41篇；其中PRL文章0→9篇。

- 全组开展粲物理分析的学生从约12人增加到目前的约30人。

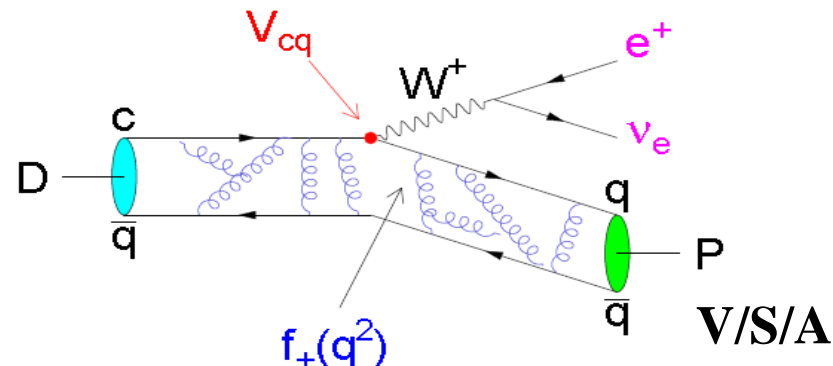
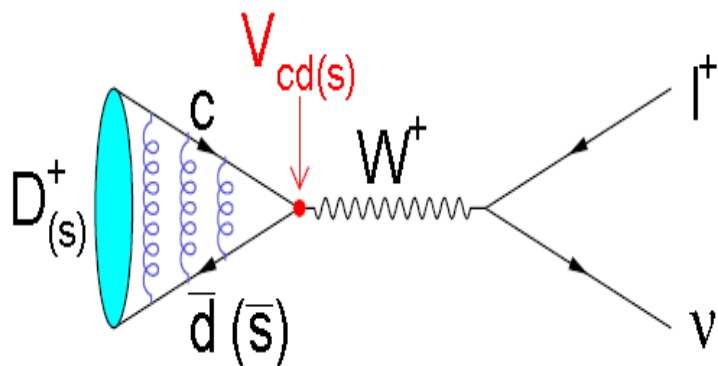
稳中向好



# $D_{(s)}$ 轻子和半轻衰变

- $l^+ \nu$
- $P(\text{赝标介子}) l^+ \nu \rightarrow \text{Some selected topics}$
- $V(\text{矢量介子}) l^+ \nu$
- $S(\text{标量介子}) l^+ \nu$
- Rare SL decays

# $D_{(s)}$ 纯轻和半轻衰变：标准模型精密检验



$$\Gamma(D_{(s)}^+ \rightarrow \ell^+ \nu_\ell) = \frac{G_F^2 f_{D_{(s)}^+}^2}{8\pi} |V_{cd(s)}|^2 m_\ell^2 m_{D_{(s)}^+}^2 \left(1 - \frac{m_\ell^2}{m_{D_{(s)}^+}^2}\right)^2$$

$$\frac{d\Gamma}{dq^2} = X \frac{G_F^2 |V_{cd(s)}|^2}{24\pi^3} p^3 |f_+(q^2)|^2$$

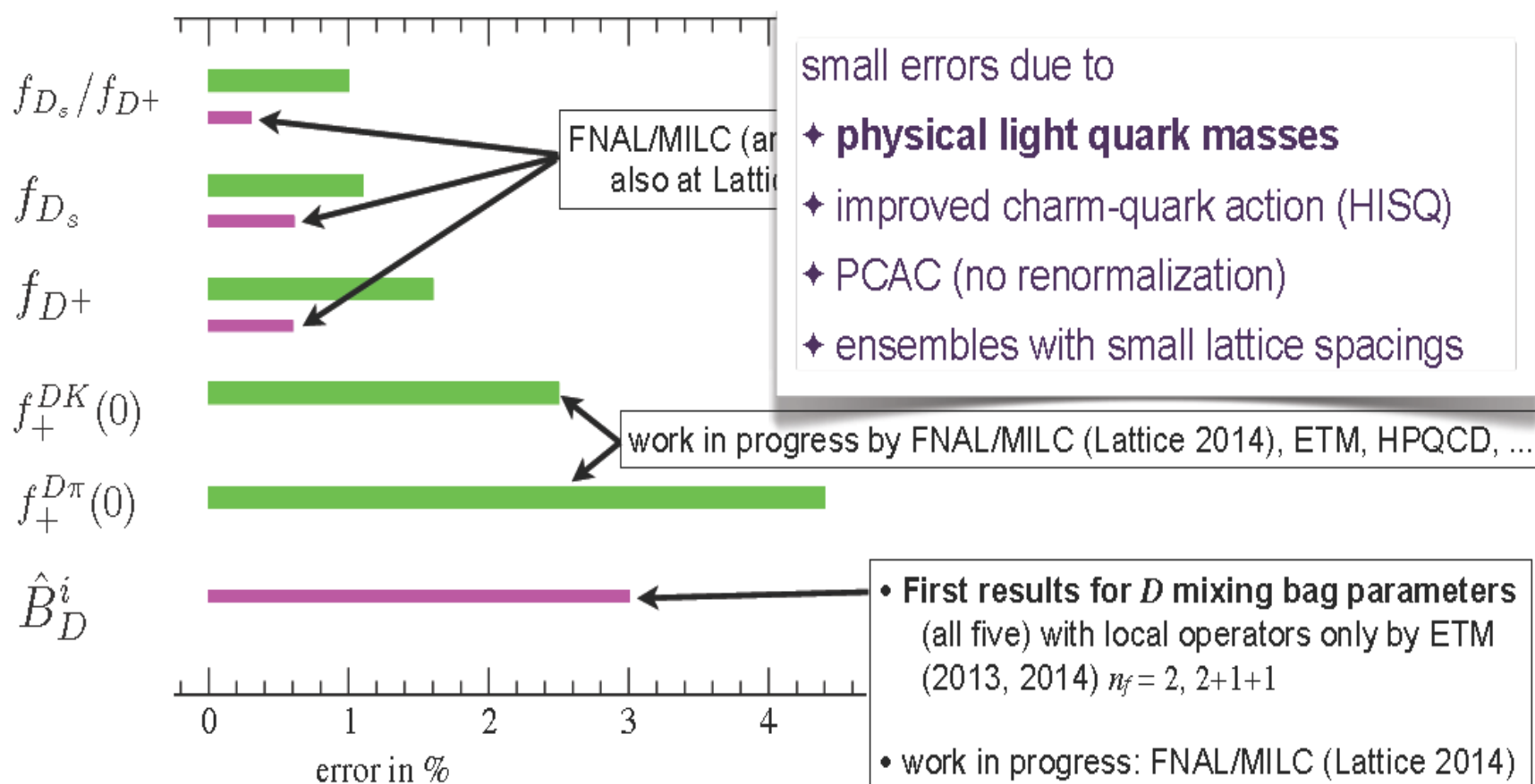
- 测定  $|V_{cs}|$ 、 $|V_{cd}|$ ，检验CKM矩阵的么正性
- 测定D衰变常数、半轻形状因子，检验理论计算
- 寻找含标量介子(S)、轴矢量介子(A)半轻衰变
- 轻子味道普适性(LFU)检验.....

$$U = \begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix}$$

# 格点QCD计算取得重要进展

Taking from Aida X. El-Khadra's talk at Beauty2014

errors (in %) comparison: **FLAG-2 averages** vs. **new results**



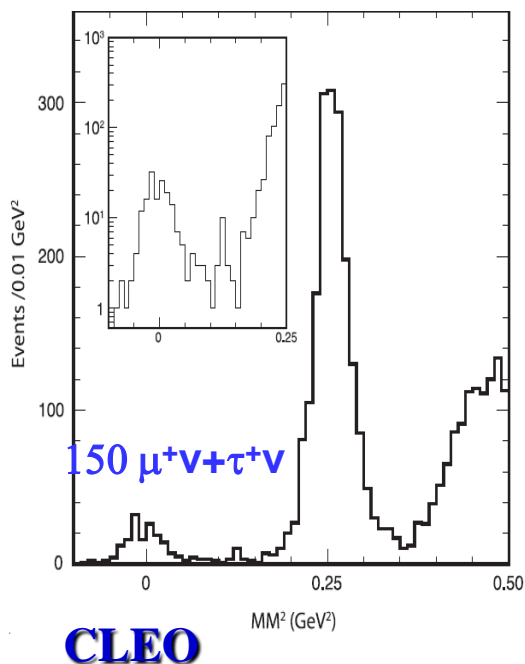
review by C. Bouchard @ Lattice 2014



# 最高精度的 $f_{D^+}$ /首次使用 $D^+ \rightarrow \mu^+ \nu$ 测定 $|V_{cd}|$

818 pb<sup>-1</sup> at  $\psi(3770)$   
(2004–2008)

PRD78(2008)052003

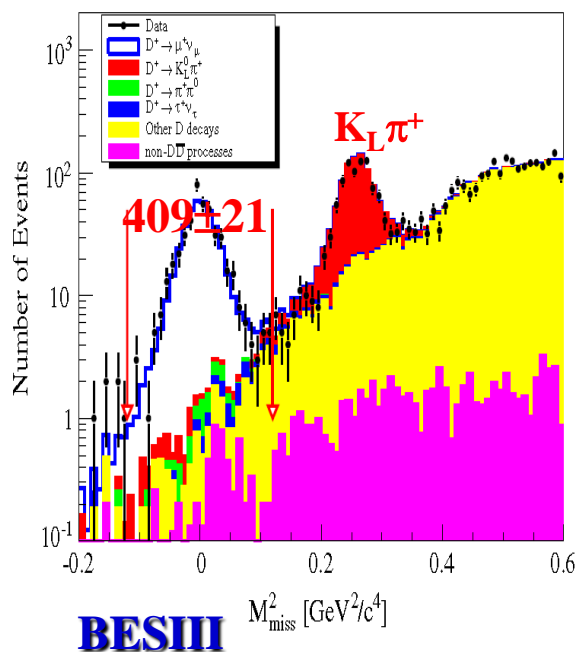


$$B_{D^+ \rightarrow \mu^+ \nu} = (3.82 \pm 0.32 \pm 0.09) \times 10^{-4}$$

$$f_{D^+} = 205.8 \pm 7.5 \pm 2.5 \text{ MeV}$$

2.93 fb<sup>-1</sup> data@ 3.773 GeV

PRD89(2014)051104(RC)

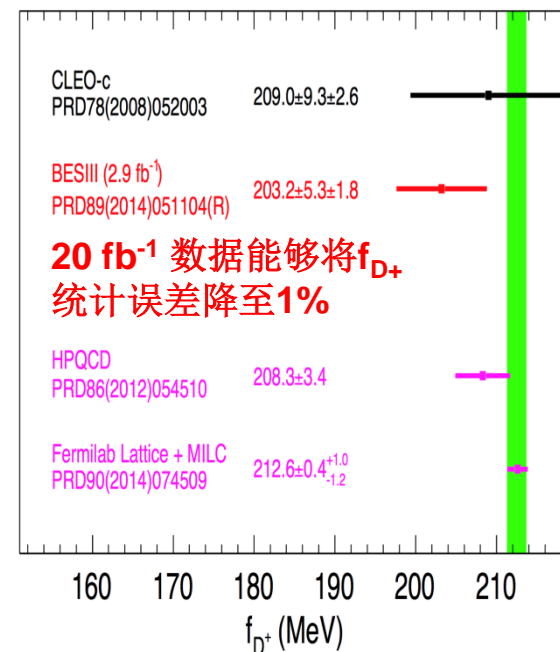


$$B_{D^+ \rightarrow \mu^+ \nu} = (3.71 \pm 0.19 \pm 0.06) \times 10^{-4}$$

$$f_{D^+} = (203.2 \pm 5.3 \pm 1.8) \text{ MeV}$$

$$|V_{cd}| = 0.2210 \pm 0.0058 \pm 0.0047$$

**BESIII**获得世界上单次测量精度最高的 $f_{D^+}$ 和 $|V_{cd}|$



**D**轻子测量方案改变了此前 $|V_{cd}|$ 测量由中微子散射、D半轻方案主导的局面，随即被PDG采纳，使得 $|V_{cd}|$ 世界平均值误差从4.8%降至1.8%

# $f_{D^+}$ , $f_{D_s^+}$ 和 $f_{D^+}:f_{D_s^+}$ 比较(2014)

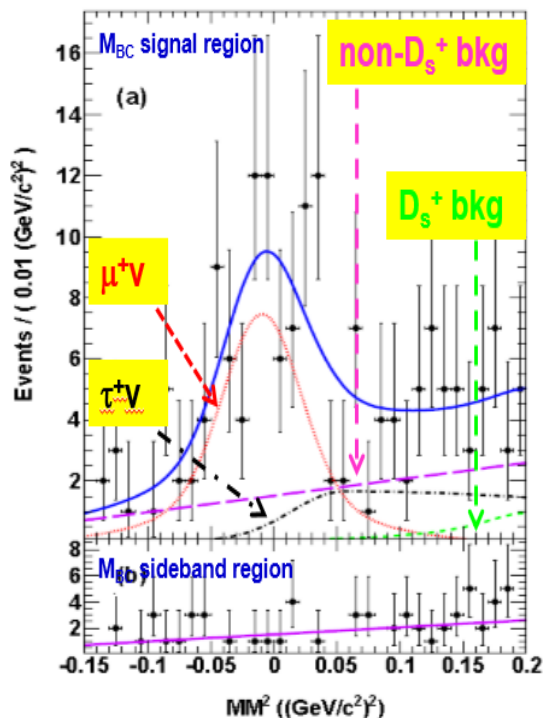
	Experiments	Femilab Lattice+MILC (2014)		HPQCD (2012)	
	Averaged	Expected	$\Delta$	Expected	$\Delta$
$f_{D^+}(\text{MeV})$	$203.9 \pm 4.7$	$212.6 \pm 0.4^{+1.0}_{-1.2}$	$1.8\sigma$	$208.3 \pm 3.4$	$0.8\sigma$
$f_{D_s^+}(\text{MeV})$	$256.9 \pm 4.4$	$249.0 \pm 0.3^{+1.1}_{-1.5}$	$1.7\sigma$	$246.0 \pm 3.6$	$1.4\sigma$
$f_{D^+}:f_{D_s^+}$	$1.260 \pm 0.036$	$1.1712 \pm 0.0010^{+0.0029}_{-0.0032}$	$2.5\sigma$	$1.187 \pm 0.013$	$1.9\sigma$

- 实验精度远小于理论精度( $f_{D^+}$ ,  $f_{D_s^+}$ ,  $f_{D^+}:f_{D_s^+}$  达0.5%,0.5%,0.3%)
- 实验与理论预期 $f_{D^+}$ ,  $f_{D_s^+}$ ,  $f_{D^+}:f_{D_s^+}$  偏离约 $2\sigma$
- 期待实验上更精确的结果

# $D_s^+ \rightarrow l^+ \nu \rightarrow$ 单次最高精度的 $f_{D_s} |V_{cs}|$

0.48 fb<sup>-1</sup> data @ 4.01 GeV

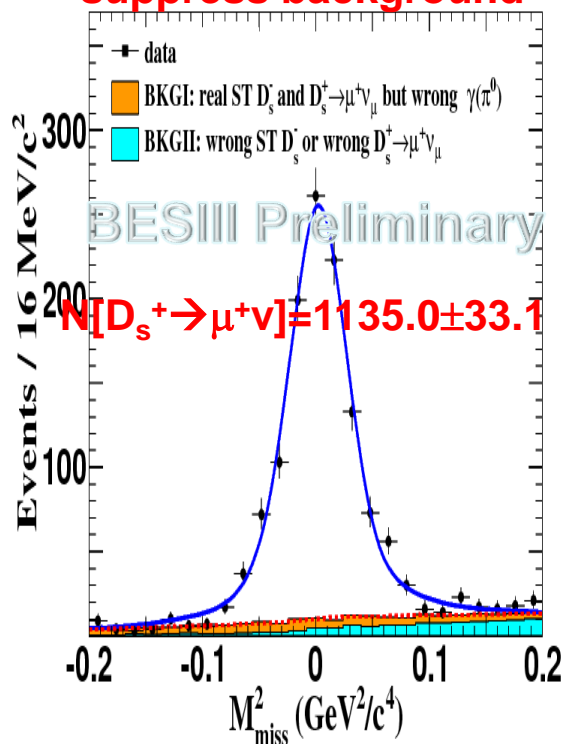
PRD94(2016)072004



$$f_{D_s^+} = (241.0 \pm 16.3 \pm 6.6) \text{ MeV}$$

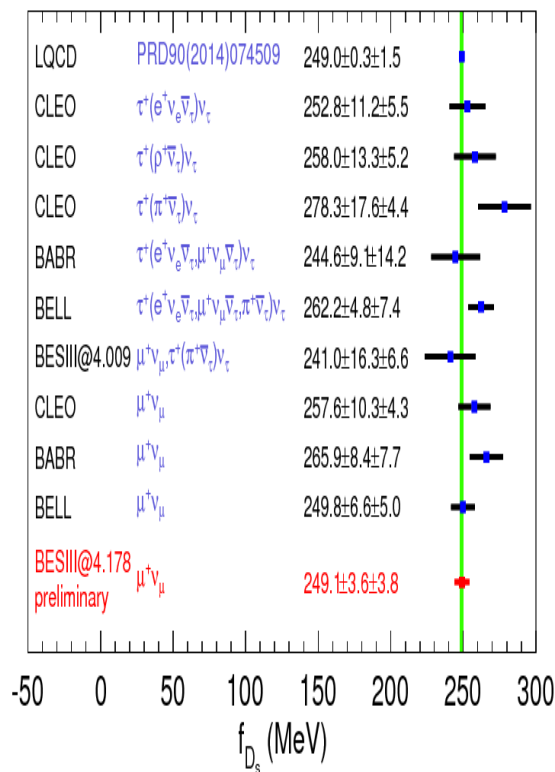
3.19 fb<sup>-1</sup> data @ 4.178 GeV

Use  $\mu$  counter to suppress background



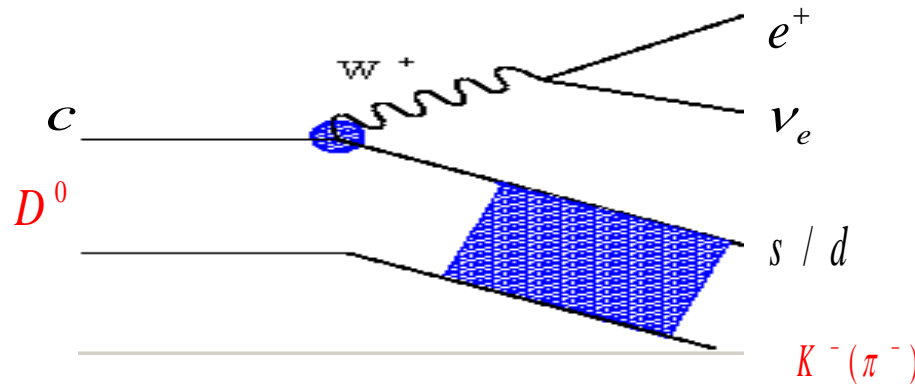
$$f_{D_s} |V_{cs}| = 242.5 \pm 3.5 \pm 3.7 \text{ MeV}$$

BESIII 获得世界上单次测量精度最高的  $f_{D_s^+}$  和  $|V_{cs}|$



BESIII  $f_{D_s^+}$  精度达2%，  
联合  $\tau^+ \nu$  研究，能够降  
至1.5%水平

# 分析 $D^0 \rightarrow K(\pi)^- e^+ \nu$ 提取 $f_{+}^{K(\pi)}(0) |V_{cs(d)}|$



$$\frac{\Delta \Gamma(D^0 \rightarrow K/\pi^- e^+ \nu_e)}{dq^2} = X \frac{G_F^2 |V_{cs(d)}|^2}{24\pi^3} p^3 |f_+(q^2)|^2$$

– Single pole form

$$f_+(q^2) = \frac{f_+(0)}{1 - \frac{q^2}{M_{\text{pole}}^2}}$$

– Modified pole model

$$f_+(q^2) = \frac{f_+(0)}{(1 - \frac{q^2}{M_{\text{pole}}^2})(1 - \alpha \frac{q^2}{M_{\text{pole}}^2})}$$

– ISGW2 model

$$f_+(q^2) = f_+(q_{\text{max}}^2) \left(1 + \frac{r_{\text{ISGW2}}^2}{12} (q_{\text{max}}^2 - q^2)\right)^{-2}$$

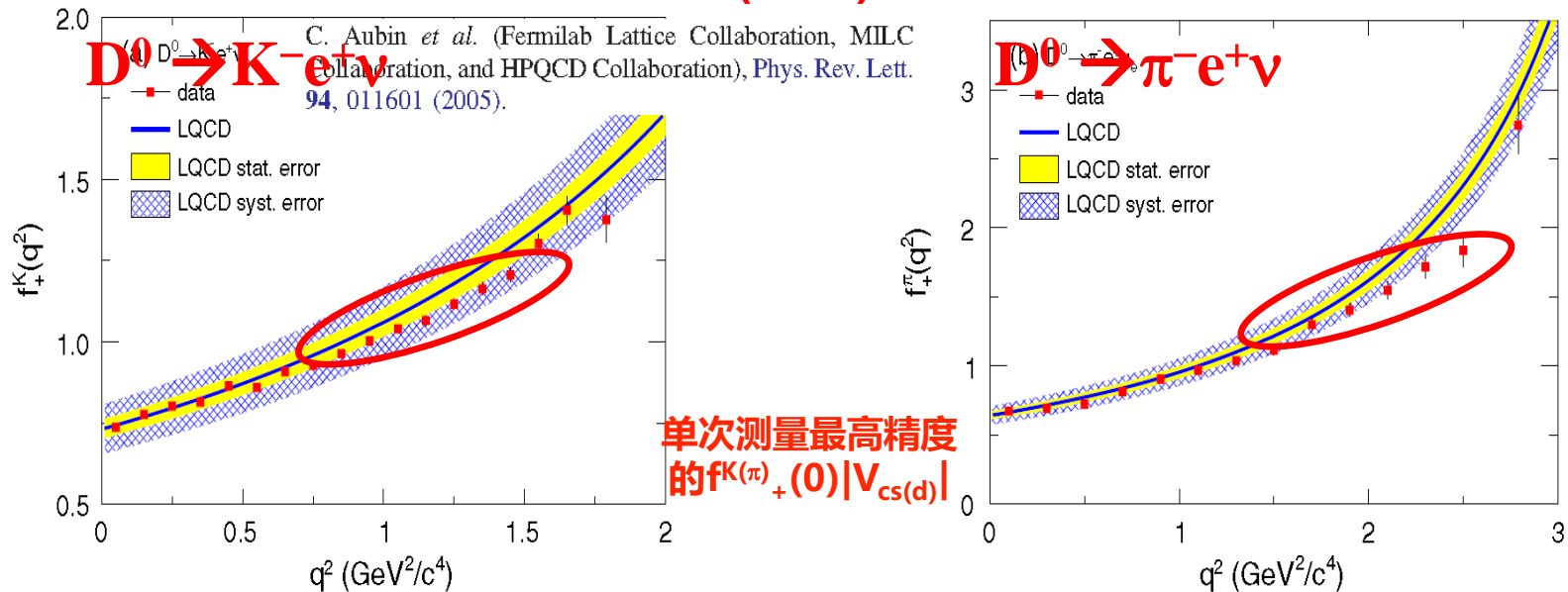
– Series expansion model

$$f_+(t) = \frac{1}{P(t)\Phi(t, t_0)} a_0(t_0) \left(1 + \sum_{k=1}^{\infty} r_k(t_0) [z(t, t_0)]^k\right)$$

**Recently improved LQCD calculations on  $f_+^{D \rightarrow K(\pi)}(0)$  [2.4(4.4)%] provide good chance to precisely measure the CKM matrix element  $|V_{cs(d)}|$ , which are important for the unitarity test of the CKM matrix and search for NP beyond the SM**

# 检验LQCD计算的 $f_K^{(\pi)}(q^2)$

PRD92(2015)072012



J. Zhang and C.X. Yue, arXiv:1805.00700v1 [hep-ph]

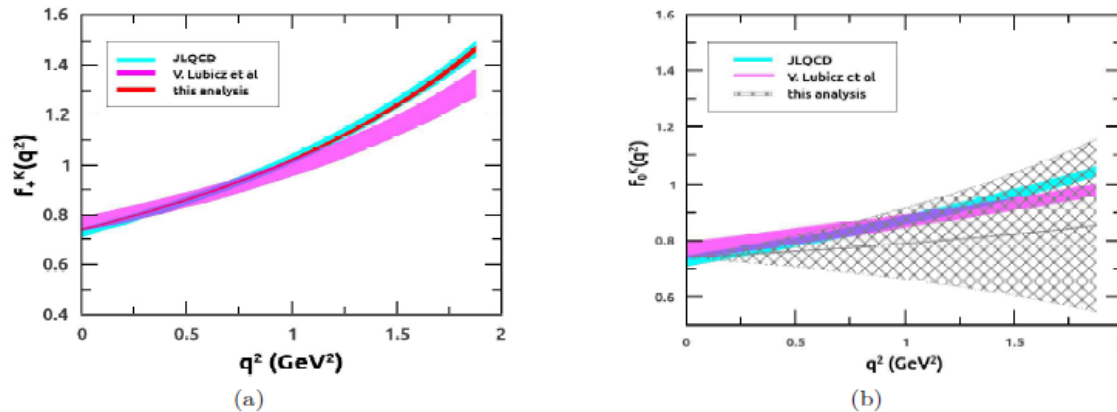
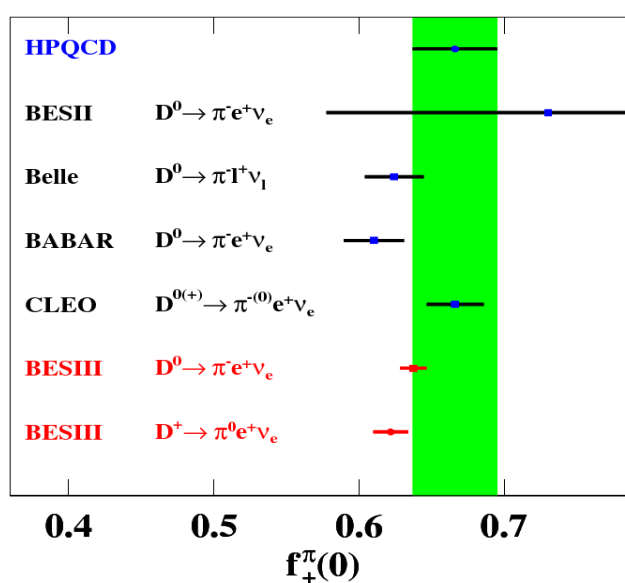
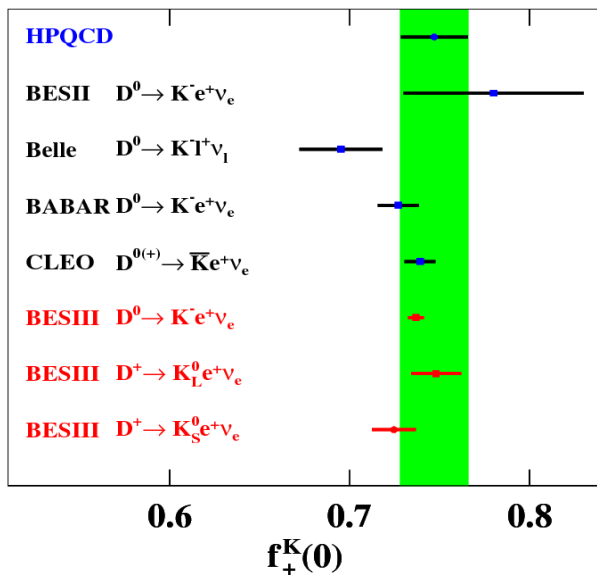
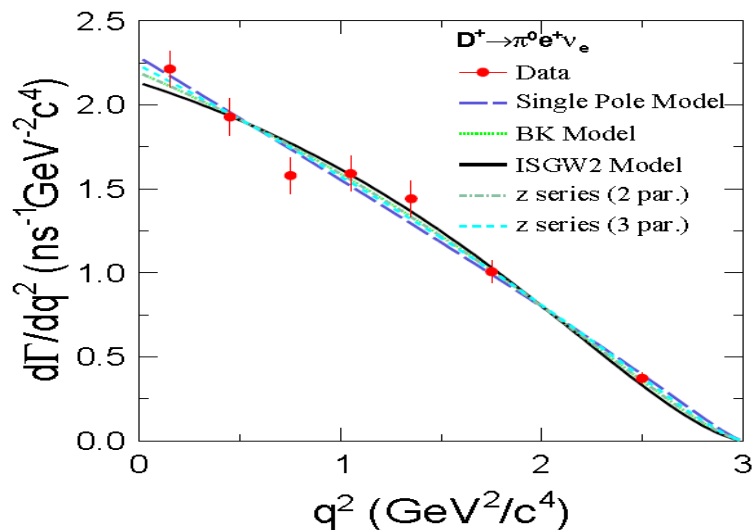
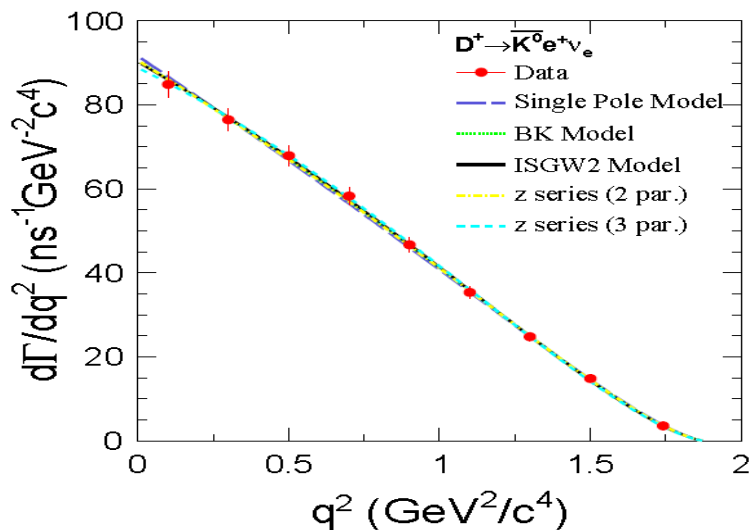


Figure 7: Comparisons of the result of fit to experimental measurements and lattice calculations for  $f_+^K(q^2)$  (a) and  $f_0^K(q^2)$  (b).

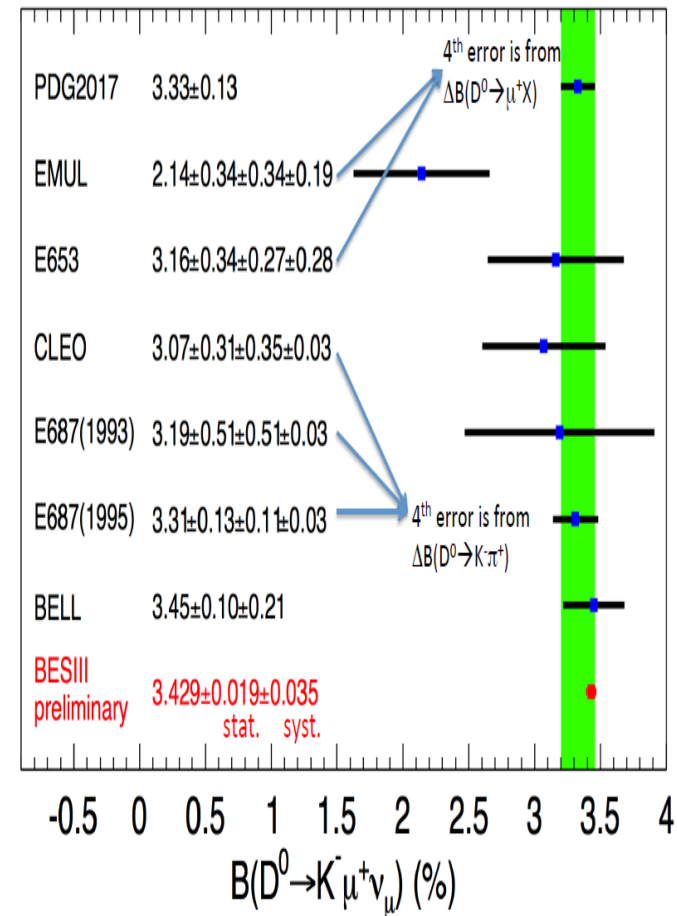
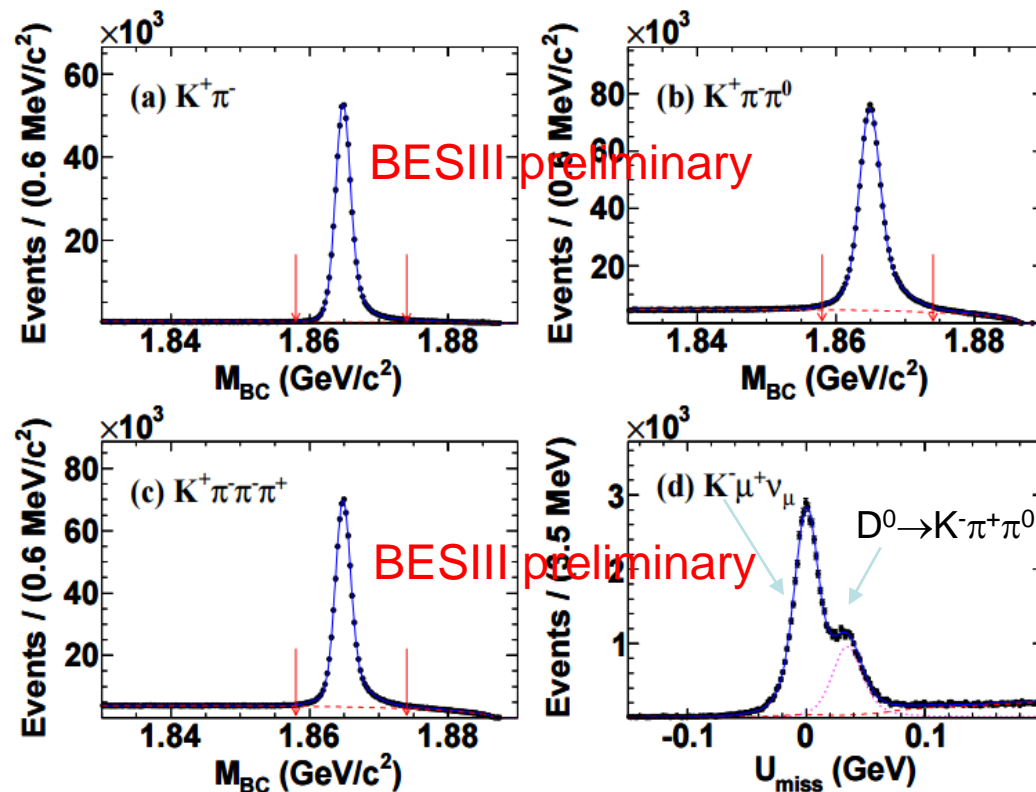
# 分析 $D^+ \rightarrow \bar{K}^0(\pi^0)e^+\nu$ 提取 $f^{K(\pi)}_+(0)|V_{cs(d)}|$

PRD96(2017)012002



BESIII 获得世界上单次测量精度最高的形状因子  $f^{D \rightarrow K(\pi)}_+(0)$ , 精度好于 1%

# $D^0 \rightarrow K^- \mu^+ \nu$ 分支比的精密测量



Total ST yield:  $(234 \pm 2) \times 10^4$

DT yield:  $47100 \pm 259$

# $D^0 \rightarrow K^- \mu^+ \nu$ 衰变的精密动力学研究

## Differential partial widths

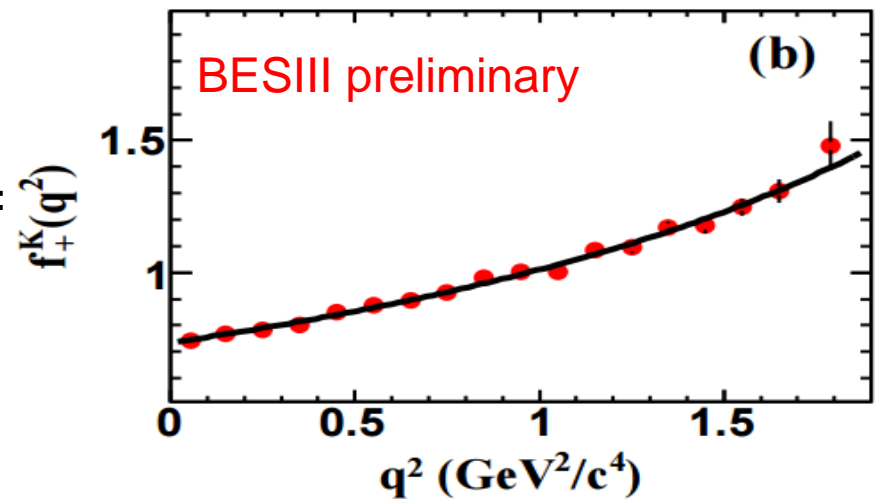
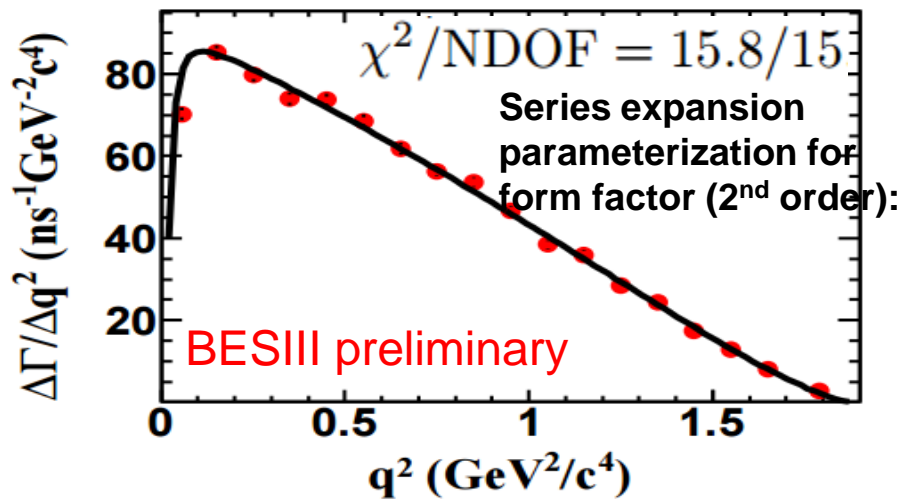
$$\begin{aligned} \frac{d\Gamma}{dq^2} = & \frac{G_F^2 |V_{cs}|^2}{8\pi^3 m_D} |\vec{p}_K| |f_+^K(q^2)|^2 \left( \frac{W_0 - E_K}{F_0} \right)^2 \\ & \times \left[ \frac{1}{3} m_D |\vec{p}_K|^2 + \frac{m_\ell^2}{8m_D} (m_D^2 + m_K^2 + 2m_D E_K) \right. \\ & + \frac{1}{3} m_\ell^2 \frac{|\vec{p}_K|^2}{F_0} + \frac{1}{4} m_\ell^2 \frac{m_D^2 - m_K^2}{m_D} \text{Re} \left( \frac{f_-^K(q^2)}{f_+^K(q^2)} \right) \\ & \left. + \frac{1}{4} m_\ell^2 F_0 \left| \frac{f_-^K(q^2)}{f_+^K(q^2)} \right|^2 \right] \end{aligned}$$

Assumed to be independent of  $q^2$  following FOCUS's treatment  
(PLB607(2005)233)

$$q = p_\mu + p_\nu$$

$$W_0 = (m_D^2 + m_K^2 - m_\ell^2)/2m_D$$

$$F_0 = W_0 - E_K + m_\ell^2/2m_D$$



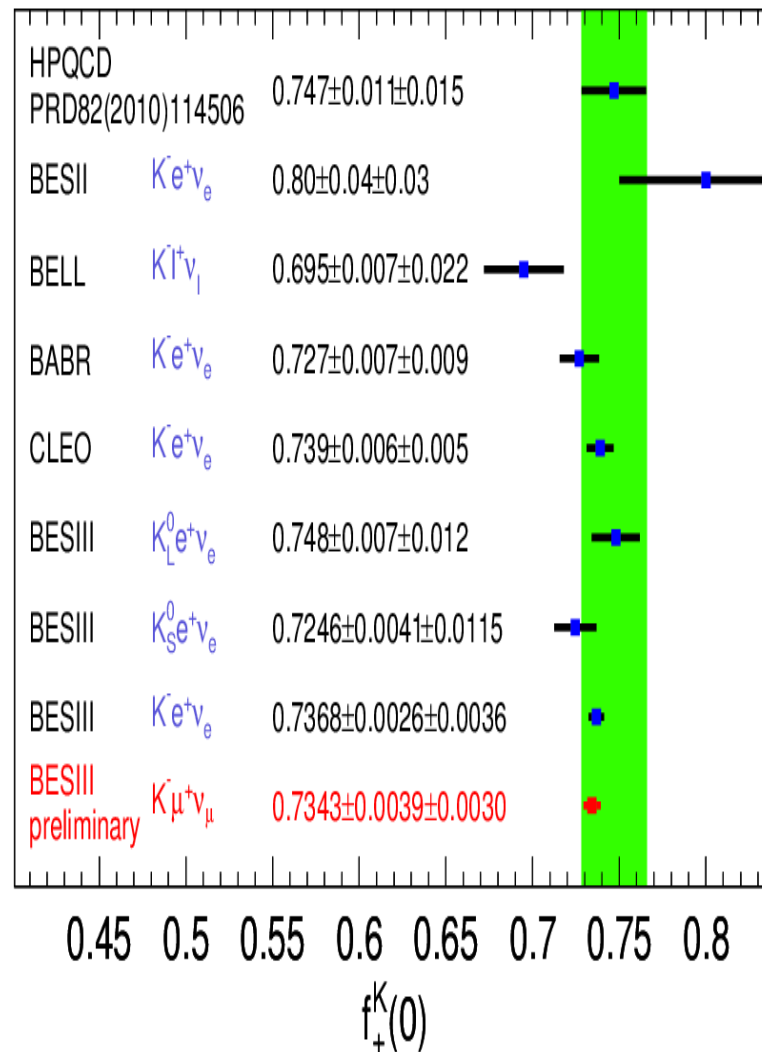
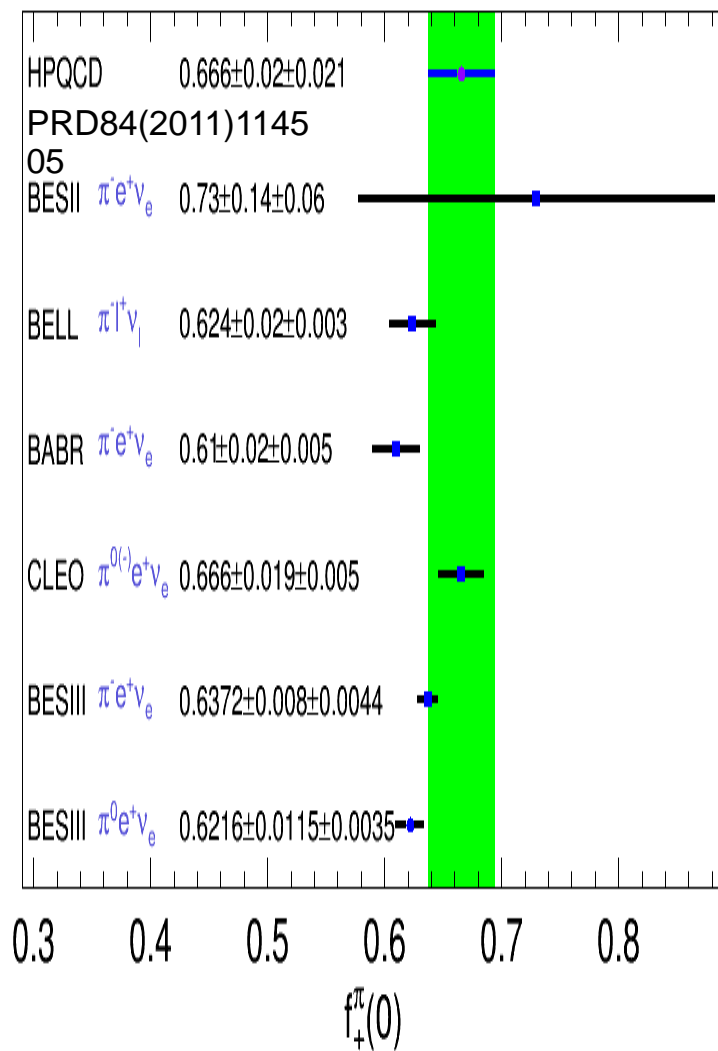
$$f_+^K(0) |V_{cs}| = 0.7148 \pm 0.0038_{\text{stat.}} \pm 0.0029_{\text{syst.}}$$

$$r_1 = -1.94 \pm 0.21_{\text{stat.}} \pm 0.07_{\text{syst.}}$$

$$f_-^K / f_+^K = -0.7 \pm 0.9_{\text{stat.}} \pm 0.1_{\text{syst.}}$$

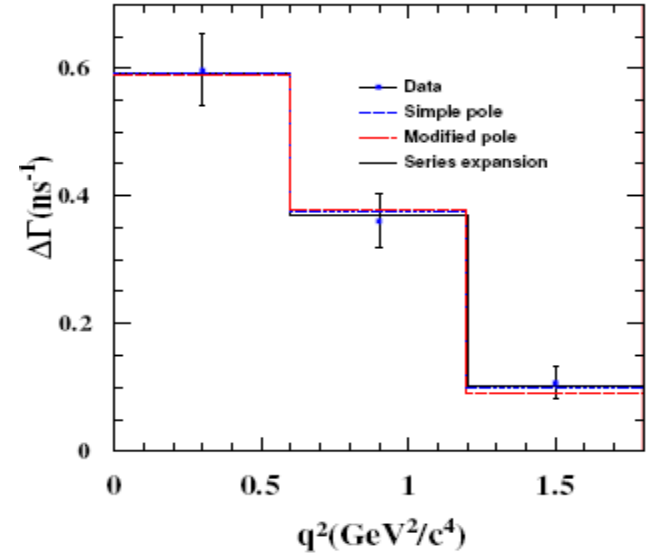
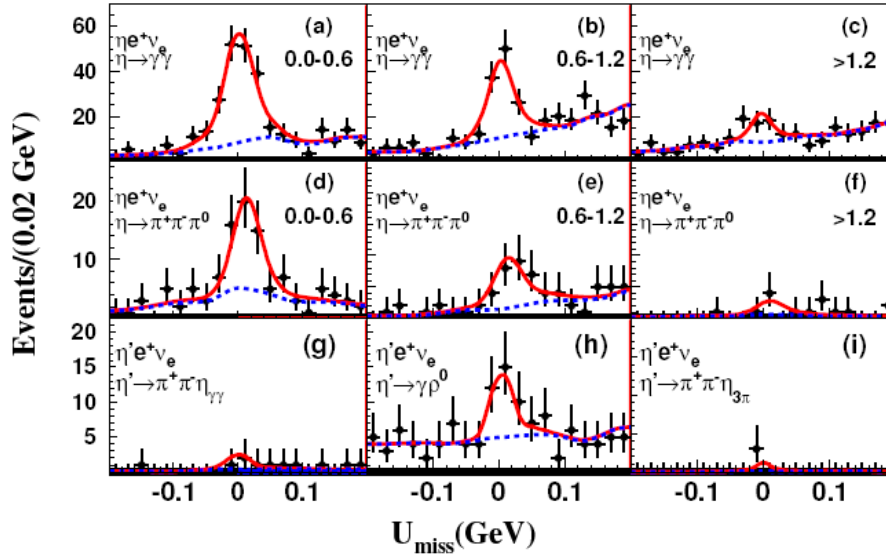


# 形状因子 $f_+^{K(\pi)}(0)$ 的实验和理论比较



# $D^+ \rightarrow \eta^{(\prime)} e^+ \nu$ 分支比和动力学研究

PRD97(2018)092009



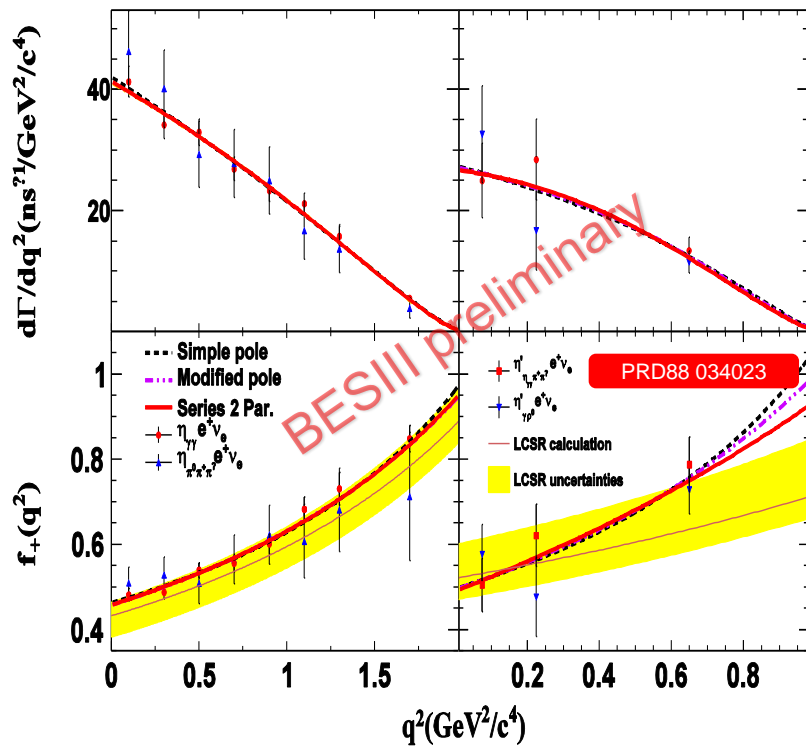
Fit parameters	Simple pole	Modified pole	Series expansion
$f_+(0) V_{cd}  (\times 10^{-2})$	$8.15 \pm 0.45 \pm 0.18$	$8.24 \pm 0.51 \pm 0.22$	$7.86 \pm 0.64 \pm 0.21$
Shape parameter	$1.73 \pm 0.17 \pm 0.03$	$0.50 \pm 0.54 \pm 0.08$	$-7.33 \pm 1.69 \pm 0.40$
$\rho$	0.80	-0.85	0.90
$\chi^2/\text{ndf}$	$0.1/(3-2)$	$0.3/(3-2)$	$0.5/(3-2)$

- $\langle \eta | = \cos \phi_P \langle \eta_q | - \sin \phi_P \langle \eta_s |,$
  - $\langle \eta' | = \cos \phi_G (\sin \phi_P \langle \eta_q | + \cos \phi_P \langle \eta_s |) + \sin \phi_G \langle gg |;$
  - $\frac{\Gamma(D^+ \rightarrow \eta' \ell^+ \nu_\ell)}{\Gamma(D^+ \rightarrow \eta \ell^+ \nu_\ell)} = \tilde{R}_D \tan^2 \phi_P,$
- $\mathcal{B}_{\eta e^+ \nu_e} = (10.74 \pm 0.81 \pm 0.51) \times 10^{-4}$   
 $\mathcal{B}_{\eta' e^+ \nu_e} = (1.91 \pm 0.51 \pm 0.13) \times 10^{-4}$   
 $\phi_P = (40 \pm 3 \pm 3)^\circ (\phi_G=0)$

该方法需要输入外部参数

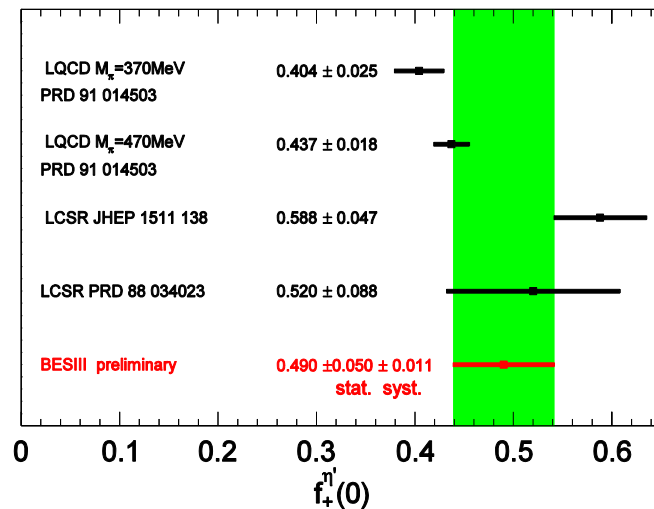
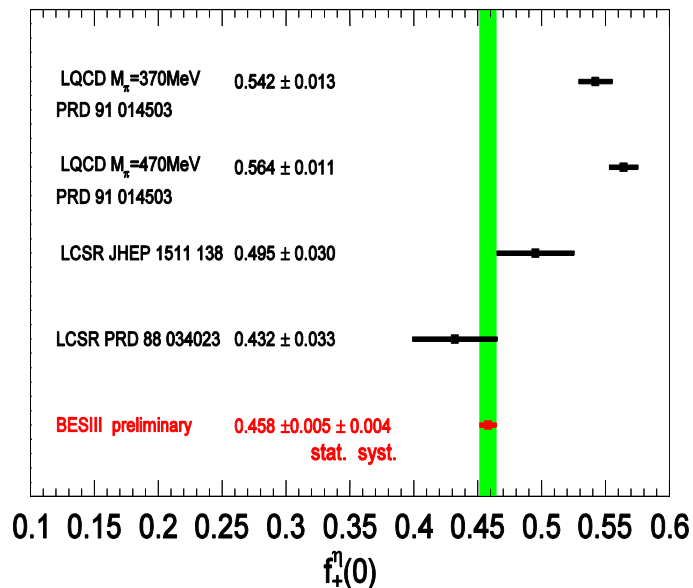
# $D_s \rightarrow \eta^{(\prime)} e^+ \nu$ 形状因子的首次测量

## Fits to partial decay rates



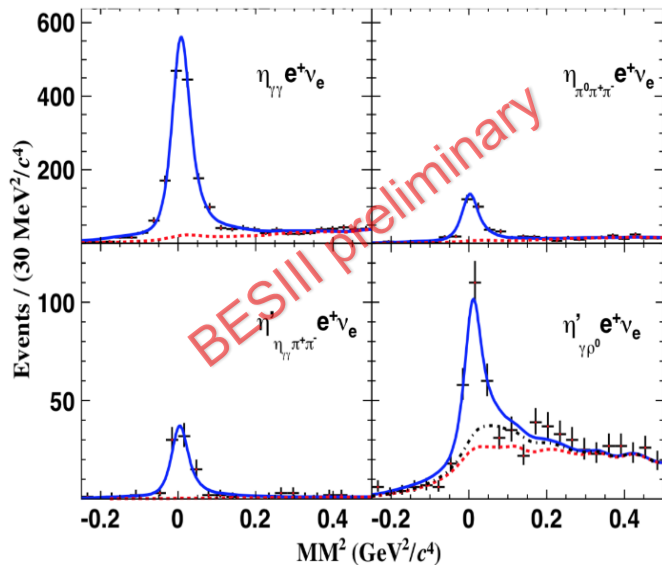
Case	Simple pole			Modified pole			Series 2 Par.		
	$f_+^{\eta^{(\prime)}}(0) V_{cs} $	$M_{\text{pole}}$	$\chi^2/\text{NDOF}$	$f_+^{\eta^{(\prime)}}(0) V_{cs} $	$\alpha$	$\chi^2/\text{NDOF}$	$f_+^{\eta^{(\prime)}}(0) V_{cs} $	$r_1$	$\chi^2/\text{NDOF}$
$\eta e^+ \nu_e$	0.450(5)(3)	3.77(8)(5)	12.2/14	0.445(5)(3)	0.30(4)(3)	11.4/14	0.446(5)(4)	-2.2(2)(1)	11.5/14
$\eta' e^+ \nu_e$	0.494(45)(10)	1.88(54)(5)	1.8/4	0.481(44)(10)	1.62(91)(11)	1.8/4	0.477(49)(11)	-13.1(76)(11)	1.9/4

## Comparisons of form factors



# $D_s \rightarrow \eta^{(\prime)} e^+ \nu$ 分支比和 $\eta-\eta'$ 混合角

## MM<sup>2</sup> fits



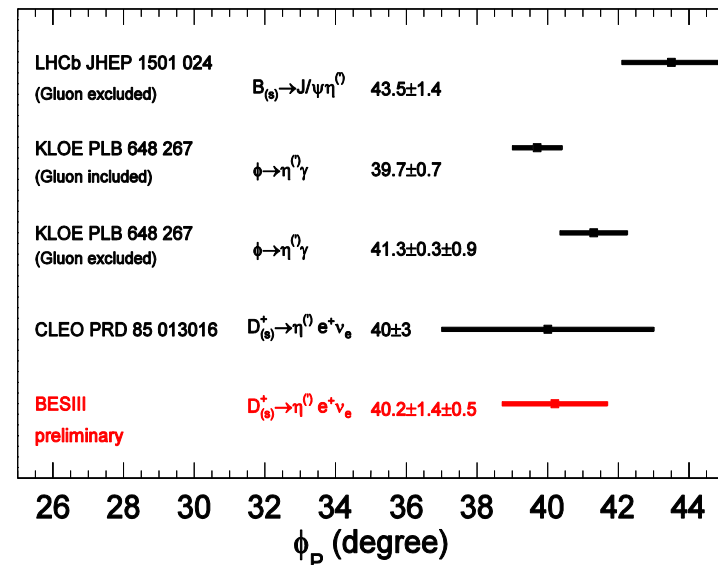
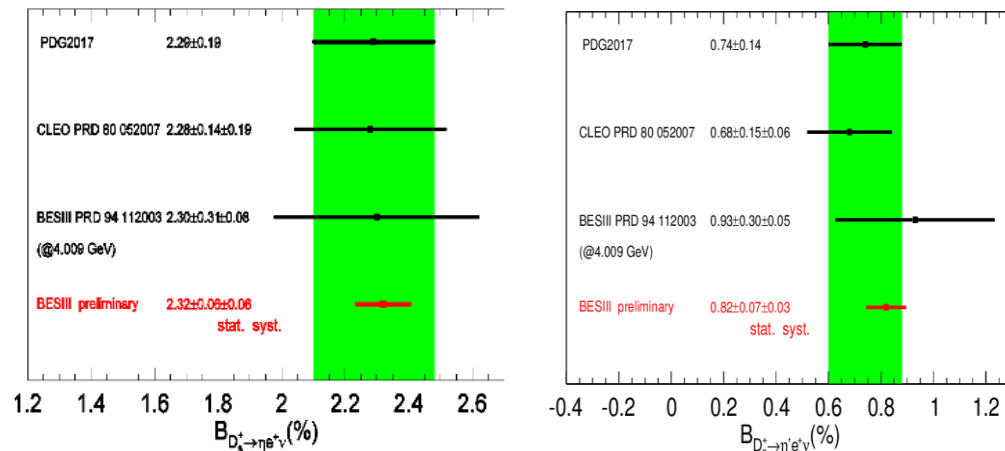
Decay $\eta^{(\prime)}$	decay	$\epsilon_{\gamma(\pi^0)SL} (\%)$	$N_{DT}^{tot}$	$\mathcal{B}_{SL} (\%)$
$\eta e^+ \nu_e$	$\gamma\gamma$	$41.11 \pm 0.27$	$1834 \pm 47$	$2.32 \pm 0.06 \pm 0.06$
	$\pi^0 \pi^+ \pi^-$	$16.06 \pm 0.31$		
$\eta' e^+ \nu_e$	$\eta \pi^+ \pi^-$	$14.07 \pm 0.10$	$261 \pm 22$	$0.82 \pm 0.07 \pm 0.03$
	$\gamma \rho^0$	$18.98 \pm 0.10$		

Combining the branching fractions measured in this work and  $\mathcal{B}[D^+ \rightarrow \eta e^+ \nu] = (10.74 \pm 0.81 \pm 0.51) \times 10^{-4}$ ,  $\mathcal{B}[D^+ \rightarrow \eta' e^+ \nu] = (1.91 \pm 0.51 \pm 0.13) \times 10^{-4}$  (BESIII arxiv: 1803.05570) into below equation, we obtain

## $\eta-\eta'$ mixing angle

$$\frac{\Gamma(D_s^+ \rightarrow \eta' e^+ \nu) / \Gamma(D_s^+ \rightarrow \eta e^+ \nu)}{\Gamma(D^+ \rightarrow \eta' e^+ \nu) / \Gamma(D^+ \rightarrow \eta e^+ \nu)} \simeq \cot^4 \phi_P$$

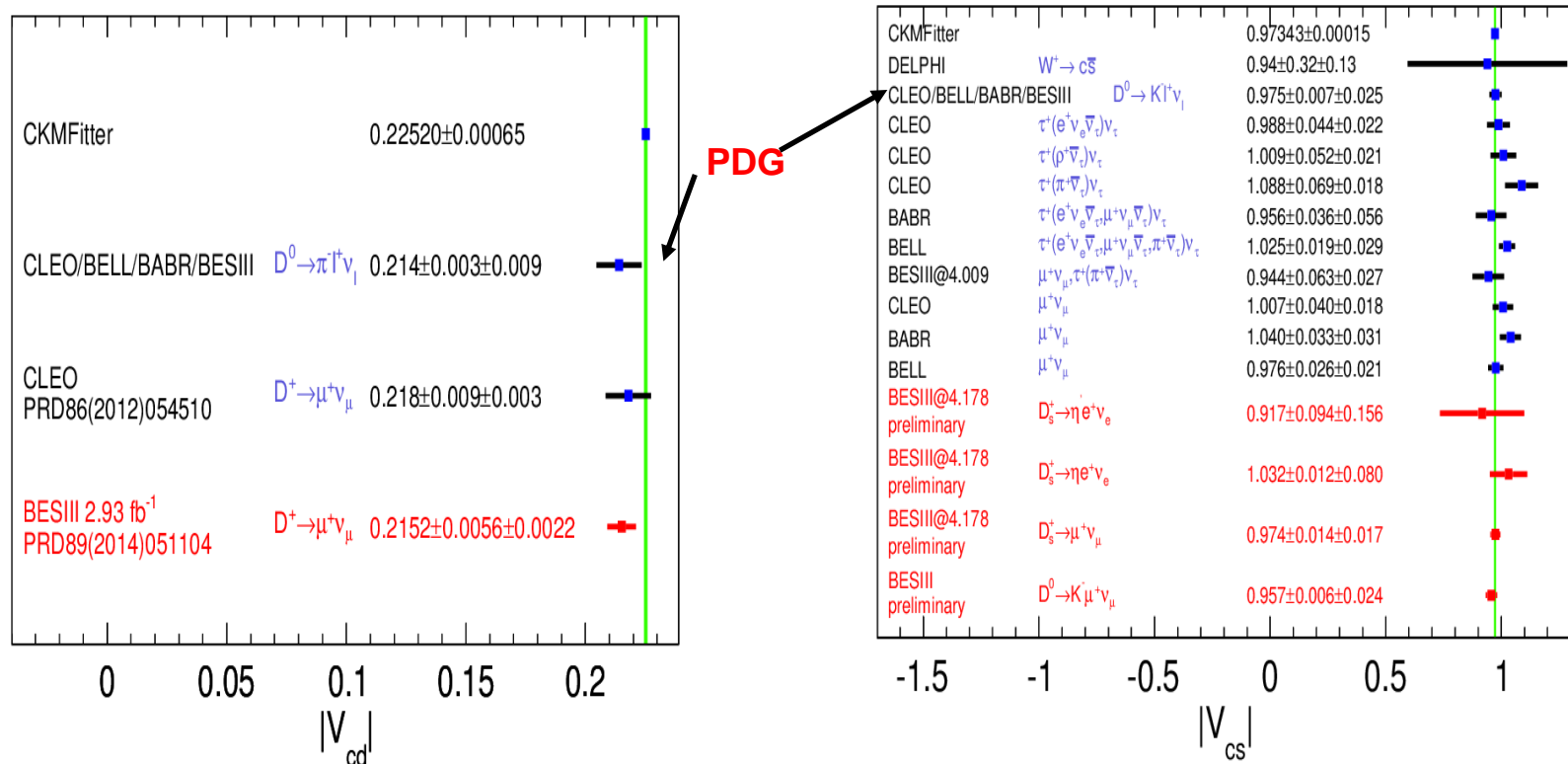
## Comparisons of branching fractions



# BESIII获得最高精度的 $|V_{cs(d)}|$

- **Method 1**  $f_{D(s)}|V_{cd(s)}|$   $|V_{cd(s)}|$
- **Method 2**  $f^{D \rightarrow K(\pi)}_+(0)|V_{cs(d)}|$   $|V_{cs(d)}|$
- **Method 3**  $f^{D(s) \rightarrow \eta}_+(0)|V_{cd(s)}|$   $|V_{cd(s)}|$  ← Limited by both statistics and LQCD input

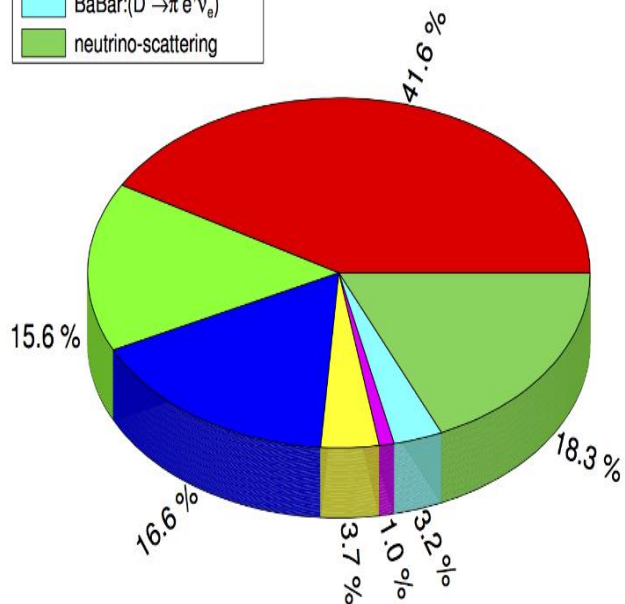
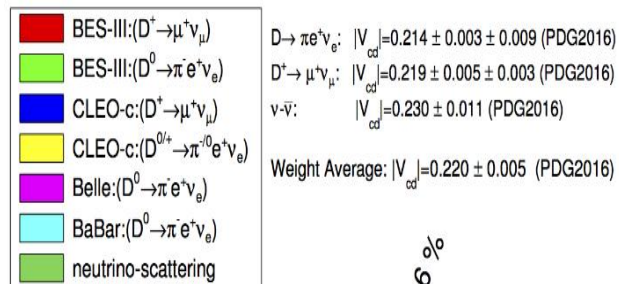
For measurements, the first error is the combined stat. and syst. errors, the second is LQCD uncertainty



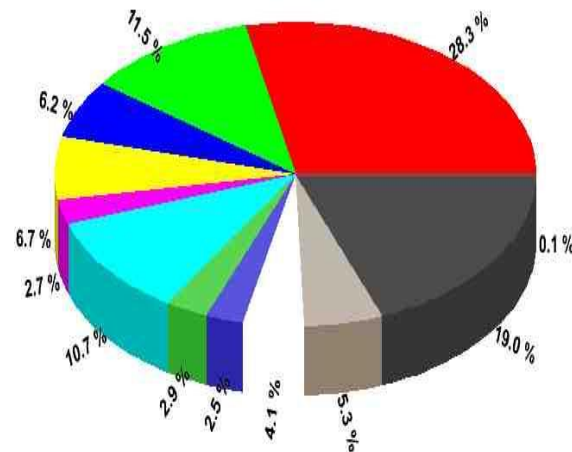
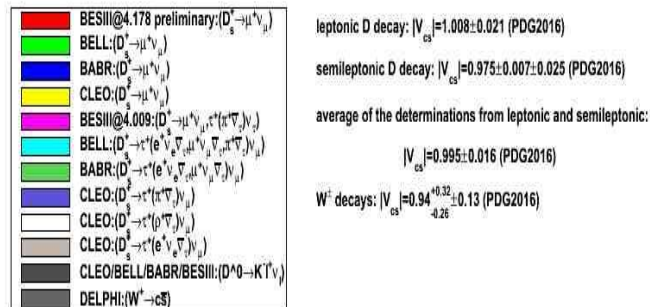
半轻方法受 $f_+^{K(\pi)}(0)$ 格点计算精度限制 **[2.4(4.4)%]**

# 各实验测量对 $|V_{cs(d)}|$ 的权重

**BESIII  $|V_{cd}|$ 权重>50%**



**BESIII  $D_s^+ \rightarrow \mu^+ \nu$ 对 $|V_{cs}|$ 贡献的权重为28%**

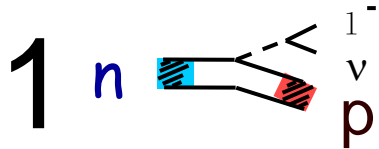


**BESIII  $D_s^+ \rightarrow \tau^+ \nu$ 研究完成后，对 $|V_{cs}|$ 贡献的权重有望达到50%左右**

# CKM矩阵的测量状态[2001→2018]

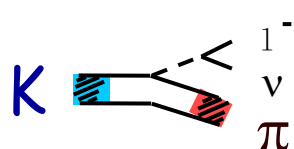
$$\Delta V_{ud}/V_{ud} = 0.1\%$$

0.02%



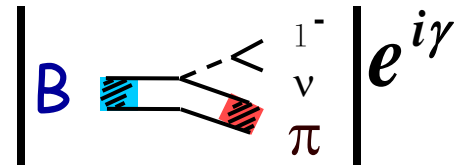
$$\Delta V_{us}/V_{us} = 1\%$$

0.4%



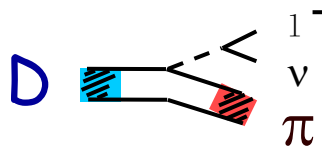
$$\Delta V_{ub}/V_{ub} = 25\%$$

12%



$$\Delta V_{cd}/V_{cd} = 7\%$$

2.3%

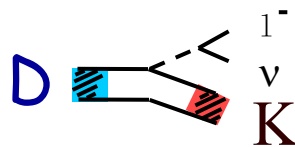


联合  $D^+ \rightarrow l^+ \nu$

BESIII 纯轻结果主导

$$\Delta V_{cs}/V_{cs} = 16\%$$

1.7%

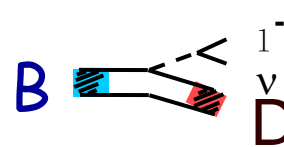


联合  $D_s^+ \rightarrow l^+ \nu$

BESIII 纯轻结果有望  
在未来两年主导

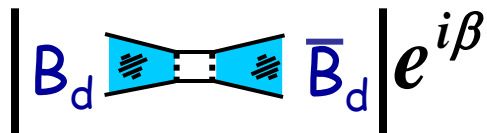
$$\Delta V_{cb}/V_{cb} = 5\%$$

3.1%



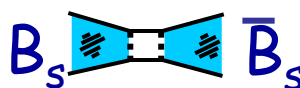
$$\Delta V_{td}/V_{td} = 36\%$$

7.3%



$$\Delta V_{ts}/V_{ts} = 39\%$$

6.8%

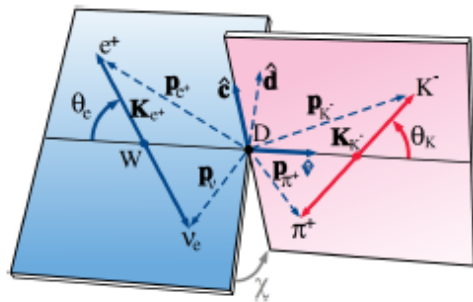


$$\Delta V_{tb}/V_{tb} = 29\%$$

3.1%

1

# D → Ve<sup>+</sup>ν形状因子研究



- $m^2 = (p_{\pi^+} + p_{K^-})^2$

- $\cos(\theta_K) = \frac{\hat{d} \cdot \mathbf{K}_{K^-}}{|\mathbf{K}_{K^-}|}$

- $\cos(\chi) = \hat{e} \cdot \hat{d}$

- $q^2 = (p_{e^+} + p_{\nu_e})^2$

- $\cos(\theta_e) = -\frac{\hat{e} \cdot \mathbf{K}_{e^+}}{|\mathbf{K}_{e^+}|}$

- $\sin(\chi) = (\hat{e} \times \hat{d}) \cdot \hat{d}$

Decay rate depend on 5 variables and 3 form factors

$$d^5\Gamma = \frac{G_F^2 |V_{cs}|^2}{(4\pi)^6 m_D^2} X \beta \mathcal{I}(m^2, q^2, \theta_K, \theta_e, \chi) dm^2 dq^2 d\cos(\theta_K) d\cos(\theta_e) d\chi$$

- $X = p_{K\pi} m_D$ ,  $p_{K\pi}$  is the momentum of the  $K\pi$  system in the  $D$  rest frame
- $\beta = 2p^*/m$ ,  $p^*$  is the breakup momentum of the  $K\pi$  system in its rest frame
- $\mathcal{I}$  can be expressed in terms of helicity amplitudes  $H_{0,\pm}$ :

$$H_0(q^2) = \frac{1}{2m_q} \left[ (m_D^2 - m^2 - q^2)(m_D + m) A_1(q^2) - 4 \frac{m_D^2 p_{K\pi}^2}{m_D + m} A_2(q^2) \right]$$

$$H_{\pm}(q^2) = (m_D + m) A_1(q^2) \mp \frac{2m_D p_{K\pi}}{m_D + m} V(q^2)$$

- Vector form factor:  $V(q^2) = \frac{V(0)}{1 - q^2/m_V^2}$ ; or: FF ratio  $r_V = V(0)/A_1(0)$
- Axial-vector form factor:  $A_1(q^2) = \frac{A_1(0)}{1 - q^2/m_A^2}$ ,  $A_2(q^2) = \frac{A_2(0)}{1 - q^2/m_A^2}$ ; or: FF ratio  $r_2 = A_2(0)/A_1(0)$

Determine FFs in  $D \rightarrow Ve^+\nu$  and understand nature of resonance  $V$  <sup>28</sup>



# $D^+ \rightarrow K^- \pi^+ e^+ \nu$ 振幅分析

PRD94(2016)032001

## Fractions with $>5\sigma$ significance

$$f(D^+ \rightarrow (K^- \pi^+)_{K^{*0}(892)} e^+ \nu_e) = (93.93 \pm 0.22 \pm 0.18)\%$$

$$f(D^+ \rightarrow (K^- \pi^+)_{S\text{-wave}} e^+ \nu_e) = (6.05 \pm 0.22 \pm 0.18)\%$$

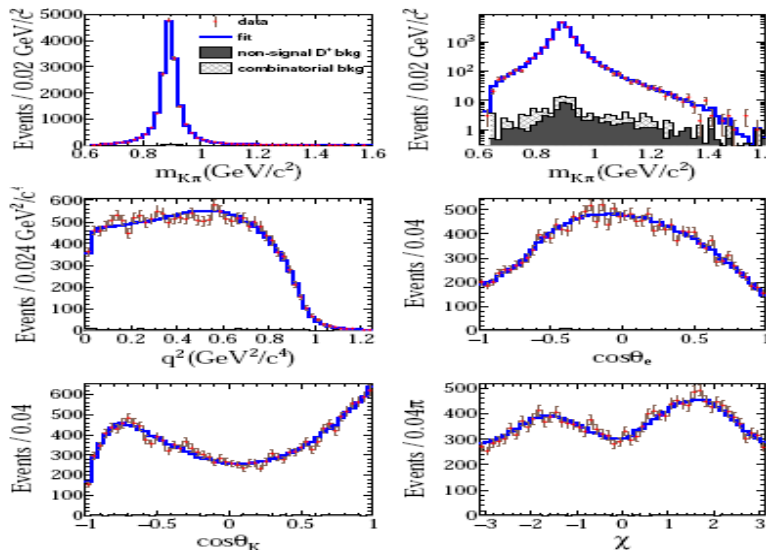
## Properties of different $K\pi$ (non-) resonant amplitudes

$$m_{K^{*0}(892)} = (894.60 \pm 0.25 \pm 0.08) \text{ MeV}/c^2$$

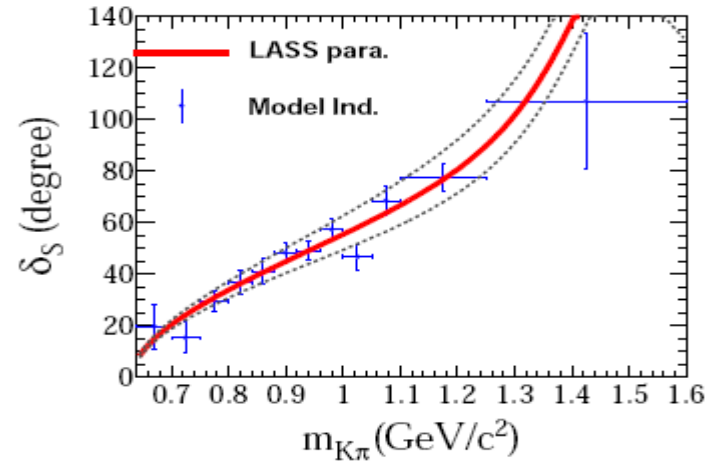
$$\Gamma_{K^{*0}(892)} = (46.42 \pm 0.56 \pm 0.15) \text{ MeV}/c^2$$

$$r_{BW} = (3.07 \pm 0.26 \pm 0.11) (\text{GeV}/c)^{-1}$$

## $q^2$ dependent form factors in $D^+ \rightarrow \bar{K}^{*0}(892) e^+ \nu$



## Model independent S-wave phase measurement



$$V(q^2) = \frac{V(0)}{1 - q^2/m_V^2}, \quad A_{1,2}(q^2) = \frac{A_{1,2}(0)}{1 - q^2/m_A^2}$$

$M_{V/A}$  is expected to  $M_{D^{*(1-/+)}}$

$$m_V = (1.81^{+0.25}_{-0.17} \pm 0.02) \text{ GeV}/c^2$$

$$m_A = (2.61^{+0.22}_{-0.17} \pm 0.03) \text{ GeV}/c^2$$

$$A_1(0) = 0.573 \pm 0.011 \pm 0.020$$

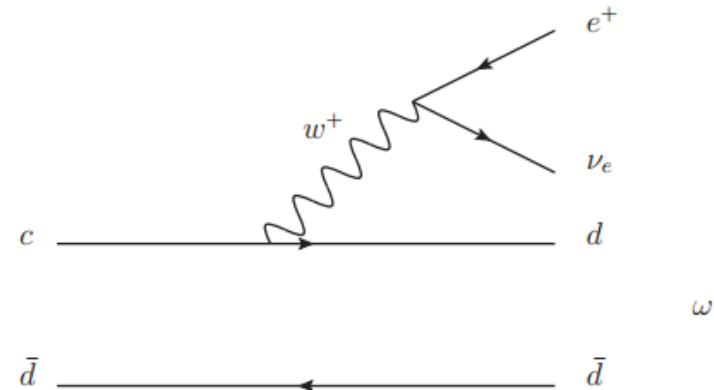
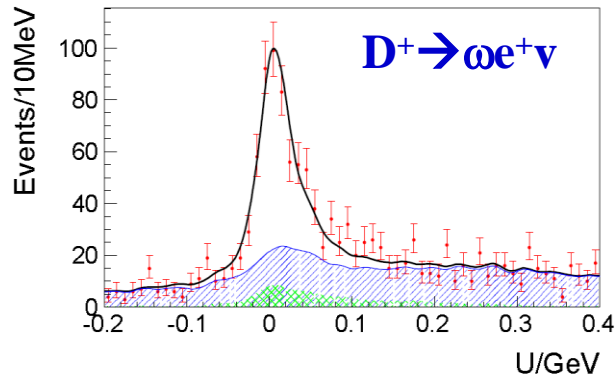
$$r_V = V(0)/A_1(0) = 1.411 \pm 0.058 \pm 0.007$$

$$r_2 = A_2(0)/A_1(0) = 0.788 \pm 0.042 \pm 0.008$$

## Model independent form factors

# $D^+ \rightarrow \omega e^+ \nu$ 振幅分析研究

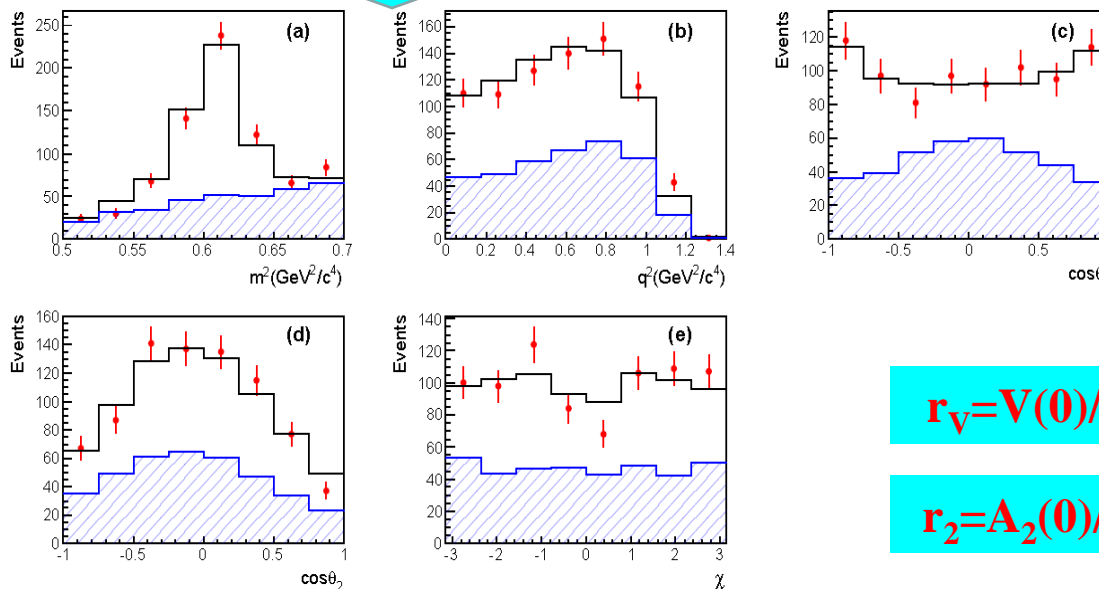
PRD92(2015)071101(RC)



$$B[D^+ \rightarrow \omega e^+ \nu] = (1.63 \pm 0.11 \pm 0.08) \times 10^{-3}$$

Better precision or sensitivity

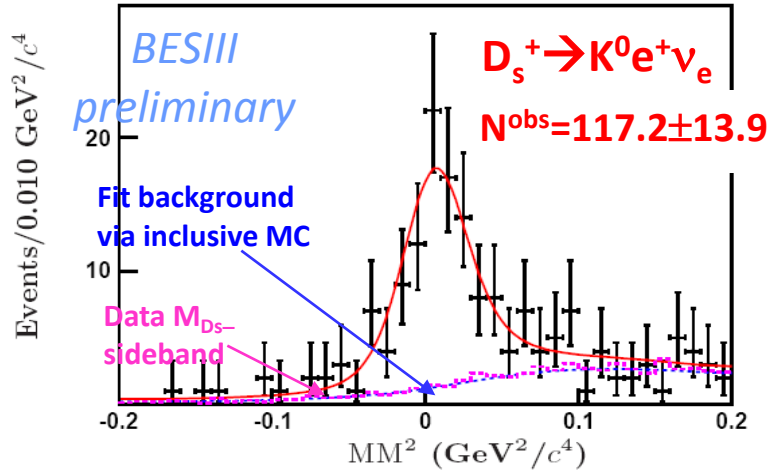
Amplitude analysis of  $D^+ \rightarrow \omega e^+ \nu$  is performed for the first time



$$r_V = V(0)/A_1(0) = 1.24 \pm 0.09 \pm 0.06$$

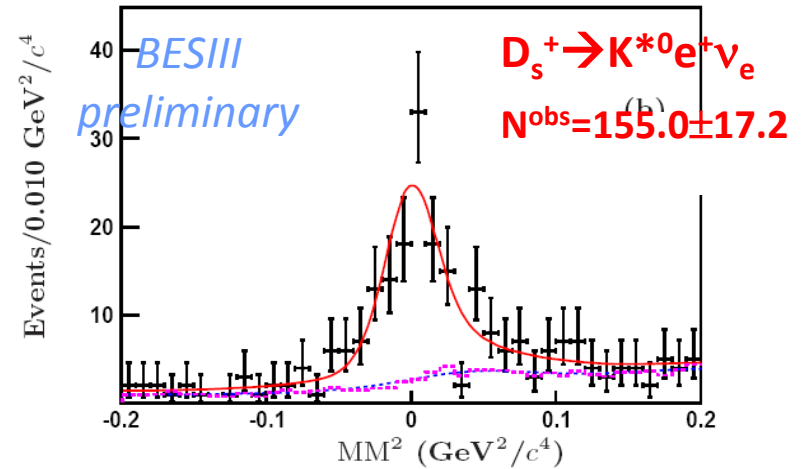
$$r_2 = A_2(0)/A_1(0) = 1.06 \pm 0.15 \pm 0.05$$

# $D_s^+ \rightarrow K^{(*)0} e^+ \nu$ 形状因子的首次测量



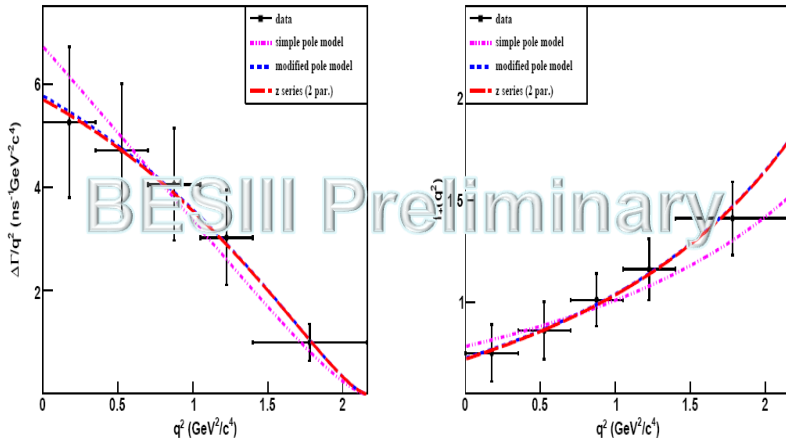
$$B[D_s^+ \rightarrow K^0 e^+ \nu_e] = (3.25 \pm 0.38_{\text{stat}} \pm 0.14_{\text{syst}}) \times 10^{-3}$$

$$(3.9 \pm 0.9) \times 10^{-3} \text{ [PDG17]}$$



$$B[D_s^+ \rightarrow K^{*0} e^+ \nu_e] = (2.38 \pm 0.26_{\text{stat}} \pm 0.12_{\text{syst}}) \times 10^{-3}$$

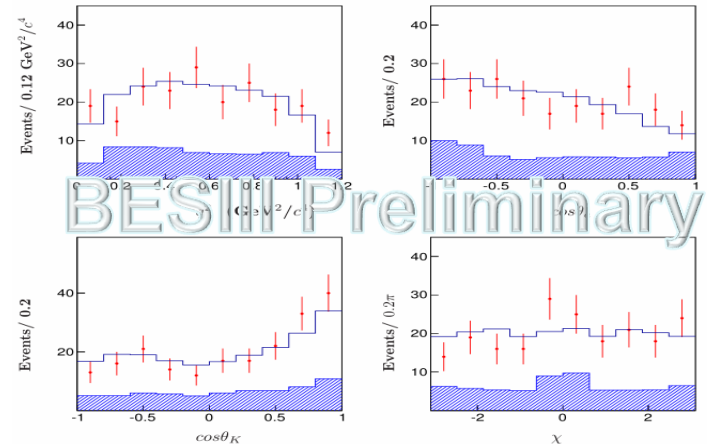
$$(1.8 \pm 0.4) \times 10^{-3} \text{ [PDG17]}$$



Model	Parameter	Value	$f_+(0)$
Simple pole	$f_+(0) V_{cd} $	$0.175 \pm 0.010 \pm 0.001$	$0.778 \pm 0.044 \pm 0.004$
Modified pole model	$f_+(0) V_{cd} $	$0.163 \pm 0.017 \pm 0.003$	$0.725 \pm 0.076 \pm 0.013$
	$\alpha$	$0.45 \pm 0.44 \pm 0.02$	
Series two parameters	$f_+(0) V_{cd} $	$0.162 \pm 0.019 \pm 0.003$	$0.720 \pm 0.084 \pm 0.013$
	$r_1$	$-2.94 \pm 2.32 \pm 0.14$	

Taking  $|V_{CKM}^{\text{fitter}}|_{cd}|$  as input

Four dimensional un-binned likelihood fit is performed.  $K^*$  parameters are fixed



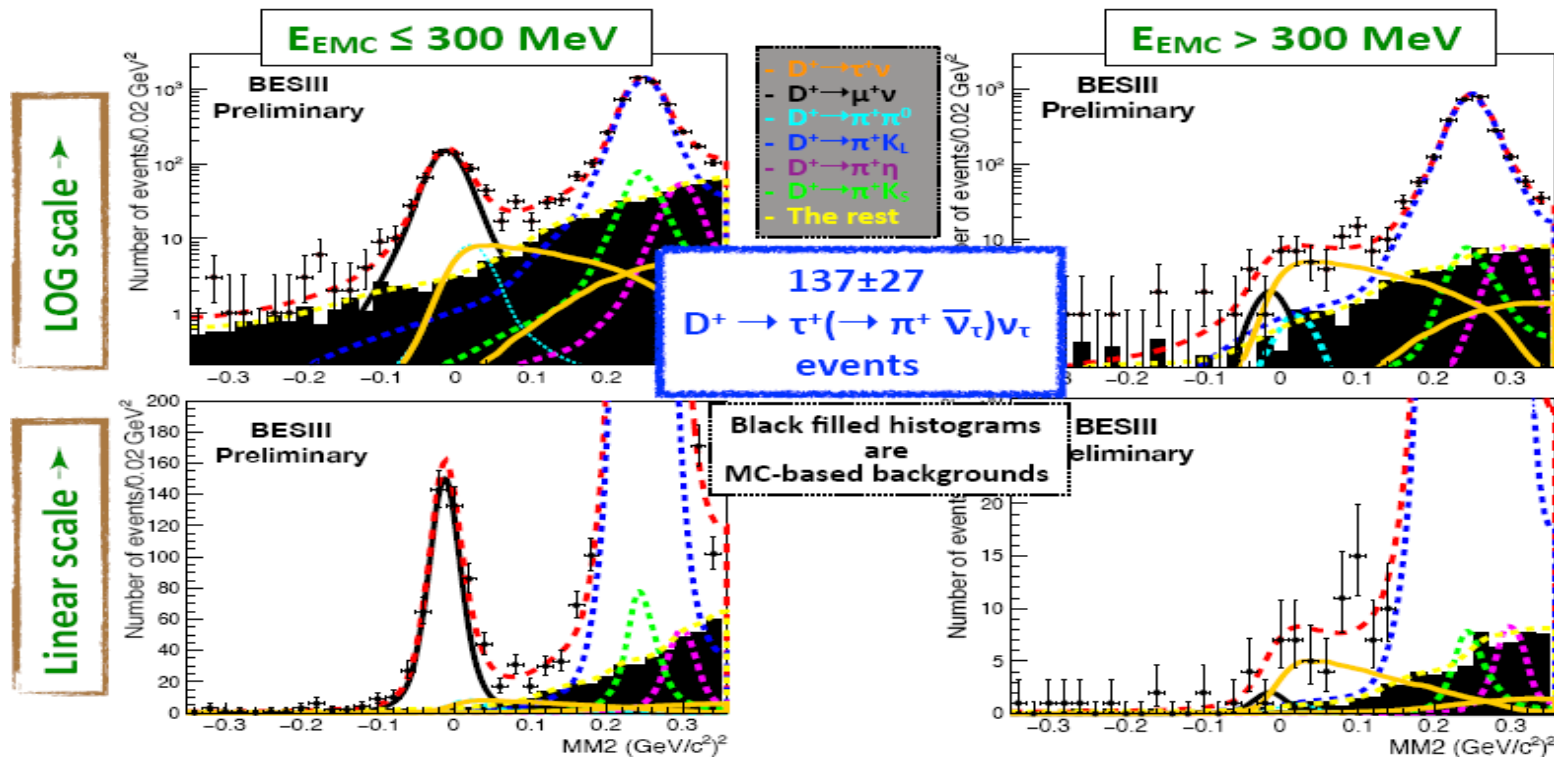
$$r_V = 1.67 \pm 0.34 \pm 0.16$$

$$r_2 = 0.77 \pm 0.28 \pm 0.07$$

# 首次测量 $D^+ \rightarrow \tau^+ \nu$ 和LFU检验

11

## Fitting to DATA



**$4\sigma$**

$$B[D^+ \rightarrow \tau^+ \nu] = (1.20 \pm 0.24_{\text{stat.}}) \times 10^{-3}$$

$$R \equiv \frac{\Gamma(D^+ \rightarrow \tau^+ \nu)}{\Gamma(D^+ \rightarrow \mu^+ \nu)} = \frac{m_{\tau^+}^2 \left(1 - \frac{m_{\tau^+}^2}{M_{D^+}^2}\right)^2}{m_{\mu^+}^2 \left(1 - \frac{m_{\mu^+}^2}{M_{D^+}^2}\right)^2}$$

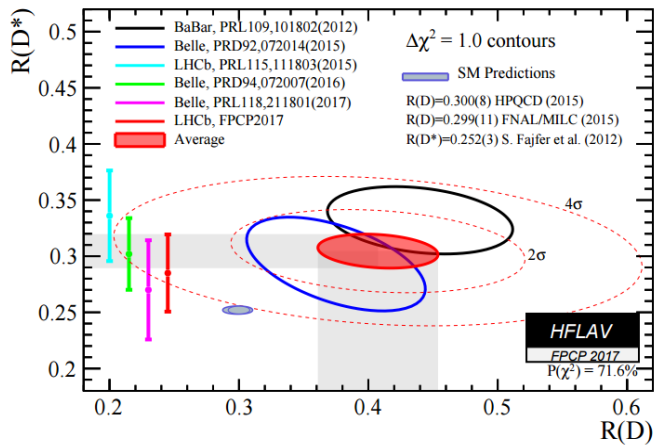
**SM prediction: 2.66**

**BESIII: 3.21±0.64**

# $D^{0(+)} \rightarrow \pi l^+ \nu$ 分支比测量和LFU检验

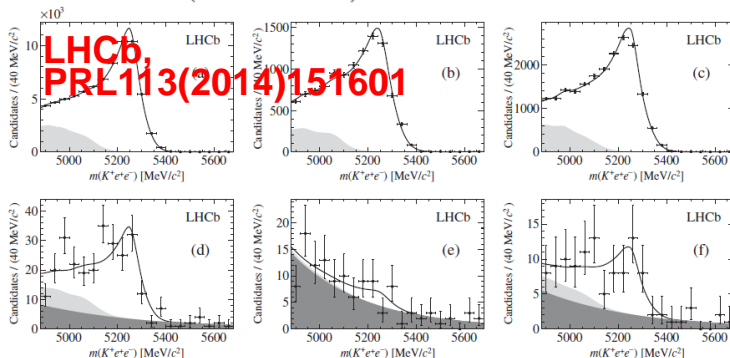
Evidence of violation of LFU at  $4\sigma$  in

$$R(D^{(*)}) = \frac{B(B \rightarrow D^{(*)} \tau \nu)}{B(B \rightarrow D^{(*)} l \nu)}$$



Evidence at  $2.6\sigma$  in FCNC decays  $B^+ \rightarrow K^+ \mu^+ \mu^- / K^+ e^+ e^-$

$$R_K = \frac{\Gamma(\bar{B} \rightarrow \bar{K} \mu^+ \mu^-)}{\Gamma(\bar{B} \rightarrow \bar{K} e^+ e^-)} = 0.745^{+0.090}_{-0.074} \pm 0.036$$

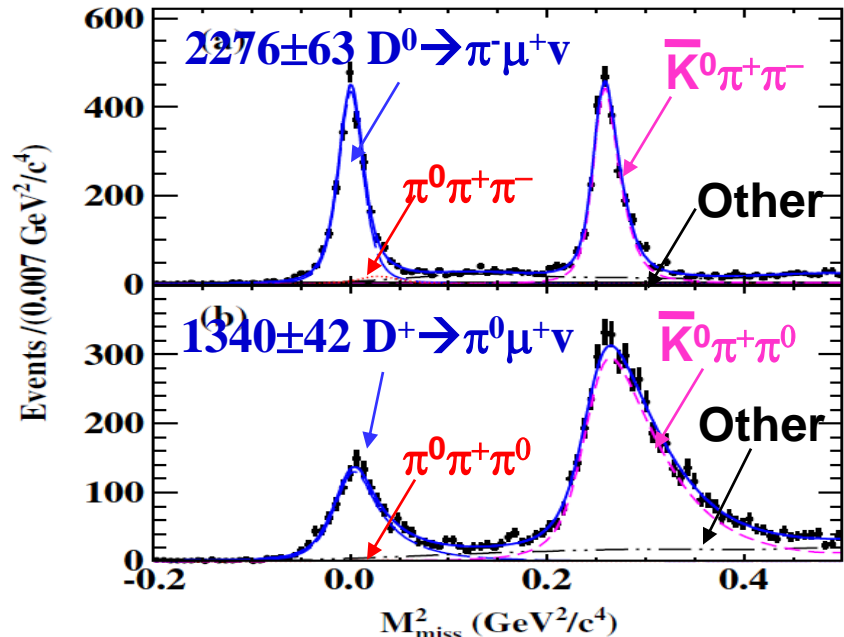


$$R_{LU}^{0(+)} = \frac{B(D^{0(+)} \rightarrow \pi^{-(0)} \mu^+ \nu)}{B(D^{0(+)} \rightarrow \pi^{-(0)} e^+ \nu)} \sim 0.985(2)$$

**B<sup>PDG16</sup>:**  $R_{LU}^0 = 0.82 \pm 0.08$  ( $\sim 2.1\sigma$ )

$$B(D^0 \rightarrow \pi^- \mu^+ \nu) = (0.237 \pm 0.024)\%$$

arXiv:1802.05492, submitted to PRL



$$B[D^0 \rightarrow \pi \mu^+ \nu] = (0.267 \pm 0.007 \pm 0.007)\%$$

$$B[D^+ \rightarrow \pi^0 \mu^+ \nu] = (0.342 \pm 0.011 \pm 0.010)\%$$

$$\mathcal{R}_{LU}^0 = 0.905 \pm 0.027_{\text{stat.}} \pm 0.023_{\text{syst.}}$$

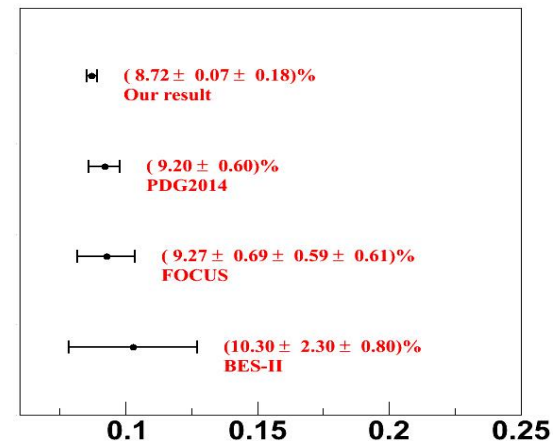
$$\mathcal{R}_{LU}^+ = 0.942 \pm 0.037_{\text{stat.}} \pm 0.027_{\text{syst.}}$$

# $D \rightarrow \bar{K} l^+ \nu$ 分支比或分宽度和LFU检验

EPJC76(2016)369

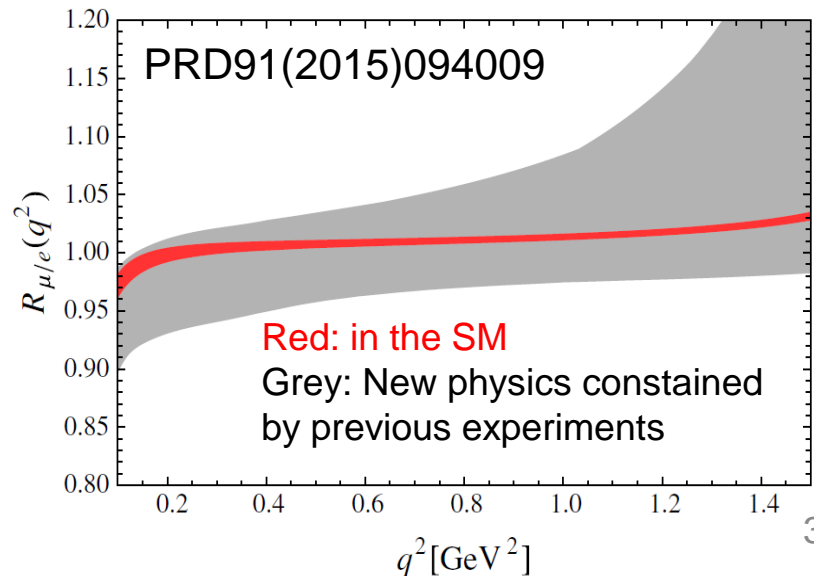
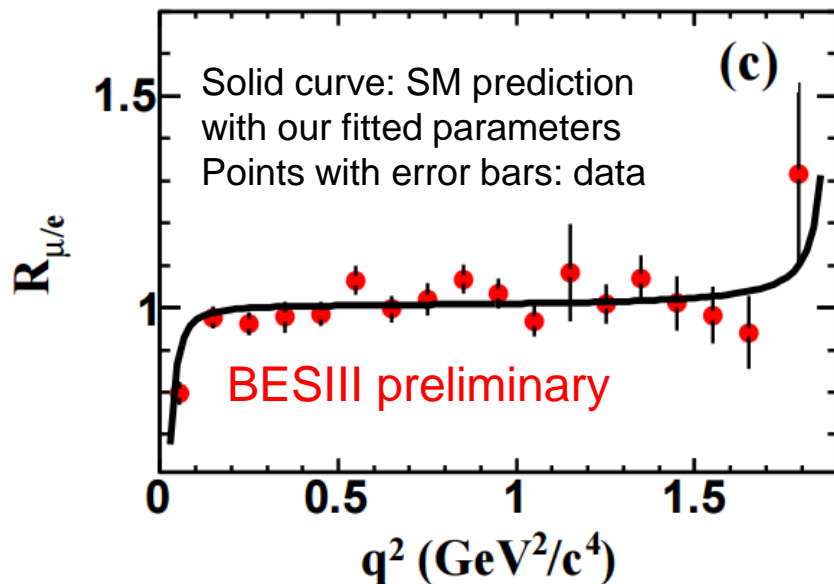
$$\frac{\Gamma[D^+ \rightarrow \bar{K}^0 \mu^+ \nu]}{\Gamma[D^+ \rightarrow \bar{K}^0 e^+ \nu]} = 0.988 \pm 0.033$$

Consistent with theory  
prediction 0.97 within error



BESIII preliminary

$$R_{\mu/e} = \frac{\Gamma(D^0 \rightarrow K^- \mu^+ \nu_\mu)}{\Gamma(D^0 \rightarrow K^- e^+ \nu_e)} = 0.978 \pm 0.007_{stat.} \pm 0.012_{syst.}$$



# $D^+ \rightarrow \text{Se}^+ \nu$ 半轻衰变的首次观测

- Explore the nontrivial internal structure of light mesons, traditional  $q\bar{q}$  states, tetra quark system.
- With chiral unitarity approach in the coupled channels, BF is predicted to be order of  $5(6) \times 10^{-5}$  for  $D^{0(+)}$  decays
- Improve understanding of classification of light scalar mesons

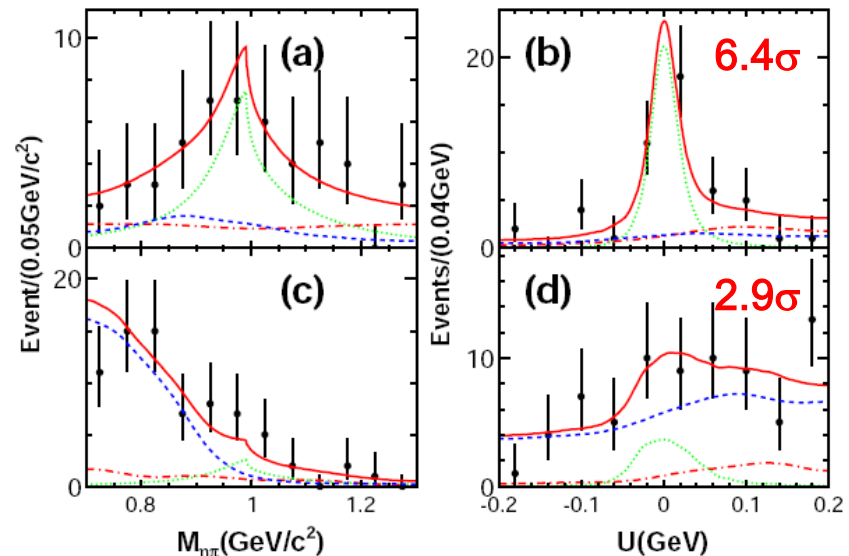
arXiv:1803.02166, accepted by PRL

$$R \equiv \frac{B(D^+ \rightarrow f_0 l^+ \nu) + B(D^+ \rightarrow \sigma l^+ \nu)}{B(D^+ \rightarrow a_0 l^+ \nu)}$$

$R=1(3)$  if traditional  $q\bar{q}$  (tetra quark) system

$$\begin{aligned} & \mathcal{B}(D^+ \rightarrow a_0(980)^0 e^+ \nu_e) \times \mathcal{B}(a_0(980)^0 \rightarrow \eta \pi^0) \\ &= (1.66_{-0.66}^{+0.81} \pm 0.11) \times 10^{-4}, \quad < 3.0 \times 10^{-4} \text{ at the } 90\% \text{ C.L.} \end{aligned}$$

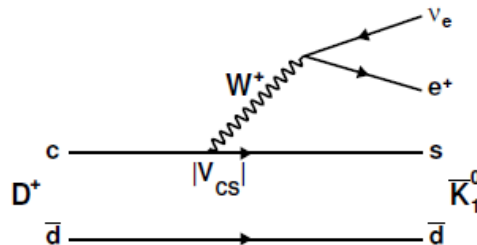
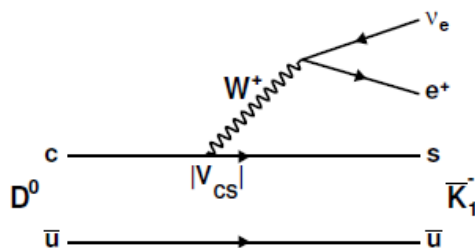
$$\begin{aligned} & \mathcal{B}(D^0 \rightarrow a_0(980)^- e^+ \nu_e) \times \mathcal{B}(a_0(980)^- \rightarrow \eta \pi^-) \\ &= (1.33_{-0.29}^{+0.33} \pm 0.09) \times 10^{-4} \end{aligned}$$



$$\frac{\Gamma(D^0 \rightarrow a_0(980)^- e^+ \nu_e)}{\Gamma(D^+ \rightarrow a_0(980)^0 e^+ \nu_e)} = 2.03 \pm 0.95 \pm 0.06 \quad 35$$



# D $\rightarrow$ Ae $^+$ v半轻衰变的寻找



D $^+$  $\rightarrow\bar{K}_1^0(1270)e^+\nu$ 是CF衰变

D $_s\rightarrow\bar{K}_1^0(1270)e^+\nu$ 是CS衰变

它们应大约满足20倍的关系

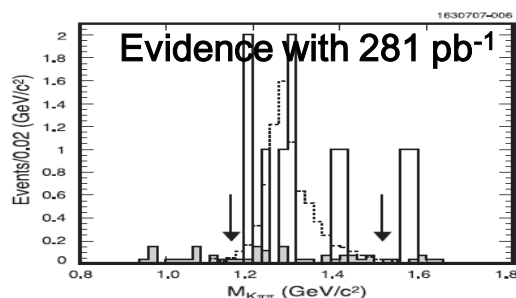
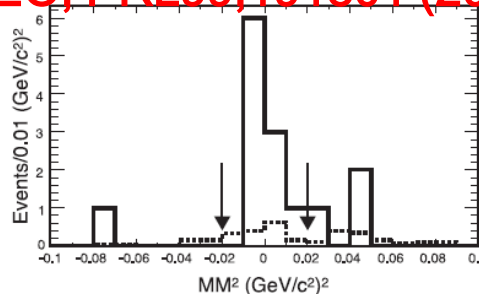
PRD52,2783(1995)预期:  
其占c $\rightarrow$ s $l^+\nu$ 总宽度的2%。  
D $^0\sim$ 0.12% , D $^+\sim$ 0.34%

EPJC77, 587(2017)

**Table 1** Branching fractions of  $D$  and  $D_s$  decays to  $(P, V, S, A)e^+\nu_e$ . Units are shown in parentheses. PDG average values are taken from Ref. [30], while data are not yet available for the  $S$  and  $A$  modes. When the error bar is comparable to the central value, instead we show the minimum and maximum values in the brackets

Channel	$D \rightarrow \pi$	$D \rightarrow \bar{K}$	$D \rightarrow \eta$	$D \rightarrow \eta'$	$D_s \rightarrow K$	$D_s \rightarrow \eta$	$D_s \rightarrow \eta'$
Theory ( $10^{-2}$ )	$0.41 \pm 0.03$	$10.32 \pm 0.93$	$0.12 \pm 0.01$	$0.018 \pm 0.002$	$0.27 \pm 0.02$	$2.26 \pm 0.21$	$0.89 \pm 0.09$
PDG ( $10^{-2}$ )	$0.41 \pm 0.02$	$8.82 \pm 0.13$	$0.11 \pm 0.01$	$0.022 \pm 0.005$	$0.39 \pm 0.09$	$2.29 \pm 0.19$	$0.74 \pm 0.14$
Channel	$D \rightarrow \rho$	$D \rightarrow \omega$	$D \rightarrow \bar{K}^*$	$D_s \rightarrow K^*$	$D_s \rightarrow \phi$		
Theory ( $10^{-2}$ )	$0.23 \pm 0.02$	$0.21 \pm 0.02$	$7.5 \pm 0.7$	$0.19 \pm 0.02$	$3.1 \pm 0.3$		
PDG ( $10^{-2}$ )	$0.22^{+0.02}_{-0.03}$	$0.17 \pm 0.01$	$5.40 \pm 0.10$	$0.18 \pm 0.04$	$2.39 \pm 0.23$		
Channel	$D \rightarrow \omega(1450)$	$D \rightarrow f_0(1500)$	$D \rightarrow f_0(1710)$	$D \rightarrow K_0^*(1450)$	$D_s \rightarrow K_0^*(1450)$	$D_s \rightarrow f_0(1500)$	$D_s \rightarrow f_0(1710)$
Theory ( $10^{-5}$ )	$0.54 \pm 0.05$	$0.11 \pm 0.02$	$(4.7 \pm 0.8) \cdot 10^{-4}$	$29 \pm 3$	$2.7 \pm 0.2$	$15 \pm 3$	$0.034 \pm 0.006$
Channel	$D \rightarrow f_1(1285)$	$D \rightarrow f_1(1420)$	$D \rightarrow h_1(1235)$	$D \rightarrow h_1(1170)$	$D \rightarrow h_1(1380)$	$D_s \rightarrow h_1(1170)$	$D_s \rightarrow h_1(1380)$
Theory ( $10^{-5}$ )	$3.7 \pm 0.8$	$[0.02, 0.14]$	$7.4 \pm 0.7$	$14 \pm 1.5$	$[0, 0.02]$	$[0, 19.7]$	$64 \pm 7$
Channel	$D \rightarrow K_1(1270)$	$D \rightarrow K_1(1400)$	$D_s \rightarrow K_1(1270)$	$D_s \rightarrow K_1(1400)$	$D_s \rightarrow f_1(1285)$	$D_s \rightarrow f_1(1420)$	
Theory ( $10^{-5}$ )	$17 \pm 2$	$[0.03, 0.10]$	$320 \pm 32$	$[1.0, 2.6]$	$[6.0, 36]$	$25 \pm 5$	

CLEO, PRL99,191801 (2007)



EPJC77, 863(2017)

$\mathcal{B}(D^0 \rightarrow K_1^- e^+ \nu_e)$	$350 \pm 40$	$\{0.2', 5'0\}$	$13 \pm 5$	$\{0'02', 0'14\}$
$\mathcal{B}(D^+ \rightarrow K_1^0 e^+ \nu_e)$	$D \rightarrow K_1^0(1530)$	$D \rightarrow K_1^0(1400)$	$D_s \rightarrow K_1^0(1530)$	$D_s \rightarrow K_1^0(1400)$

Table 1

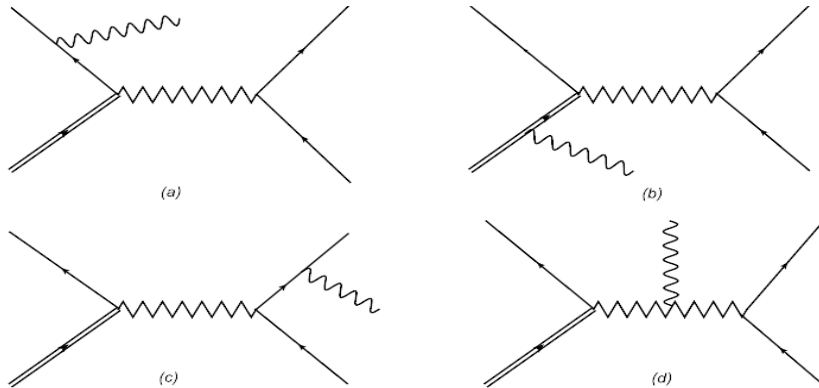
BESIII将首次观测到D $^{0(+)}$  $\rightarrow$ Ae $^+$ v衰变, 相关工作正在开展

$$\mathcal{B}(D^0 \rightarrow K_1^- (1270) e^+ \nu_e) = [7.6^{+4.1}_{-3.0}(\text{stat}) \pm 0.6(\text{syst}) \pm 0.7] \times 10^{-4}$$

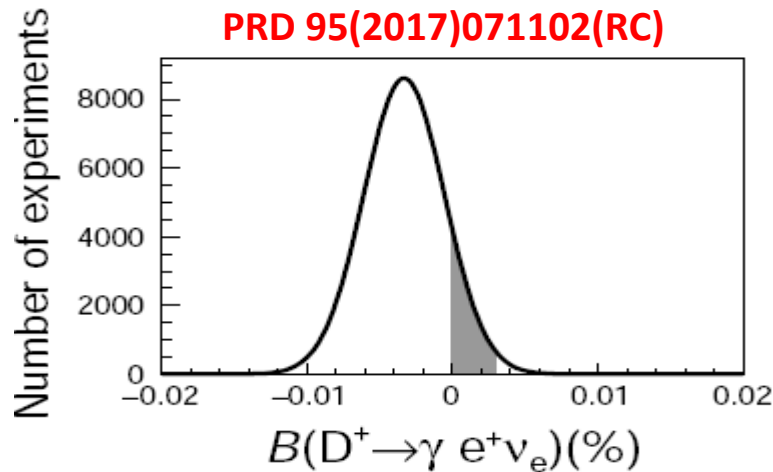


# D介子稀有半轻衰变的寻找

Various theory models  
predict BFs in  $10^{-6}$ – $10^{-4}$

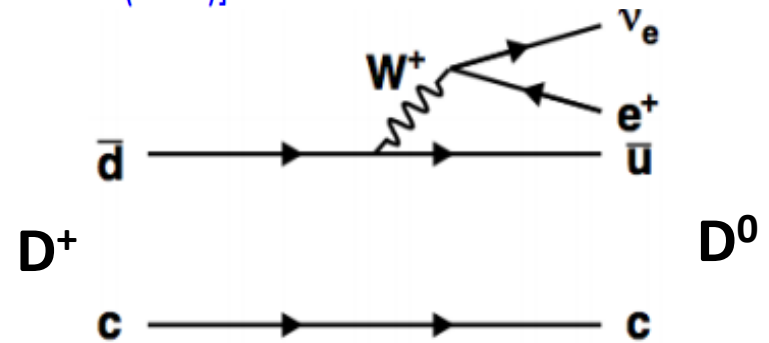


Tree level amplitudes

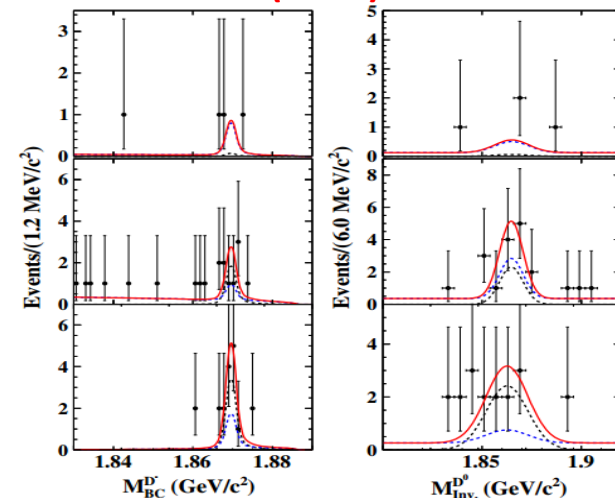


$B[D^+ \rightarrow \gamma e^+ \nu]_{|E_\gamma > 10 \text{ MeV}} < 3.0 \times 10^{-4}$   
@90% C.L.

Applying the SU(3) symmetry for the light quarks, this rare decay branching fraction can be predicted by theoretical calculation and its theoretical value is  $2.78 \times 10^{-13}$  [EPJC, 59:841-845(2009)].



PRD 96(2017)092002



$B[D^+ \rightarrow D^0 e^+ \nu] < 1 \times 10^{-4}$  @90% C.L.

# $D_{(s)}$ 强子衰变

- $D^0\bar{D}^0$  mixing parameters
- Strong phase difference
- SU(3) symmetry and break effect

# BESIII测得 $D^0\bar{D}^0$ 混合参数 $y_{CP}$

■ BESIII, 3 fb<sup>-1</sup> at 3.773 GeV

PLB744(2015)339

For D decay to CP eigenstates:

$$R_{CP\pm} \propto |A_{CP\pm}|^2 (1 \mp y_{CP})$$

$$y_{CP} = \frac{1}{2} [y \cos \phi (|\frac{q}{p}| + |\frac{p}{q}|) - x \sin \phi (|\frac{q}{p}| - |\frac{p}{q}|)]$$

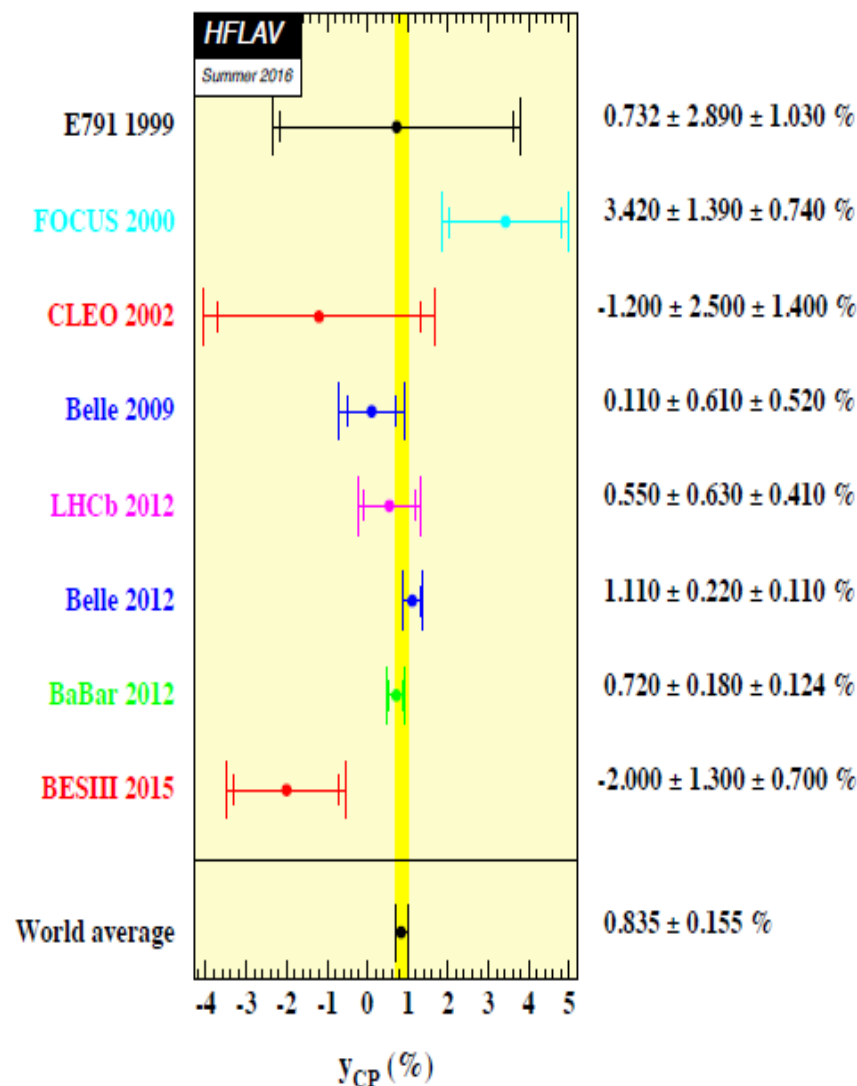
For CP tagged semileptonic D decays:

$$R_{l,CP\pm} \propto |A_l|^2 |A_{CP\pm}|^2$$

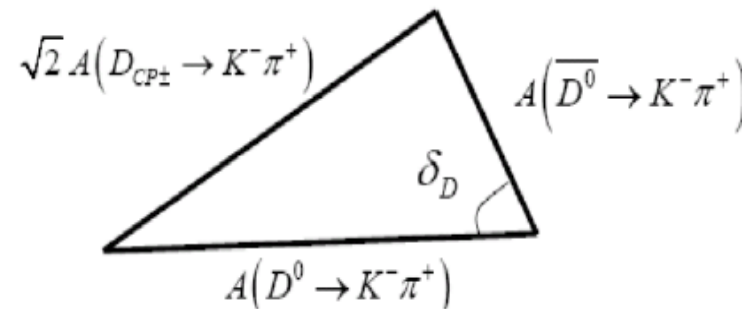
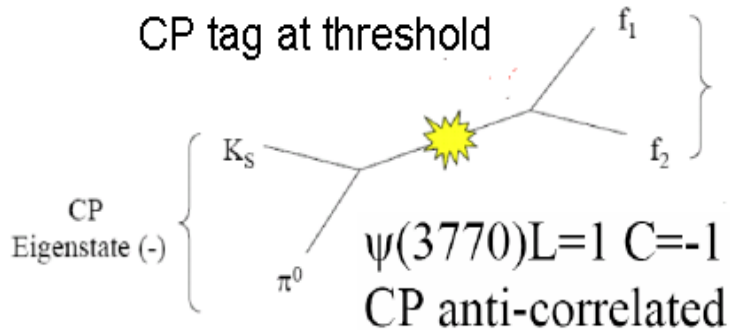
$$y_{CP} \approx \frac{1}{4} \left( \frac{R_{l,CP+} R_{CP-}}{R_{l,CP-} R_{CP+}} - \frac{R_{l,CP-} R_{CP+}}{R_{l,CP+} R_{CP-}} \right)$$

Type	Modes
$CP^+$	$K^+ K^-, \pi^+ \pi^-, K_S^0 \pi^0 \pi^0$
$CP^-$	$K_S^0 \pi^0, K_S^0 \omega, K_S^0 \eta$
$l^\pm$	$K e \nu, K \mu \nu$

$$y_{CP} = (-2.0 \pm 1.3 \pm 0.7) \%$$



# BESIII测得 $D^0\bar{D}^0$ 混合参数 $\delta_{K\pi}$



$$\mathcal{A}_{CP \rightarrow K\pi} = \frac{\mathcal{B}_{D_2 \rightarrow K^- \pi^+} - \mathcal{B}_{D_1 \rightarrow K^- \pi^+}}{\mathcal{B}_{D_2 \rightarrow K^- \pi^+} + \mathcal{B}_{D_1 \rightarrow K^- \pi^+}}.$$

$$2r \cos \delta_{K\pi} + y = (1 + R_{WS}) \cdot \mathcal{A}_{CP \rightarrow K\pi},$$

$$|D_1\rangle \equiv \frac{|D^0\rangle + |\bar{D}^0\rangle}{\sqrt{2}} \quad |D_2\rangle \equiv \frac{|D^0\rangle - |\bar{D}^0\rangle}{\sqrt{2}}.$$

$\delta_{K\pi}$  is related to mixing parameters  $x$  and  $y$  from  $x'$  and  $y'$

目前最精确结果

$$A^{K\pi}_{CP} = (12.7 \pm 1.3 \pm 0.7) \times 10^{-2}$$

$$\cos \delta_{K\pi} = 1.02 \pm 0.11 \pm 0.06 \pm 0.01$$

PLB734(2014)227

Type	Mode
Flavored	$K^- \pi^+, K^+ \pi^-$
CP+	$K^+ K^-, \pi^+ \pi^-, K_S^0 \pi^0 \pi^0, \pi^0 \pi^0, \rho^0 \pi^0$
CP-	$K_S^0 \pi^0, K_S^0 \eta, K_S^0 \omega$

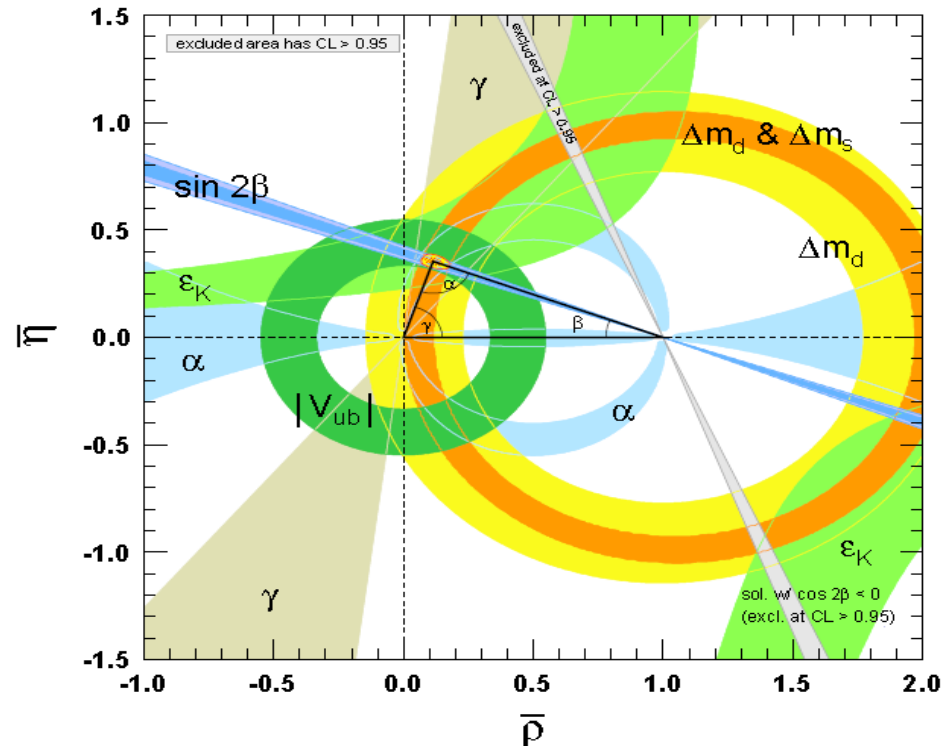
# $D^0$ 衰变强相差: 约束 $\gamma/\phi_3$ 的理想桥梁

## Direct measurement

$$\alpha/\phi_2 = (85.4^{+4.0}_{-3.9})^\circ$$
$$\beta/\phi_1 = (21.38^{+0.79}_{-0.77})^\circ$$
$$\gamma/\phi_3 = (68^{+8.0}_{-8.5})^\circ$$

$\gamma$  is the worst measured angle,  
mostly due to systematic error

Significant deviation from UT will  
imply NP beyond SM



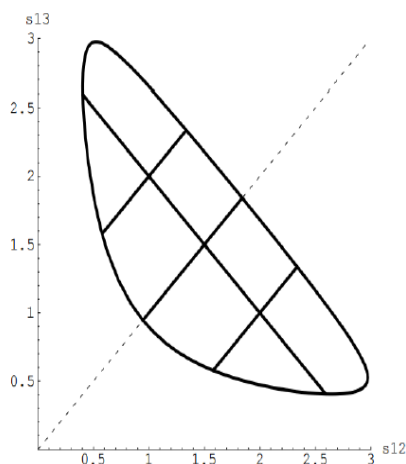
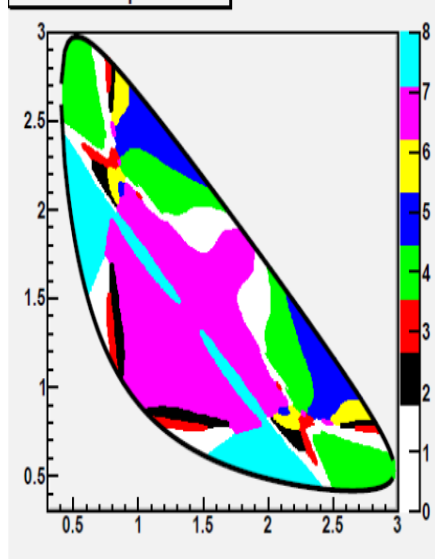
## ■ Quantum correlated $D^0\bar{D}^0$ decays in $\psi(3770)$

➤ CP asymmetry in mixing and decays

➤ Interference  $\rightarrow$  strong phase parameters  $\rightarrow$  Constrain  $\gamma/\phi_3$ , which is important for CKM UT

# $D^0 \rightarrow K_S \pi^+ \pi^-$ 衰变强相差研究

Babar 2008 Optimal Bins



Mirrored binning over  $x=y$  makes it so  $c_i = c_i$  and  $s_i = -s_i$

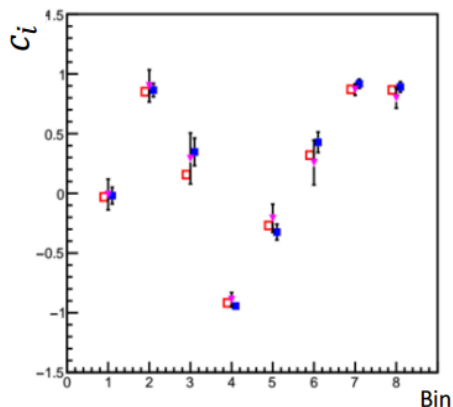
Model prediction

BESIII  
CLEO-c

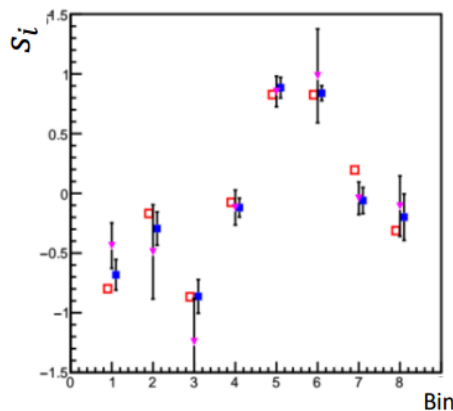
**BESIII preliminary**

**CLEO, PRD82, 112006**

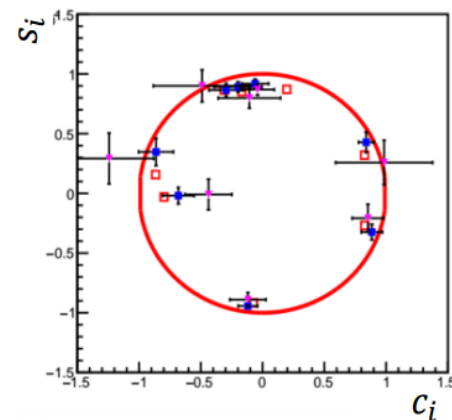
$c_i$



$s_i$



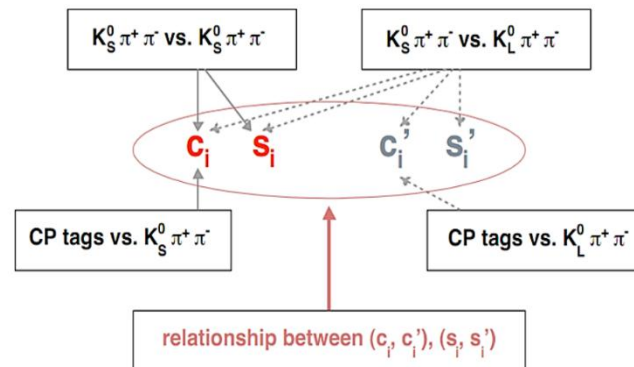
$c_i s_i$



- $T_i$ : Bin yield measured in flavor decays
- $r_B$ : color suppression factor  $\sim 0.1$
- $\delta_B$ : strong phase of B decay
- $c_i, s_i$ : weighted average of  $\cos(\Delta\delta_D)$  and  $\sin(\Delta\delta_D)$  respectively where  $\Delta\delta_D$  is the difference between phase of  $D^0$  and  $D^0$

Measured at B-Factories

Through  $D^0 \rightarrow K_S \pi^+ \pi^-$  analysis



# $D^0$ 衰变强相差对 $\gamma/\phi_3$ 的约束及前景

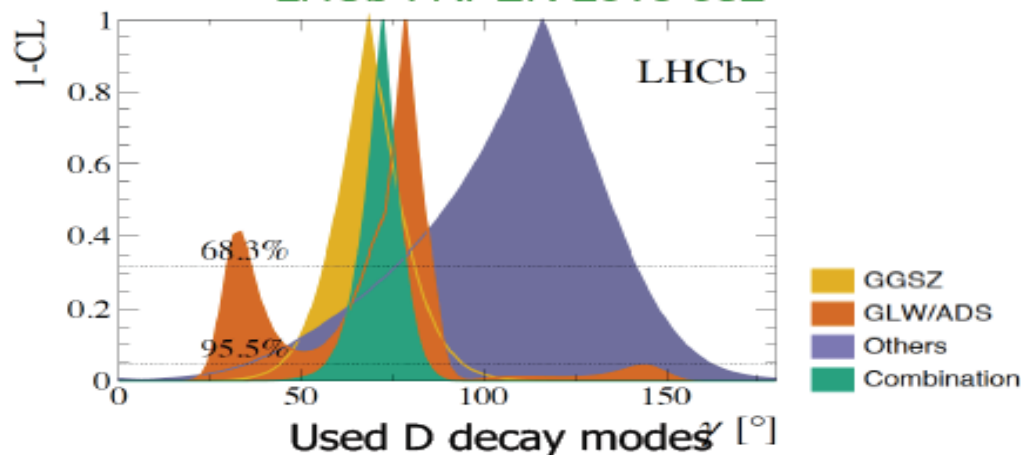
taken from Liming Zhang's talk at FPCPV2016



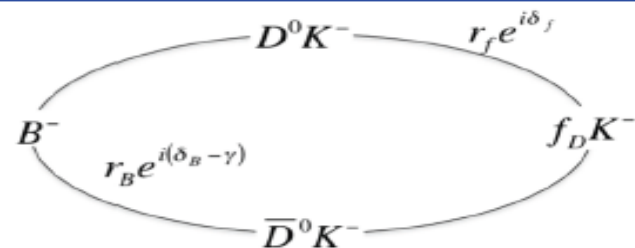
## $\gamma$ combination at LHCb

Determine  $\gamma$  from CPV measurements

LHCb-PAPER-2016-032



GLW:  $D \rightarrow K^+ K^- \pi^+ \pi^-$   
 $K_S^0 \pi^0$   
 ADS:  $D \rightarrow \pi^+ K^-$   
 quasi-ADS:  $D \rightarrow \pi^+ K^- \pi^+ \pi^-$   
 $\pi^+ K^- \pi^0$   
 GGSZ:  $D \rightarrow K_S^0 \pi^+ \pi^-$   
 $K_S^0 K^+ K^-$   
 quasi-GLW:  $D \rightarrow \pi^+ \pi^- \pi^+ \pi^-$   
 $K^+ K^- \pi^0$   
 $\pi^+ \pi^- \pi^0$   
 GLS:  $D \rightarrow K_S^0 K^+ \pi^+$   
 $K_S^0 \pi^+ K^+$



$$\gamma = (72.2_{-7.3}^{+6.8})^\circ \text{ syst. included}$$

BaBar:  $\gamma = (70 \pm 18)^\circ$

Belle:  $\gamma = (73^{+13}_{-15})^\circ$

### Prospects

Sample	$\sigma_{\text{stat}}(\gamma)^\circ$
Run 1	8
Run 2	4
Upgrade	$\sim 1$
Future upgrade	$< 0.5$

- Current one syst.  $\sim 2^\circ$  from CLEO strong phase measurements
- 15-20  $\text{fb}^{-1}$   $\psi(3770)$  data from BESIII are desired to avoid syst. limitation for upgrade scenario

More 15  $\text{fb}^{-1}$   $\psi(3770)$  data@BESIII will avoid syst. limitation for  $\gamma/\phi_3$  measurement

# SU(3)对称性及破坏效应

- Ratio of branching fractions of D to KK and pi pi

$$R = \frac{Br(D^0 \rightarrow K^+ K^-)}{Br(D^0 \rightarrow \pi^+ \pi^-)} \approx 2.8$$

- R=1 in the SU(3) flavour symmetry limit
- Branching fraction of  $\mathcal{B}(D^0 \rightarrow K^0 \bar{K}^0) = (0.320 \pm 0.038) \times 10^{-3}$  vanishes in the SU(3) limit
- DDbar mixing parameters
$$x, y \sim \sin^2 \theta_C \times [SU(3) \text{ breaking}]^2$$
- Non-zero mixing parameters indicate large SU(3) breaking effect



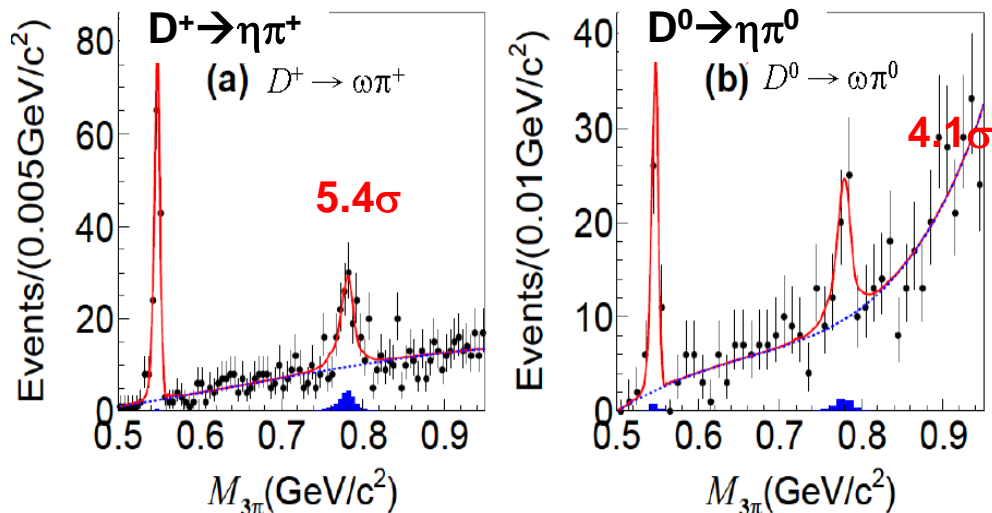
# 两体D衰变分支比的理论计算

Modes	Amplitudes	Br(FSI)	Br(diagrammatic)	Br(pole)	Br(FAT)	Br(FAT[mix])	Br(exp)
$D^0 \rightarrow \pi^+ \rho^-$	$T_V, (E_P)$	6.5	$3.92 \pm 0.46$	$3.5 \pm 0.6$	4.74	4.66	$4.96 \pm 0.24$
$D^0 \rightarrow \pi^0 \rho^0$	$C_P, C_V, (E_P, E_V)$	1.7	$2.96 \pm 0.98$	$1.4 \pm 0.6$	3.55	3.83	$3.72 \pm 0.22$
$D^0 \rightarrow \pi^0 \omega$	$C_P, C_V, (E_P, E_V)$	0.08	$0.10 \pm 0.18$	$0.08 \pm 0.02$	0.85	0.18	$< 0.26$
$D^0 \rightarrow \pi^0 \phi$	$C_P$	1.1	$1.22 \pm 0.08$	$1.0 \pm 0.3$	1.11	1.11	$1.31 \pm 0.10$
$D^0 \rightarrow \pi^- \rho^+$	$T_P, (E_V)$	8.2	$8.34 \pm 1.69$	$10.2 \pm 1.5$	10.2	10.0	$9.8 \pm 0.4$
$D^0 \rightarrow K^+ K^{*-}$	$T_V, (E_P)$	2.8	$1.99 \pm 0.24$	$1.6 \pm 0.3$	1.72	1.73	$1.56 \pm 0.12$
$D^0 \rightarrow K^0 \bar{K}^{*0}$	$E_P, E_V$	0.99	$0.29 \pm 0.22$	$0.16 \pm 0.05$	1.1	1.1	$< 1$
$D^0 \rightarrow \bar{K}^0 K^{*0}$	$E_P, E_V$	0.99	$0.29 \pm 0.22$	$0.16 \pm 0.05$	1.1	1.1	$< 0.56$
$D^0 \rightarrow K^- K^{*+}$	$T_P, (E_V)$	4.5	$4.25 \pm 0.86$	$4.7 \pm 0.8$	4.37	4.37	$4.38 \pm 0.21$
$D^0 \rightarrow \eta \rho^0$	$C_P, C_V, (E_P, E_V)$	0.24	$1.11 \pm 0.86$	$0.05 \pm 0.01$	0.54	0.45	
$D^0 \rightarrow \eta \omega$	$C_P, C_V, (E_P, E_V)$	1.9	$3.08 \pm 1.42$	$1.2 \pm 0.3$	2.4	2.0	
$D^0 \rightarrow \eta \phi$	$C_P, (E_P, E_V)$	0.57	$0.31 \pm 0.10$	$0.23 \pm 0.06$	0.19	0.18	$0.14 \pm 0.05$
$D^0 \rightarrow \eta' \rho^0$	$C_P, C_V, (E_P, E_V)$	0.10	$0.14 \pm 0.02$	$0.08 \pm 0.02$	0.21	0.27	
$D^0 \rightarrow \eta' \omega$	$C_P, C_V, (E_P, E_V)$	0.001	$0.07 \pm 0.02$	$0.0001 \pm 0.0001$	0.04	0.02	
$D^+ \rightarrow \pi^+ \rho^0$	$T_V, C_P, (A_P, A_V)$	1.7		$0.8 \pm 0.7$	0.42	0.58	$0.81 \pm 0.15$
$D^+ \rightarrow \pi^+ \omega$	$T_V, C_P, (A_P, A_V)$	0.35		$0.3 \pm 0.3$	0.95	0.80	$< 0.34$
$D^+ \rightarrow \pi^+ \phi$	$C_P$	5.9	$6.21 \pm 0.43$	$5.1 \pm 1.4$	5.65	5.65	$5.42^{+0.22}_{-0.24}$
$D^+ \rightarrow \pi^0 \rho^+$	$T_P, C_V, (A_P, A_V)$	3.7		$3.5 \pm 1.6$	2.7	2.5	
$D^+ \rightarrow K^+ \bar{K}^{*0}$	$T_V, (A_V)$	2.5		$4.1 \pm 1.0$	3.61	3.60	$3.675^{+0.14}_{-0.21}$
$D^+ \rightarrow \bar{K}^0 K^{*+}$	$T_P, (A_P)$	1.70		$12.4 \pm 2.4$	11	11	$32 \pm 14$
$D^+ \rightarrow \eta \rho^+$	$T_P, C_V, (A_P, A_V)$	0.002		$0.4 \pm 0.4$	0.7	2.2	$< 15$
$D^+ \rightarrow \eta' \rho^+$	$T_P, C_V, (A_P, A_V)$	1.3		$0.8 \pm 0.1$	0.7	0.8	
$D_s^+ \rightarrow \pi^+ K^{*0}$	$T_V, (A_V)$	3.3		$1.5 \pm 0.7$	2.52	2.35	$2.25 \pm 0.39$
$D_s^+ \rightarrow \pi^0 K^{*+}$	$C_V, (A_V)$	0.29		$0.1 \pm 0.1$	0.8	1.0	
$D_s^+ \rightarrow K^+ \rho^0$	$C_P, (A_P)$	2.4		$1.0 \pm 0.6$	1.9	2.5	$2.7 \pm 0.5$
$D_s^+ \rightarrow K^+ \omega$	$C_P, (A_P)$	0.72		$1.8 \pm 0.7$	0.6	0.07	$< 2.4$
$D_s^+ \rightarrow K^+ \phi$	$T_V, C_P, (A_V)$	0.15		$0.3 \pm 0.3$	0.166	0.166	$0.184 \pm 0.045$
$D_s^+ \rightarrow K^0 \rho^+$	$T_P, (A_P)$	19.5		$7.5 \pm 2.1$	9.1	9.6	
$D_s^+ \rightarrow \eta K^{*+}$	$T_P, C_V, (A_P, A_V)$	0.24		$1.0 \pm 0.4$	0.2	0.2	
$D_s^+ \rightarrow \eta' K^{*+}$	$T_P, C_V, (A_P, A_V)$	0.24		$0.6 \pm 0.2$	0.2	0.2	

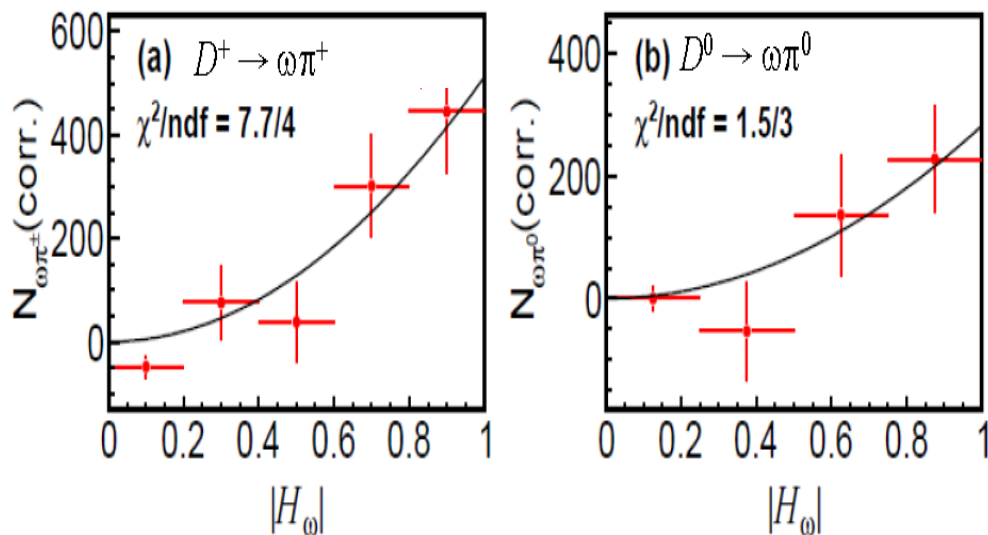
# D→VP衰变 $\omega\pi$ 的首次观测

## Double tag method

PRL116(2016)082001



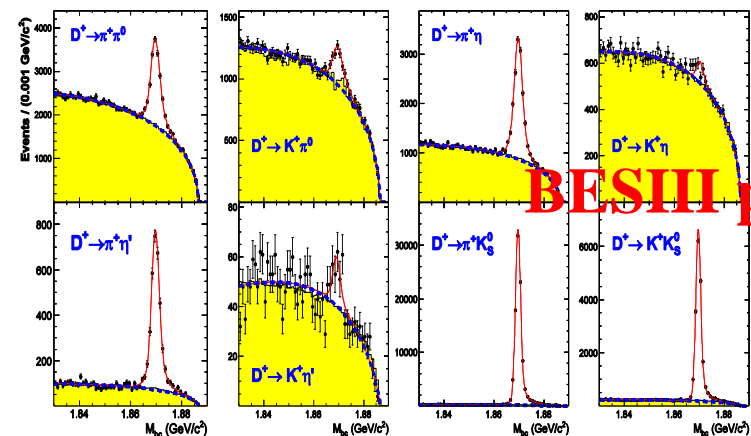
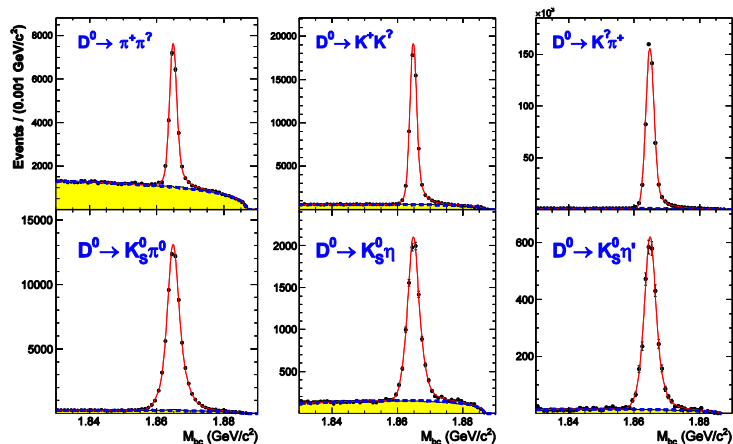
Decay mode	This work	Previous measurements
$D^+ \rightarrow \omega\pi^+$	$(2.74 \pm 0.58 \pm 0.17) \times 10^{-4}$	$< 3.4 \times 10^{-4}$ at 90% C.L.
$D^0 \rightarrow \omega\pi^0$	$(1.05 \pm 0.41 \pm 0.09) \times 10^{-4}$	$< 2.6 \times 10^{-4}$ at 90% C.L.
$D^+ \rightarrow \eta\pi^+$	$(3.13 \pm 0.22 \pm 0.19) \times 10^{-3}$	$(3.53 \pm 0.21) \times 10^{-3}$
$D^0 \rightarrow \eta\pi^0$	$(0.67 \pm 0.10 \pm 0.05) \times 10^{-3}$	$(0.68 \pm 0.07) \times 10^{-3}$



**Studies of singly cabibbo-suppressed decays is limited by data set and background**

**Benefit the understanding of SU(3) symmetry breaking and CP violation, improve theory calculation**

# D<sup>0</sup>(<sup>+</sup>) → PP 分支比的改进测量



BESIII preliminary

- ◆ The study of the hadronic decays of charmed  $D$  mesons is of great significance in the study of the strong and weak interactions in  $D$  decays.
- ◆ The analysis on  $D \rightarrow PP$  modes will provide materials for the study of SU(3) breaking effect<sup>1</sup>. And the observation of CP violation in  $D$  decay is commonly believed to be indications of new physics.
- ◆  $D^0 \rightarrow K^- \pi^+$  is an important normalization mode.
- ◆ Most of the  $D$  decays have been studied by CLEO in 2010<sup>2</sup>, other measurements come from Belle<sup>3</sup>, BaBar<sup>4</sup> and CDF<sup>5</sup>, etc.
- ◆ Some of the branching fractions (BFs) are not well established. With the 2.93 fb<sup>-1</sup> data taken at 3.773 GeV within BESIII, the results will help to improve these measurements.

Mode	$N_{\text{signal}}^{\text{net}}$	$\epsilon$ (%)	$\mathcal{B} \pm (\text{stat}) \pm (\text{sys})$	$\mathcal{B}_{\text{PDG}}$
$\pi^+ \pi^-$	$21105 \pm 249$	$66.03 \pm 0.25$	$(1.505 \pm 0.018 \pm 0.031) \times 10^{-3}$	$(1.421 \pm 0.025) \times 10^{-3}$
$K^+ K^-$	$1543 \pm 273$	$62.82 \pm 0.32$	$(4.229 \pm 0.020 \pm 0.087) \times 10^{-3}$	$(4.01 \pm 0.07) \times 10^{-3}$
$K^- \pi^+$	$537745 \pm 767$	$64.98 \pm 0.09$	$(3.896 \pm 0.006 \pm 0.073) \%$	$(3.93 \pm 0.04) \%$
$K_S^0 \pi^0$	$66539 \pm 302$	$38.06 \pm 0.17$	$(1.236 \pm 0.006 \pm 0.032) \%$	$(1.20 \pm 0.04) \%$
$K_S^0 \eta$	$9532 \pm 126$	$31.96 \pm 0.14$	$(5.149 \pm 0.068 \pm 0.134) \times 10^{-3}$	$(4.85 \pm 0.30) \times 10^{-3}$
$K_S^0 \eta'$	$3007 \pm 61$	$12.66 \pm 0.08$	$(9.562 \pm 0.197 \pm 0.379) \times 10^{-3}$	$(9.5 \pm 0.5) \times 10^{-3}$
$\pi^0 \pi^+$	$10108 \pm 267$	$48.98 \pm 0.34$	$(1.259 \pm 0.033 \pm 0.025) \times 10^{-3}$	$(1.24 \pm 0.06) \times 10^{-3}$
$\pi^0 K^+$	$1834 \pm 168$	$51.52 \pm 0.42$	$(2.171 \pm 0.198 \pm 0.060) \times 10^{-4}$	$(1.89 \pm 0.25) \times 10^{-4}$
$\eta \pi^+$	$11636 \pm 215$	$46.96 \pm 0.25$	$(3.790 \pm 0.070 \pm 0.075) \times 10^{-3}$	$(3.66 \pm 0.22) \times 10^{-3}$
$\eta K^+$	$439 \pm 72$	$48.21 \pm 0.31$	$(1.393 \pm 0.228 \pm 0.124) \times 10^{-4}$	$(1.12 \pm 0.18) \times 10^{-4}$
$\eta' \pi^+$	$3088 \pm 83$	$21.49 \pm 0.18$	$(5.122 \pm 0.140 \pm 0.210) \times 10^{-3}$	$(4.84 \pm 0.31) \times 10^{-3}$
$\eta' K^+$	$87 \pm 25$	$22.39 \pm 0.22$	$(1.377 \pm 0.428 \pm 0.202) \times 10^{-4}$	$(1.83 \pm 0.23) \times 10^{-4}$
$K_S^0 \pi^+$	$93884 \pm 352$	$51.38 \pm 0.18$	$(1.591 \pm 0.006 \pm 0.033) \times 10^{-2}$	$(1.53 \pm 0.06) \times 10^{-2}$
$K_S^0 K^+$	$17704 \pm 151$	$48.45 \pm 0.14$	$(3.183 \pm 0.028 \pm 0.065) \times 10^{-3}$	$(2.95 \pm 0.15) \times 10^{-3}$

$$\mathcal{B} = \frac{N_{\text{signal}}^{\text{net}}}{2 \cdot N_{D^0 \bar{D}^0} (D^+ D^-) \cdot \epsilon}, N_{D^0 \bar{D}^0} = (10,621 \pm 29_{\text{stat}}) \times 10^3, N_{D^+ D^-} = (8,296 \pm 31_{\text{stat}}) \times 10^3$$

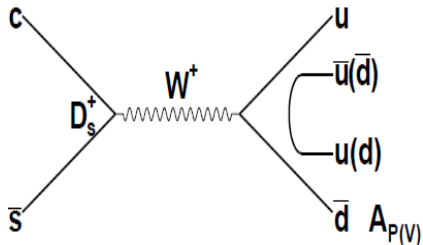
quoted from Derrick's talk given at APS2014

The  $\mathcal{B}(D^0 \rightarrow K^- \pi^+)$  has been corrected by the PDG value of  $\mathcal{B}(D^0 \rightarrow K^+ \pi^-)$ .

For  $D^0 \rightarrow K_S^0 \eta$ ,  $D^+ \rightarrow \pi^0 \pi^+$ ,  $D^+ \rightarrow \eta \pi^+$ ,  $D^+ \rightarrow \eta' \pi^+$ ,  $D^+ \rightarrow K_S^0 \pi^+$  and  $D^+ \rightarrow K_S^0 K^+$ , it shows better precision than the present values.

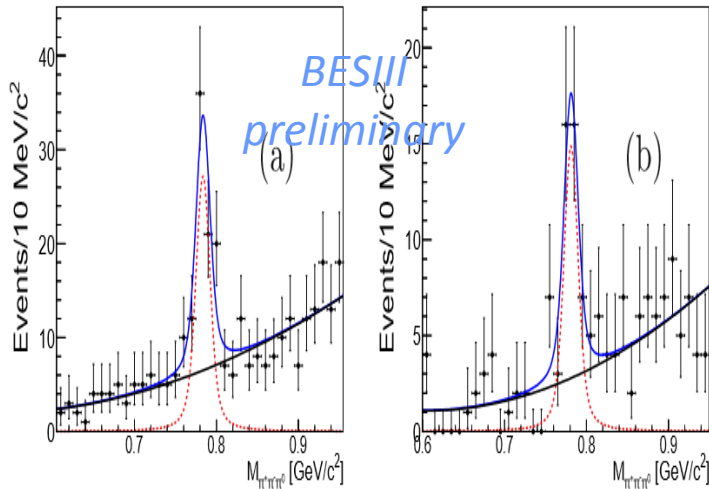
# $D_s^+$ 介子纯湮灭衰变和重子衰变的首次观测

首次确认纯湮灭衰变  $D_s^+ \rightarrow \omega \pi^+$   
并首次测定  $D_s^+ \rightarrow \omega K^+$



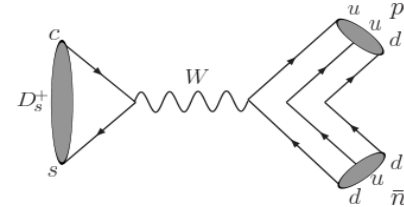
Under the model-independent approach:  

$$A(D_s^+ \rightarrow \omega \pi^+) = \frac{1}{\sqrt{2}} (A_P + A_V)$$
 ( $A_{P,V}$ :  $P, V$  contain  $\bar{q}q'$  of  $q\bar{q}'$  configuration)

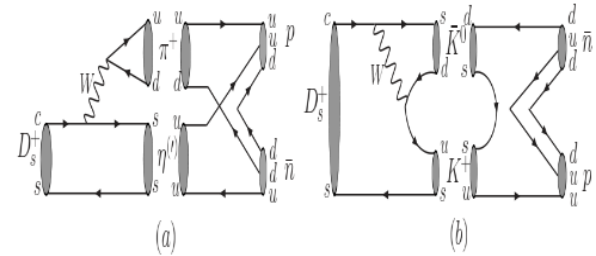


Signal mode	Branching fraction ( $10^{-3}$ )
$D_s^+ \rightarrow \omega \pi^+$	$1.85 \pm 0.30(\text{stat.}) \pm 0.19(\text{sys.})$
$D_s^+ \rightarrow \omega K^+$	$1.13 \pm 0.24(\text{stat.}) \pm 0.14(\text{sys.})$

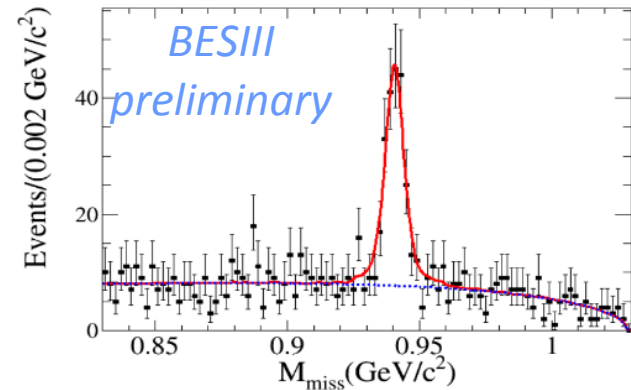
首次确认重子衰变  $D_s^+ \rightarrow p \bar{n}$



(a) Short-distance effects



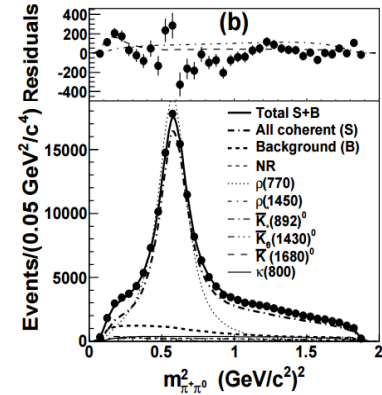
(b) Long-distance effects



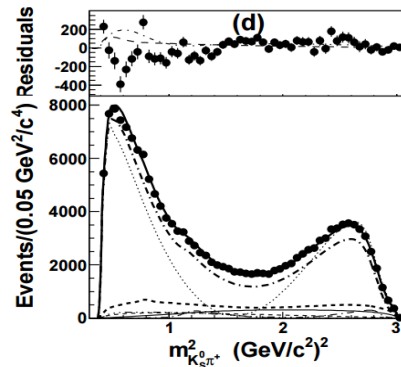
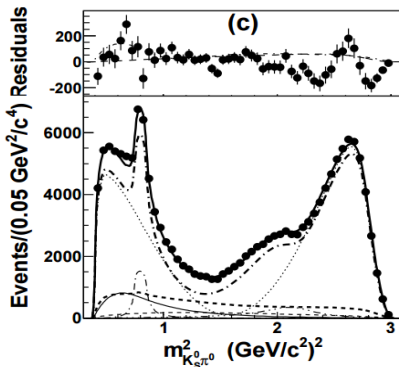
$$\mathcal{B}_{D_s^+ \rightarrow p \bar{n}} = (1.22 \pm 0.10) \times 10^{-3}$$

# 多体D衰变振幅分析:VP/VV/SP/...两体衰变

$$D^+ \rightarrow K_S \pi^+ \pi^0$$



PRD89(2014)052001



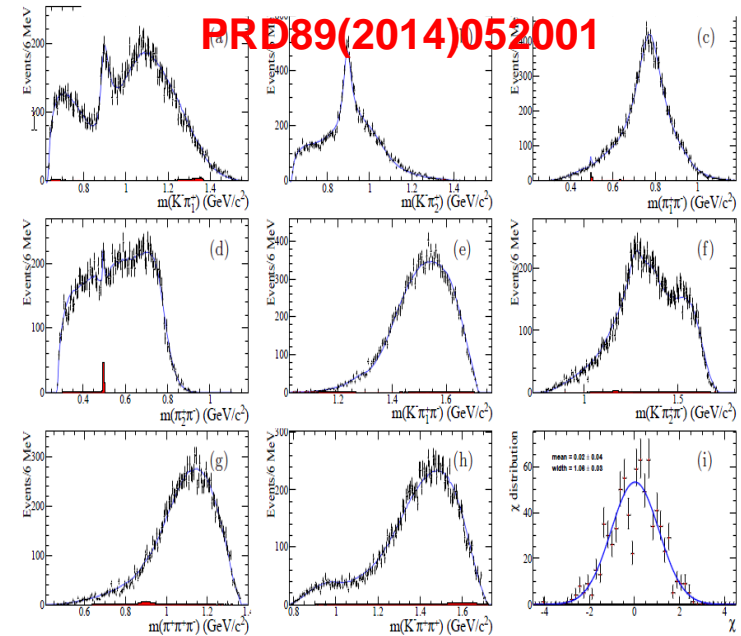
Mode	Partial Branching Fraction (%)
$D^+ \rightarrow K_S^0 \pi^+ \pi^0$ Non Resonant	$0.32 \pm 0.05 \pm 0.25^{+0.28}_{-0.25}$
$D^+ \rightarrow \rho^+ K_S^0, \rho^+ \rightarrow \pi^+ \pi^0$	$5.83 \pm 0.16 \pm 0.30^{+0.45}_{-0.15}$
$D^+ \rightarrow \rho(1450)^+ K_S^0, \rho(1450)^+ \rightarrow \pi^+ \pi^0$	$0.15 \pm 0.02 \pm 0.09^{+0.07}_{-0.11}$
$D^+ \rightarrow \bar{K}^*(892)^0 \pi^+, \bar{K}^*(892)^0 \rightarrow K_S^0 \pi^0$	$0.250 \pm 0.012 \pm 0.015^{+0.025}_{-0.024}$
$D^+ \rightarrow \bar{K}_0^*(1430)^0 \pi^+, \bar{K}_0^*(1430)^0 \rightarrow K_S^0 \pi^0$	$0.26 \pm 0.04 \pm 0.05 \pm 0.06$
$D^+ \rightarrow \bar{K}^*(1680)^0 \pi^+, \bar{K}^*(1680)^0 \rightarrow K_S^0 \pi^0$	$0.09 \pm 0.01 \pm 0.05^{+0.04}_{-0.08}$
$D^+ \rightarrow \bar{\kappa}^0 \pi^+, \bar{\kappa}^0 \rightarrow K_S^0 \pi^0$	$0.54 \pm 0.09 \pm 0.28^{+0.36}_{-0.19}$
$NR + \bar{\kappa}^0 \pi^+$	$1.30 \pm 0.12 \pm 0.12^{+0.12}_{-0.30}$
$K_S^0 \pi^0$ S-wave	$1.21 \pm 0.10 \pm 0.16^{+0.19}_{-0.27}$

$$D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$$

Help to determine the absolute BF, strong phase. benefit  $\gamma/\phi_2$

Previous analyses only from MarkIII and E691

PRD89(2014)052001

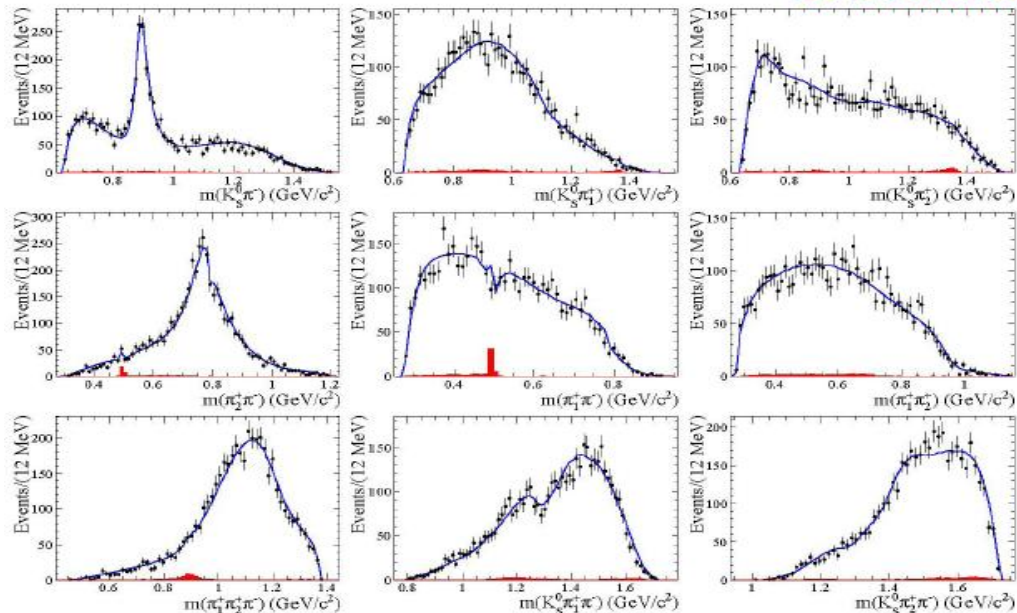


Component	Branching fraction (%)	PDG value (%)
$D^0 \rightarrow \bar{K}^0 \rho^0$	$0.99 \pm 0.04 \pm 0.04 \pm 0.03$	$1.05 \pm 0.23$
$D^0 \rightarrow K^- a_1^+(1260)(\rho^0 \pi^+)$	$4.41 \pm 0.22 \pm 0.30 \pm 0.13$	$3.6 \pm 0.6$
$D^0 \rightarrow K_1^-(1270)(\bar{K}^0 \pi^-) \pi^+$	$0.07 \pm 0.01 \pm 0.02 \pm 0.00$	$0.29 \pm 0.03$
$D^0 \rightarrow K_1^-(1270)(K^- \rho^0) \pi^+$	$0.27 \pm 0.02 \pm 0.04 \pm 0.01$	
$D^0 \rightarrow K^- \pi^+ \rho^0$	$0.68 \pm 0.09 \pm 0.20 \pm 0.02$	$0.51 \pm 0.23$
$D^0 \rightarrow \bar{K}^0 \pi^+ \pi^-$	$0.57 \pm 0.03 \pm 0.04 \pm 0.02$	$0.99 \pm 0.23$
$D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$	$1.77 \pm 0.05 \pm 0.04 \pm 0.05$	$1.88 \pm 0.26$



# $D^+ \rightarrow K_S \pi^+ \pi^+ \pi^-$ 振幅分析

BESIII Preliminary



BESIII Preliminary

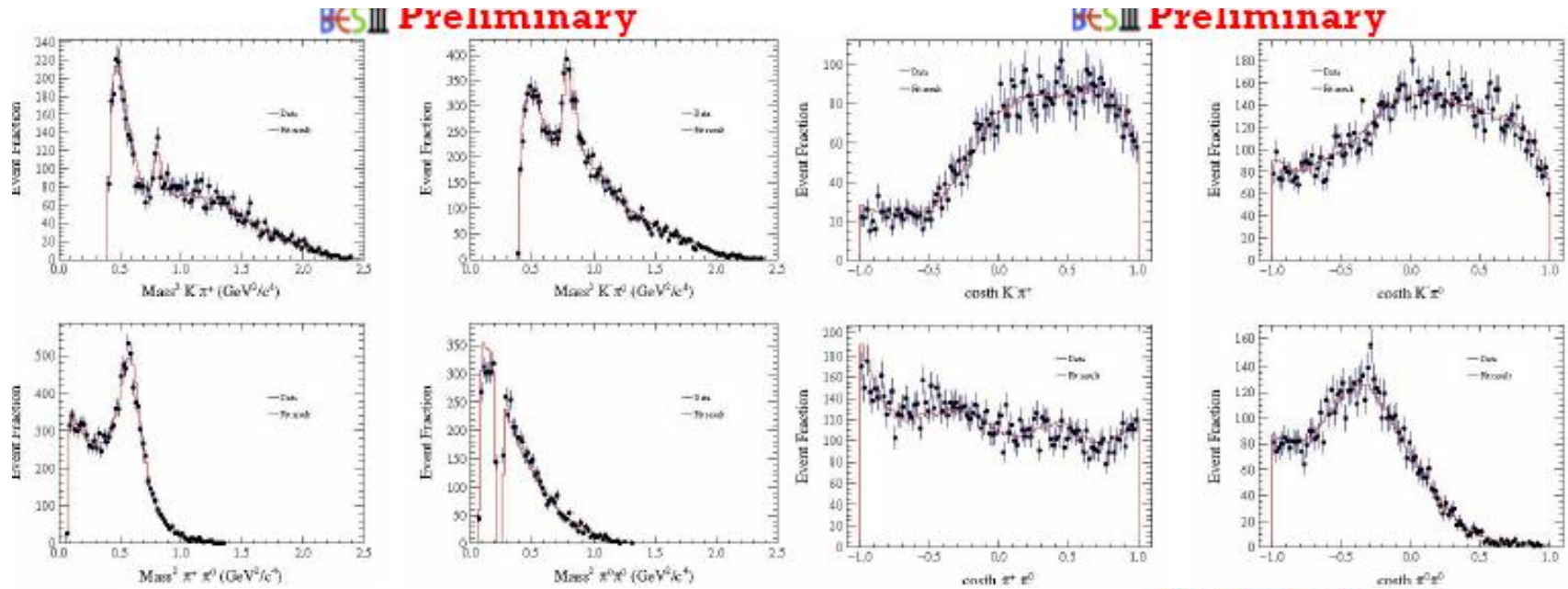
Component	Branching fraction (%)
$D^+ \rightarrow K_S^0 a_1(1260)^+ (\rho^0 \pi^+)$	$1.684 \pm 0.059 \pm 0.131 \pm 0.062$
$D^+ \rightarrow K_S^0 a_1(1260)^+ (f_0(500) \pi^+)$	$0.149 \pm 0.018 \pm 0.021 \pm 0.006$
$D^+ \rightarrow \bar{K}_1(1400)^0 (K^{*-} \pi^+) \pi^+$	$1.105 \pm 0.045 \pm 0.048 \pm 0.041$
$D^+ \rightarrow \bar{K}_1(1270)^0 (K_S^0 \rho^0) \pi^+$	$0.107 \pm 0.012 \pm 0.006 \pm 0.004$
$D^+ \rightarrow \bar{K}(1460)^0 (K_S^0 \rho^0) \pi^+$	$0.042 \pm 0.012 \pm 0.009 \pm 0.002$
$D^+ \rightarrow K_S^0 \pi^+ \rho^0$	$0.131 \pm 0.015 \pm 0.015 \pm 0.005$
$D^+ \rightarrow K^{*-} \pi^+ \pi^+$	$0.413 \pm 0.036 \pm 0.059 \pm 0.015$
$D^+ \rightarrow K_S^0 \pi^+ \pi^+ \pi^-$	$0.220 \pm 0.015 \pm 0.024 \pm 0.008$

Stat. uncertainty from FF

Sys. uncertainty from FF

uncertainties related to  $B(D^+ \rightarrow K_S^0 \pi^+ \pi^+ \pi^-)$  in PDG

# $D^+ \rightarrow K^- \pi^+ \pi^0 \pi^0$ 振幅分析



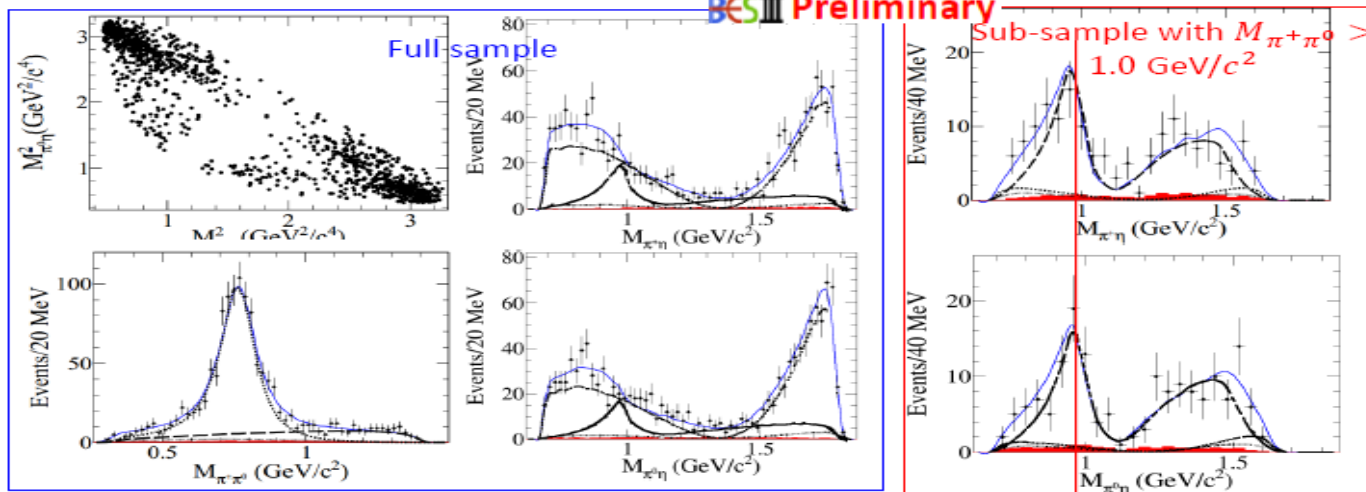
Amplitude	$\phi$	Fit fraction
$D^+ \rightarrow K_S^0 a_1(1260)^+, a_1(1260)^+ \rightarrow \rho^0 \pi^+[S]$	0.000(fixed)	$0.567 \pm 0.020 \pm 0.044$
$D^+ \rightarrow K_S^0 a_1(1260)^+, a_1(1260)^+ \rightarrow f_0(500)\pi^+$	$-2.023 \pm 0.068 \pm 0.113$	$0.050 \pm 0.006 \pm 0.007$
$D^+ \rightarrow \bar{K}_1(1400)^0 \pi^+, \bar{K}_1(1400)^0 \rightarrow K^{*-} \pi^+[S]$	$-2.714 \pm 0.038 \pm 0.051$	$0.380 \pm 0.013 \pm 0.014$
$D^+ \rightarrow \bar{K}_1(1400)^0 \pi^+, \bar{K}_1(1400)^0 \rightarrow K^{*-} \pi^+[D]$	$3.431 \pm 0.137 \pm 0.117$	$0.015 \pm 0.004 \pm 0.005$
$D^+ \rightarrow \bar{K}_1(1270)^0 \pi^+, \bar{K}_1(1270)^0 \rightarrow K_S^0 \rho^0[S]$	$-0.418 \pm 0.070 \pm 0.087$	$0.036 \pm 0.004 \pm 0.002$
$D^+ \rightarrow \bar{K}(1460)^0 \pi^+, \bar{K}(1460)^0 \rightarrow K_S^0 \rho^0$	$-1.850 \pm 0.120 \pm 0.223$	$0.014 \pm 0.004 \pm 0.003$
$D^+ \rightarrow (K_S^0 \rho^0)_A[D] \pi^+$	$2.328 \pm 0.097 \pm 0.068$	$0.011 \pm 0.003 \pm 0.002$
$D^+ \rightarrow K_S^0(\rho^0 \pi^+)_P$	$1.656 \pm 0.083 \pm 0.056$	$0.031 \pm 0.004 \pm 0.010$
$D^+ \rightarrow (K^{*-} \pi^+)_A[S] \pi^+$	$1.962 \pm 0.047 \pm 0.073$	$0.132 \pm 0.011 \pm 0.011$
$D^+ \rightarrow (K^{*-} \pi^+)_A[D] \pi^+$	$0.989 \pm 0.158 \pm 0.229$	$0.013 \pm 0.004 \pm 0.004$
$D^+ \rightarrow (K_S^0(\pi^+ \pi^-)_S)_A \pi^+$	$-2.935 \pm 0.060 \pm 0.125$	$0.051 \pm 0.004 \pm 0.003$
$D^+ \rightarrow ((K_S^0 \pi^-)_S \pi^+)_P \pi^+$	$1.864 \pm 0.069 \pm 0.288$	$0.022 \pm 0.003 \pm 0.003$

First measurement!

$$\mathcal{B}(D^0 \rightarrow K^- \pi^+ \pi^0 \pi^0) = (8.98 \pm 0.13(\text{stat}) \pm 0.40(\text{syst}))\%$$

# $D_s^+ \rightarrow \eta \pi^+ \pi^0$ 振幅分析

Dalitz plot and projections



Dots with error bar: data; **solid**: total fit; dashed:  $D_s^+ \rightarrow \rho^+ \eta$ ; dotted:  $D_s^+ \rightarrow (\pi^+ \pi^0)_V \eta$ ; long dashed:  $D_s^+ \rightarrow a_0(980) \pi$ .

Obvious peaks for two  $a_0(980)$  mesons!

The significances, phases, and FFs for intermediate processes.

Amplitude	Significance ( $\sigma$ )	Phase	FF
$D_s^+ \rightarrow \rho^+ \eta$	$> 20$	0.0 (fixed)	$0.783 \pm 0.050 \pm 0.021$
$D_s^+ \rightarrow (\pi^+ \pi^0)_V \eta$	5.7	$0.612 \pm 0.172 \pm 0.342$	$0.054 \pm 0.021 \pm 0.026$
<b><math>D_s^+ \rightarrow a_0(980) \pi</math></b>	<b>16.2</b>	<b><math>2.794 \pm 0.087 \pm 0.041</math></b>	<b><math>0.232 \pm 0.023 \pm 0.034</math></b>

The amplitude analysis agrees with the isospin conserved expectation ( $A(D_s^+ \rightarrow$

$$BF(D_s^+ \rightarrow \pi^+ \pi^0 \eta) = (9.50 \pm 0.28_{stat.} \pm 0.41_{sys.})\%$$

$$BF(n) = BF(D_s^+ \rightarrow \pi^+ \pi^0 \eta) FF(n)$$

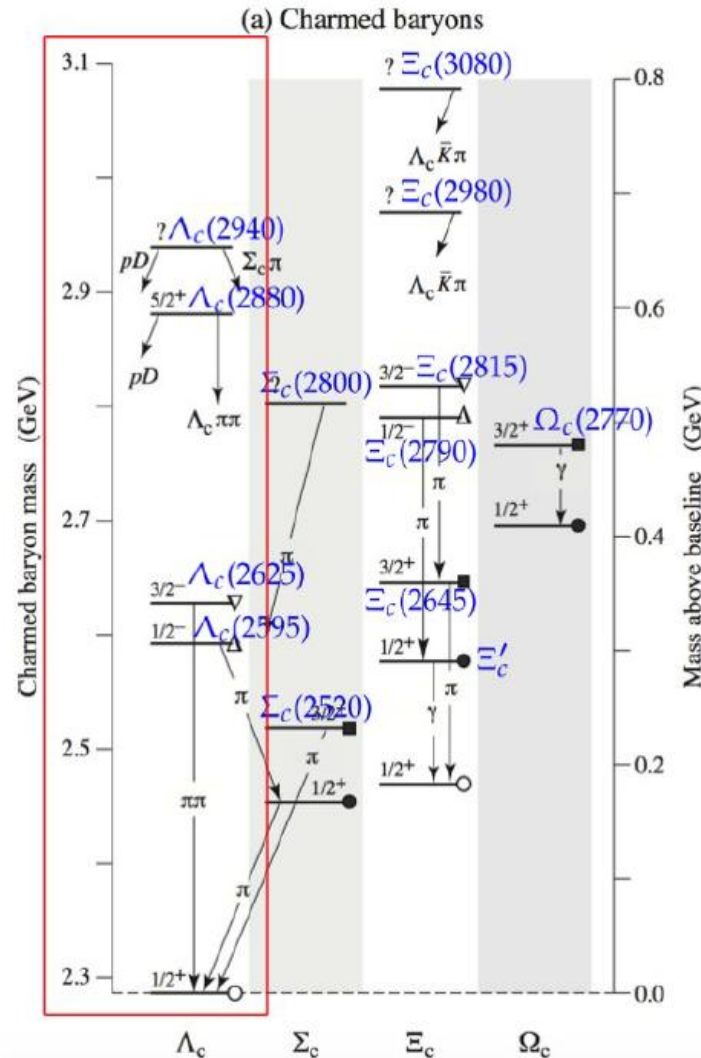
Branching fraction	This measurement (%)	PDG value (%)
$BF(D_s^+ \rightarrow \rho^+ \eta)$	$7.44 \pm 0.48_{stat.} \pm 0.44_{sys.}$	$8.9 \pm 0.9$
$BF(D_s^+ \rightarrow a_0(980) \pi) *$	$2.20 \pm 0.22_{stat.} \pm 0.34_{sys.}$	-
$BF(D_s^+ \rightarrow a_0(980)^+ \pi^0) *$	$1.46 \pm 0.15_{stat.} \pm 0.22_{sys.}$	-
$BF(D_s^+ \rightarrow a_0(980)^0 \pi^+) *$		

\*Here,  $a_0(980) \rightarrow \pi \eta$ .



# 粲重子 $\Lambda_c^+$ 衰变

# 2014年前粲重子研究



➤  $\Lambda_c^+$  was observed in 1979

➤ All decays of  $\Lambda_c^+$  were measured with high energy data and relative to  $pK^-\pi^+$ , which suffers an error of 25%. No absolute measurement using threshold  $\Lambda_c^+$  data

➤ Only about 60% decays are known

$\Lambda_c^+$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level	$p$ (MeV/c)
<b>Hadronic modes with a <math>p</math>: <math>S = -1</math> final states</b>			
$p\bar{K}^0$	( 2.3 ± 0.6 ) %		873
$pK^-\pi^+$	[a] ( 5.0 ± 1.3 ) %		823
$p\bar{K}^*(892)^0$	[b] ( 1.6 ± 0.5 ) %		685
$\Delta(1232)^{++}K^-$	( 8.6 ± 3.0 ) × 10 <sup>-3</sup>		710
$\Lambda(1520)\pi^+$	[b] ( 1.8 ± 0.6 ) %		627
$pK^-\pi^+$ nonresonant	( 2.8 ± 0.8 ) %		823
$p\bar{K}^0\pi^0$	( 3.3 ± 1.0 ) %		823
$p\bar{K}^0\eta$	( 1.2 ± 0.4 ) %		568

Systematic studies of  $\Lambda_c^+$ , search for new decays, absolute BF measurements are important to explore  $\Lambda_c^+$  decay mechanisms

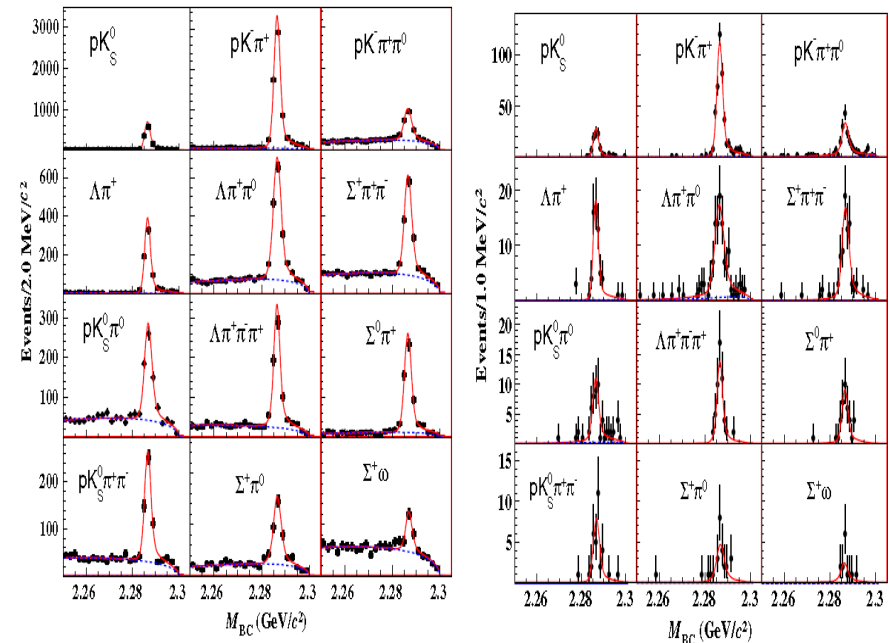
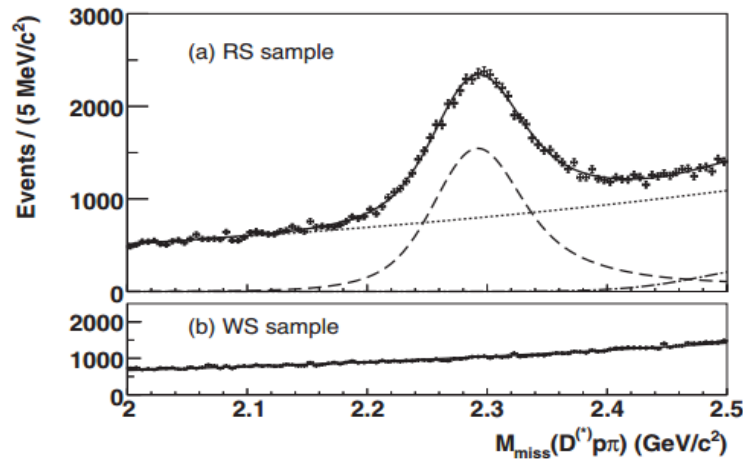
# $\Lambda_c^+ \rightarrow$ 强子衰变绝对分支比的改进测量

BELLE, PRL113(2014)042002

BESIII, PRL116(2016)052001

ST:  $\sim 15000$

DT:  $\sim 1000$

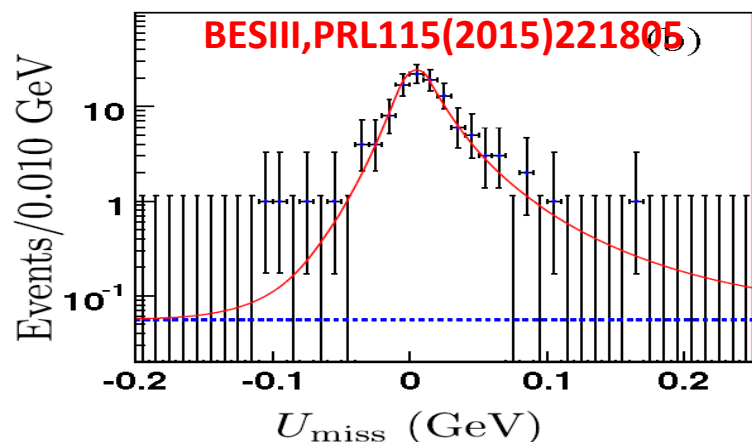


Mode	This work (%)	PDG (%)
$pK_S^0$	$1.52 \pm 0.08 \pm 0.03$	$1.15 \pm 0.30$
$pK^-\pi^+$	$5.84 \pm 0.27 \pm 0.23$	$5.0 \pm 1.3$
$pK_S^0\pi^0$	$1.87 \pm 0.13 \pm 0.05$	$1.65 \pm 0.50$
$pK_S^0\pi^+\pi^-$	$1.53 \pm 0.11 \pm 0.09$	$1.31 \pm 0.25$
$pK^-\pi^+\pi^0$	$4.53 \pm 0.23 \pm 0.30$	$3.4 \pm 1.0$
$\Lambda\pi^+$	$1.24 \pm 0.07 \pm 0.03$	$1.57 \pm 0.28$
$\Lambda\pi^+\pi^0$	$7.01 \pm 0.37 \pm 0.19$	$3.6 \pm 1.3$
$\Lambda\pi^+\pi^-\pi^+$	$3.81 \pm 0.24 \pm 0.18$	$2.6 \pm 0.7$
$\Sigma^0\pi^+$	$1.27 \pm 0.08 \pm 0.03$	$1.05 \pm 0.28$
$\Sigma^+\pi^0$	$1.18 \pm 0.10 \pm 0.03$	$1.00 \pm 0.34$
$\Sigma^+\pi^+\pi^-$	$4.25 \pm 0.24 \pm 0.20$	$3.6 \pm 1.0$
$\Sigma^+\omega$	$1.56 \pm 0.20 \pm 0.07$	$2.7 \pm 1.0$

Much better  
precision

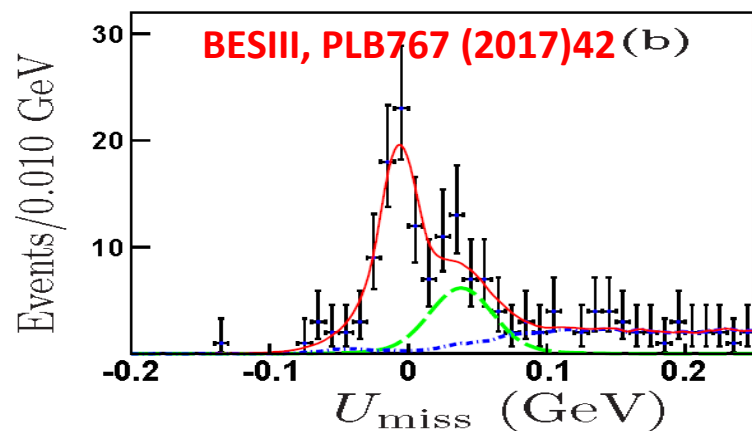
$$B[\Lambda_c^+ \rightarrow pK^-\pi^+] = (6.84 \pm 0.24^{+0.21}_{-0.27})\%$$

# 首次测定半轻衰变 $\Lambda_c^+ \rightarrow \Lambda l^+ \nu$ 的绝对分支比



$$B[\Lambda_c^+ \rightarrow \Lambda e^+ \nu] = (3.63 \pm 0.38 \pm 0.20)\%$$

3 fb<sup>-1</sup> data help to explore FF studies



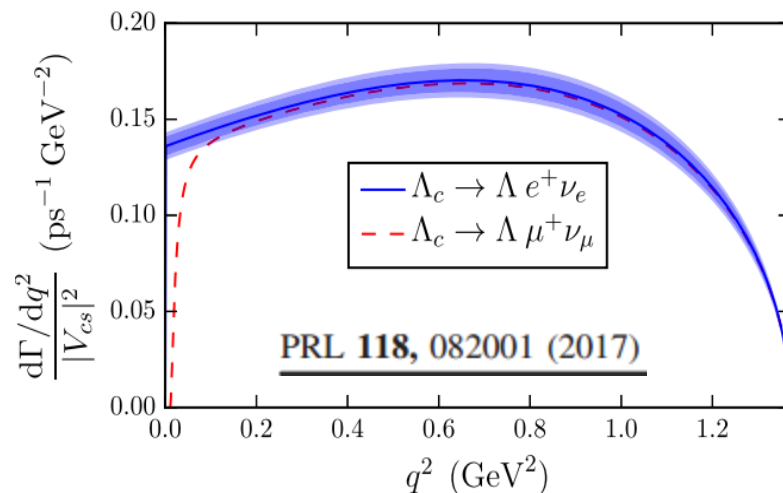
$$B[\Lambda_c^+ \rightarrow \Lambda \mu^+ \nu] = (3.49 \pm 0.46 \pm 0.26)\%$$

$$\Gamma[\Lambda_c^+ \rightarrow \Lambda \mu^+ \nu] / \Gamma[\Lambda_c^+ \rightarrow \Lambda e^+ \nu] = 0.96 \pm 0.16 \pm 0.04$$

Calibrate theoretical calculations:  
(1.4-9.2)%

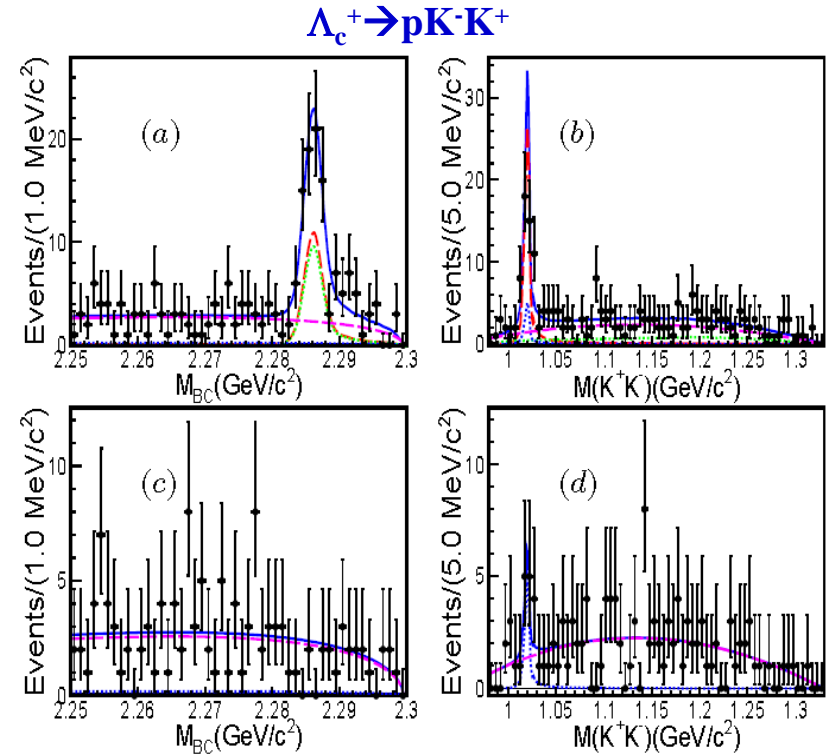
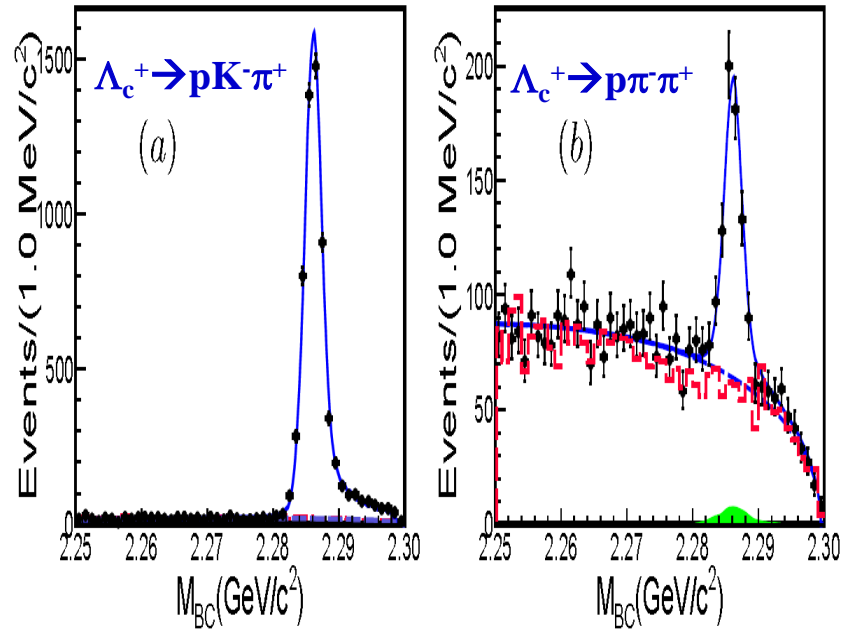
Theoretical Models	predicated branching fraction for $\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e$
MBM [1]	1.9%
NRQM [1]	2.6%
SU(4)-symmetry limit [2]	9.2%
RSQM [3]	4.4%
QCM [4]	5.62%
SQM [5]	1.96%
NRQM2 [6]	2.15%
NRQM3 [7]	1.42%
QCD SR1 [8]	$(3.0 \pm 0.9)\%$
QCD SR2 [9]	$(2.6 \pm 0.4)\%$
QCD SR3 [9]	$(5.8 \pm 1.5)\%$
STSR [10]	2.22% for $\Lambda_c^+ \rightarrow \Lambda l^+ \nu_l$
STNR [10]	1.58% for $\Lambda_c^+ \rightarrow \Lambda l^+ \nu_l$
HOSR [10]	4.72% for $\Lambda_c^+ \rightarrow \Lambda l^+ \nu_l$
HONR [10]	4.2% for $\Lambda_c^+ \rightarrow \Lambda l^+ \nu_l$
LCSR [11]	$(3.0 \pm 0.3)\%$ for $\Lambda_c^+ \rightarrow \Lambda l^+ \nu_l$ (CZ-type)
PDG 2014 [14]	$(2.1 \pm 0.6)\%$
BESIII	$(3.63 \pm 0.38 \pm 0.20)\%$

促进LQCD对形状因子的计算



# 改进测定 $\Lambda_c^+ \rightarrow pK^+K^-/p\pi^+\pi^-$ 绝对分支比

BESIII, PRL117(2016)232002

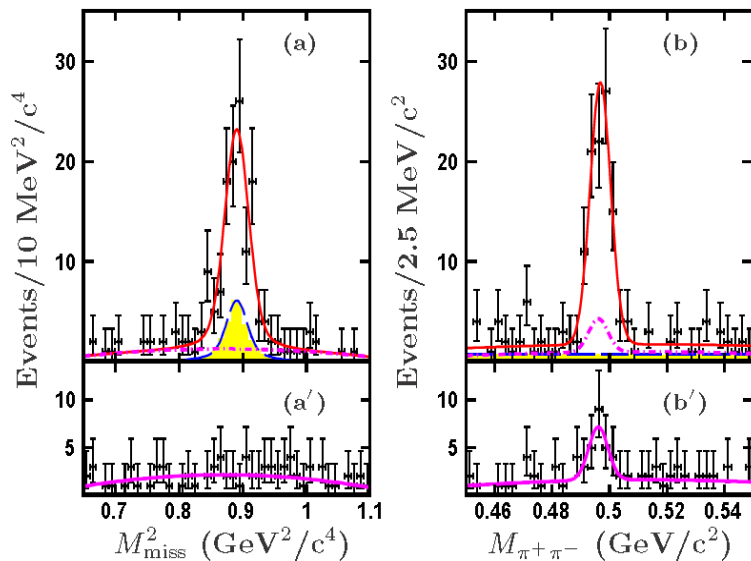


These help to distinguish predictions from different theoretical models and understand contributions from factorizable effects

Decay modes	$\mathcal{B}_{\text{mode}}/\mathcal{B}_{\text{ref.}}$	$\mathcal{B}_{\text{mode}}$	$\mathcal{B}(\text{PDG})$
$\Lambda_c^+ \rightarrow p\pi^+\pi^-$	$(6.70 \pm 0.48 \pm 0.25) \times 10^{-2}$	$(3.91 \pm 0.28 \pm 0.15 \pm 0.24) \times 10^{-3}$	$(3.5 \pm 2.0) \times 10^{-3}$
$\Lambda_c^+ \rightarrow p\phi$	$(1.81 \pm 0.33 \pm 0.13) \times 10^{-2}$	$(1.06 \pm 0.19 \pm 0.08 \pm 0.06) \times 10^{-3}$	$(8.2 \pm 2.7) \times 10^{-4}$
$\Lambda_c^+ \rightarrow pK^+K^-$ (non- $\phi$ )	$(9.36 \pm 2.22 \pm 0.71) \times 10^{-3}$	$(5.47 \pm 1.30 \pm 0.41 \pm 0.33) \times 10^{-4}$	$(3.5 \pm 1.7) \times 10^{-4}$

# 首次观测到含中子衰变 $\Lambda_c^+ \rightarrow n K_S \pi^+$

BESIII, PRL118(2017)112001



**Help to understand SU(3) and isospin symmetry and determine strong phase**

Cai-Dian Lv et al, PRD93(2016)056008

$$\cos \delta$$

$$= \frac{\mathcal{B}(n \bar{K}^0 \pi^+) - \mathcal{B}(p K^- \pi^+)}{2\sqrt{\mathcal{B}(p \bar{K}^0 \pi^0)(\mathcal{B}(p K^- \pi^+) + \mathcal{B}(n \bar{K}^0 \pi^+) - \mathcal{B}(p \bar{K}^0 \pi^0))}}$$

$$R_p = \frac{\mathcal{B}(\Lambda_c \rightarrow p \bar{K}^0 \pi^0)}{\mathcal{B}(\Lambda_c \rightarrow p K^- \pi^+)}, \quad R_n = \frac{\mathcal{B}(\Lambda_c \rightarrow n \bar{K}^0 \pi^+)}{\mathcal{B}(\Lambda_c \rightarrow p K^- \pi^+)}$$

$$\mathcal{B}[\Lambda_c^+ \rightarrow n K_S \pi^+] = (1.82 \pm 0.23 \pm 0.11)\%$$

$$\Gamma[\Lambda_c^+ \rightarrow n \bar{K}^0 \pi^+] / \Gamma[\Lambda_c^+ \rightarrow p K^- \pi^+] = 0.62 \pm 0.09$$

$$\Gamma[\Lambda_c^+ \rightarrow n \bar{K}^0 \pi^+] / \Gamma[\Lambda_c^+ \rightarrow p \bar{K}^0 \pi^+] = 0.97 \pm 0.16$$

**First measurement of BF of  $\Lambda_c^+$  decay containing neutron**

$$\cos \delta = -0.24 \pm 0.08$$

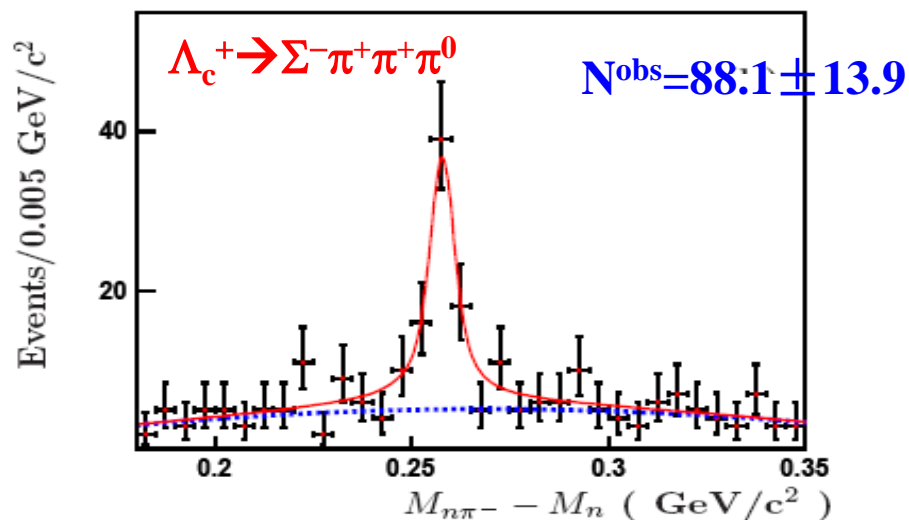
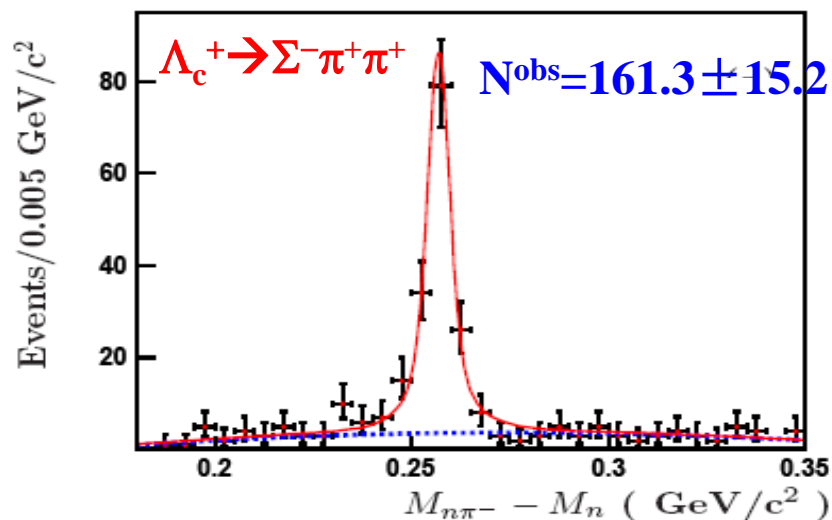
$$|I^{(1)}|/|I^{(0)}| = 1.14 \pm 0.11$$

involving a neutron. Under the isospin symmetry, its amplitude is related to those of the most favored proton modes  $\Lambda_c^+ \rightarrow p K^- \pi^+$  and  $\Lambda_c^+ \rightarrow p \bar{K}^0 \pi^0$  as  $\mathcal{A}(n \bar{K}^0 \pi^+) + \mathcal{A}(p K^- \pi^+) + \sqrt{2}\mathcal{A}(p \bar{K}^0 \pi^0) = 0$ . Hence, precise measure-

[2,3]. In the three-body  $\Lambda_c^+$  decay to  $N \bar{K} \pi$ , the total decay amplitudes can be decomposed into two isospin amplitudes of the  $N \bar{K}$  system as isosinglet ( $I^{(0)}$ ) and isospin-one ( $I^{(1)}$ ). In the factorization limit, the color-allowed tree diagram, in which the  $\pi^+$  is emitted and the  $N \bar{K}$  is an isosinglet, dominates  $I^{(0)}$ , and  $I^{(1)}$  is expected to be small compared to  $I^{(0)}$  as it can only proceed through the color-suppressed tree diagrams. Though the factorization scheme is spoiled in

# 首次测定 $\Lambda_c^+ \rightarrow \Sigma^- \pi^+ \pi^+ \pi^0$

BESIII, PLB772(2017)388



Preliminary results :

$$B[\Lambda_c^+ \rightarrow \Sigma^- \pi^+ \pi^+] = (1.81 \pm 0.17 \pm 0.09)\%$$

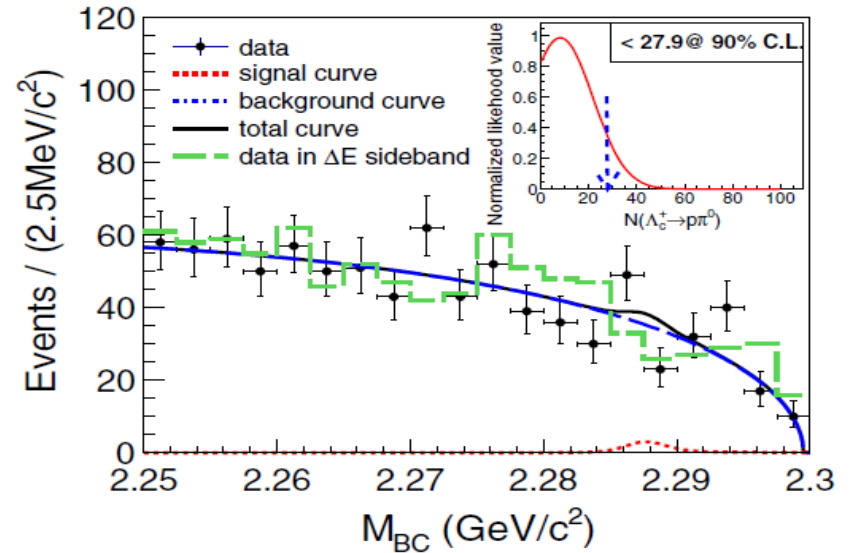
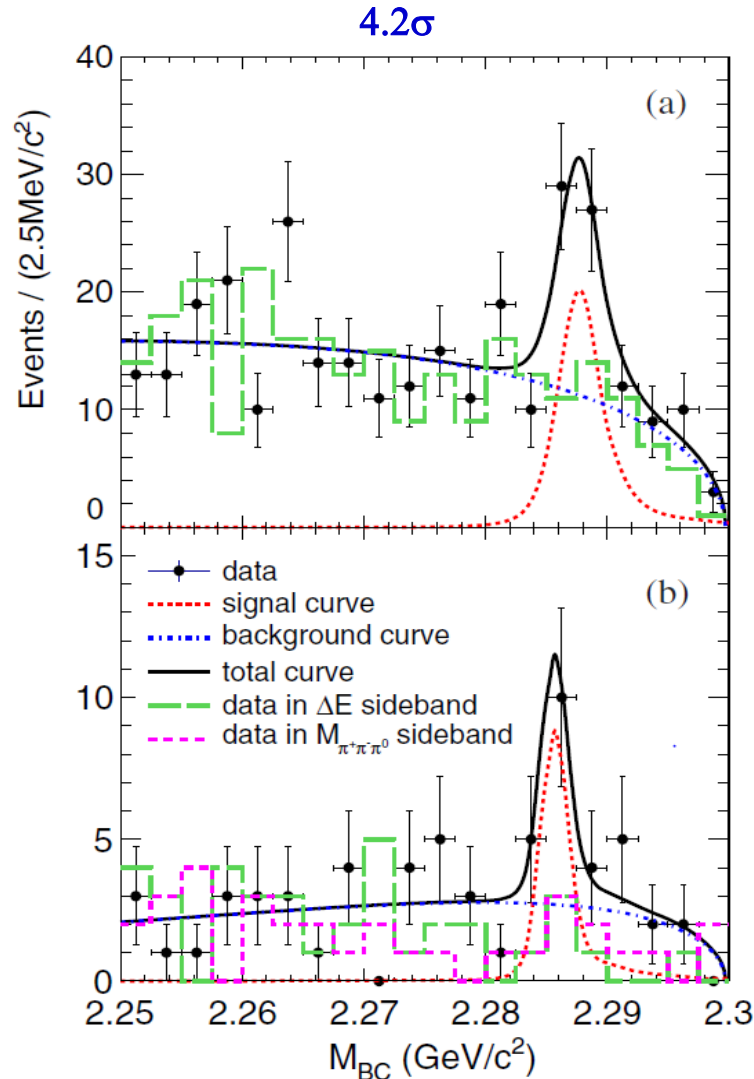
$$B[\Lambda_c^+ \rightarrow \Sigma^- \pi^+ \pi^+ \pi^0] = (2.11 \pm 0.33 \pm 0.14)\% \quad \text{[First observation]}$$

The previous one is consistent with and more precise than the PDG value of  $[\Lambda_c^+ \rightarrow \Sigma^- \pi^+ \pi^+] = (2.3 \pm 0.4)\%$ .



# 首次测定 $\Lambda_c^+ \rightarrow p\eta$ 并寻找 $\Lambda_c^+ \rightarrow p\pi^0$

BESIII, PRD95(2017)111102(RC)



$B[\Lambda_c^+ \rightarrow p\pi^0] < 2.7 \times 10^{-4} \text{ 90\%CL}$

	$\Lambda_c^+ \rightarrow p\eta$	$\Lambda_c^+ \rightarrow p\pi^0$	$\frac{B_{\Lambda_c^+ \rightarrow p\pi^0}}{B_{\Lambda_c^+ \rightarrow p\eta}}$
BESIII	$1.24 \pm 0.29$	$< 0.27$	$< 0.24$
Sharma <i>et al.</i> [3]	$0.2^a(1.7^b)$	0.2	$1.0^a(0.1^b)$
Uppal <i>et al.</i> [4]	0.3	0.1–0.2	0.3–0.7
S. L. Chen <i>et al.</i> [12]	...	0.11–0.36 <sup>c</sup>	...
Cai-Dian Lü <i>et al.</i> [13]	...	0.45	...

<sup>a</sup>Assumed to have a positive sign for the p-wave amplitude of  $\Lambda_c^+ \rightarrow \Xi^0 K^+$ .

<sup>b</sup>Assumed to have a negative sign for the p-wave amplitude of  $\Lambda_c^+ \rightarrow \Xi^0 K^+$ .

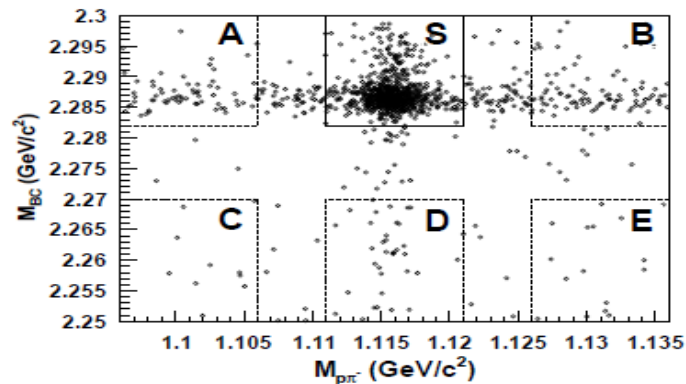
<sup>c</sup>Calculated relying on different values of parameters b and  $\alpha$ .

$B[\Lambda_c^+ \rightarrow p\eta] = (1.24 \pm 0.28 \pm 0.10) \times 10^{-3}$

# $\Lambda_c^+$ 研究最新进展

## ■ $\Lambda_c^+ \rightarrow \Lambda X$ 分支比

arXiv:1803.05706, accepted by PRL



$p$ (GeV/c)	$N_{sig}$			
	$\cos\theta$			
	[0.00, 0.20]	[0.20, 0.40]	[0.40, 0.65]	[0.65, 1.00]
[0.0, 0.3]	$5.3^{+5.1}_{-3.8}$	$11.4^{+5.5}_{-4.2}$	$9.1^{+5.5}_{-4.0}$	$6.3^{+5.4}_{-4.0}$
[0.3, 0.5]	$59.8^{+9.9}_{-8.6}$	$41.6^{+8.9}_{-7.7}$	$71.9^{+10.7}_{-9.5}$	$33.1^{+8.7}_{-7.4}$
[0.5, 0.7]	$86.7^{+10.9}_{-9.7}$	$72.5^{+10.0}_{-8.8}$	$74.8^{+10.1}_{-9.0}$	$53.9^{+9.1}_{-7.9}$
[0.7, 0.9]	$40.4^{+7.8}_{-6.6}$	$28.3^{+6.8}_{-5.6}$	$44.0^{+8.0}_{-6.9}$	$38.4^{+7.9}_{-6.7}$
[0.9, 1.1]	$6.9^{+4.9}_{-3.0}$	$12.4^{+5.0}_{-3.7}$	$8.3^{+4.2}_{-2.9}$	$5.5^{+3.9}_{-2.6}$

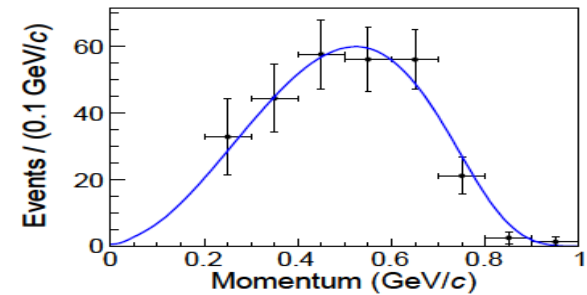
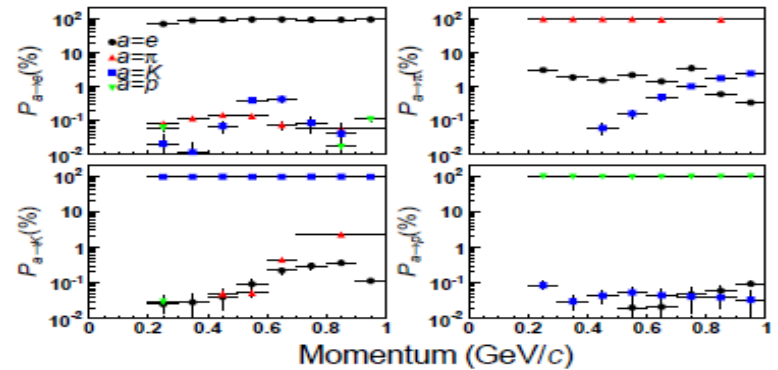
$p$ (GeV/c)	$\epsilon^{sig}$ (%)			
	$\cos\theta$			
	[0.00, 0.20]	[0.20, 0.40]	[0.40, 0.65]	[0.65, 1.00]
[0.0, 0.3]	$8.28 \pm 0.38$	$8.22 \pm 0.37$	$8.01 \pm 0.31$	$4.45 \pm 0.21$
[0.3, 0.5]	$29.03 \pm 0.37$	$28.28 \pm 0.37$	$26.56 \pm 0.33$	$14.98 \pm 0.21$
[0.5, 0.7]	$35.43 \pm 0.32$	$35.00 \pm 0.33$	$33.25 \pm 0.32$	$20.15 \pm 0.25$
[0.7, 0.9]	$39.68 \pm 0.47$	$39.27 \pm 0.50$	$36.56 \pm 0.50$	$23.80 \pm 0.51$
[0.9, 1.1]	$40.82 \pm 0.14$	$40.21 \pm 0.14$	$37.76 \pm 0.12$	$29.97 \pm 0.11$

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda + X) = (38.2^{+2.8}_{-2.2} \pm 0.8)\%.$$

$$(24.5 \pm 2.1)\% \text{ in PDG} \quad \mathcal{A}_{CP} = (2.1^{+7.0}_{-6.6} \pm 1.4)\%.$$

## ■ $\Lambda_c^+ \rightarrow X e \nu_e$ 分支比

arXiv:1805.09060, submitted to PRL



$$\mathcal{B}(\Lambda_c^+ \rightarrow X e^+ \nu_e) = (3.95 \pm 0.34 \pm 0.09)\%$$

$$\frac{\Gamma(\Lambda_c^+ \rightarrow X e^+ \nu_e)}{\Gamma(D \rightarrow X e^+ \nu_e)} = 1.26 \pm 0.12.$$

# Larger threshold $\Lambda_c^+$ data at BESIII

国际粲重子 $\Lambda_c^+$ 衰变实验研究的里程碑：**BESIII**开辟使用近阈数据绝对测量 $\Lambda_c^+$ 衰变的新领域

与**PDG14**比， $\Lambda_c^+$ 衰变测量精度普遍改进**3-5倍**。但与粲介子的测量精度(**1-2%**)水平比，统计误差仍是制约因素

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**CERN COURIER**

Mar 18, 2016

**BESIII makes first direct measurement of the  $\Lambda_c$  at threshold**

The charmed baryon,  $\Lambda_c$ , was first observed at Fermilab in 1976. Now, 40 years later, the Beijing Spectrometer (BESIII) experiment at the Beijing Electron-Positron Collider II (BEPCII) has measured the absolute branching fraction of  $\Lambda_c^+ \rightarrow p K^+ \pi^+$  at threshold for the first time.

Beam-constrained mass distribution

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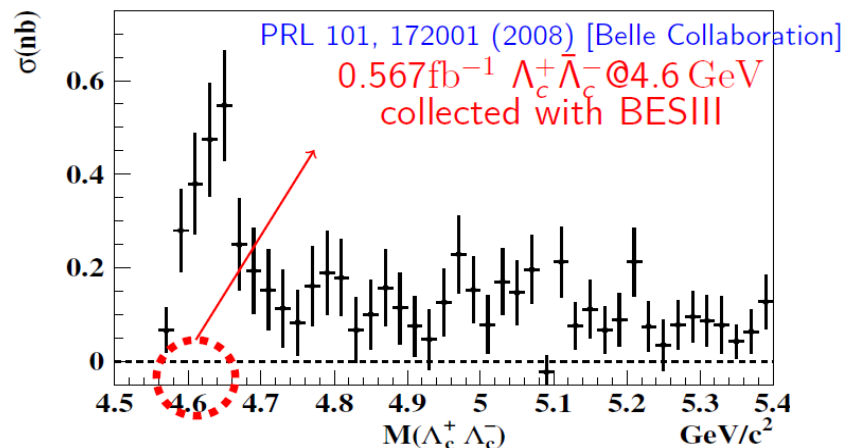
**Linde**

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- ▶ Imaging with muons
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	Golden hadronic mode	$\delta B/B$	Golden SL mode	$\delta B/B$
$D^0$	$B(K\pi)=(3.88\pm0.05)\%$	1.3%	$B(K\pi)=(3.55\pm0.05)\%$	1.4%
$D^+$	$B(K\pi\pi)=(9.13\pm0.19)\%$	2.1%	$B(K^0\pi)=(8.83\pm0.22)\%$	2.5%
$D_s$	$B(KK\pi)=(5.39\pm0.21)\%$	3.9%	$B(\phi\pi)=(2.49\pm0.14)\%$	5.6%
$\Lambda_c$	$B(pK\pi)=(5.0\pm1.3)\%$ (PDG2014) $= (6.8\pm0.36)\%$ (BELLE) $= (5.84\pm0.35)\%$ (BESIII) $= (6.46\pm0.24)\%$ (HFAG)	26% 5.3% 6.0% 3.7%	$B(\Lambda_c\pi)=(2.1\pm0.6)\%$ (PDG2014) $= (3.63\pm0.43)\%$ (BESIII) $= (3.18\pm0.32)\%$ (HFAG)	29% 12% 10%

更高能量**4.65 GeV**，更大近阈 $\Lambda_c^+$ 样本，进一步系统研究 $\Lambda_c^+$ ，寻找**40%**未知衰变(半轻、含中子和光子衰变)...



一个月左右数据已发表**10篇**物理文章，其中**6篇PRL**

# BelleII国际竞争 [举例]

See H. Atamcan at ICHEP  
and Belle II Physics Book appearing soon

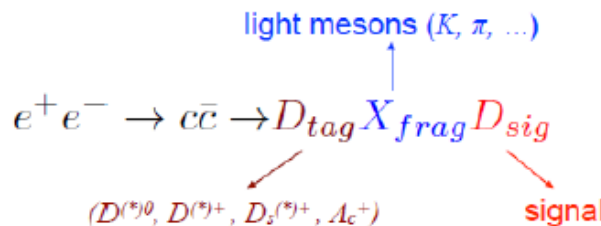


## Epilogue: Belle II

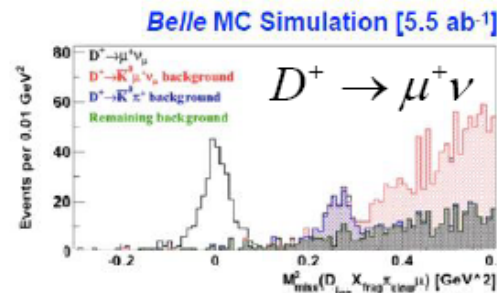
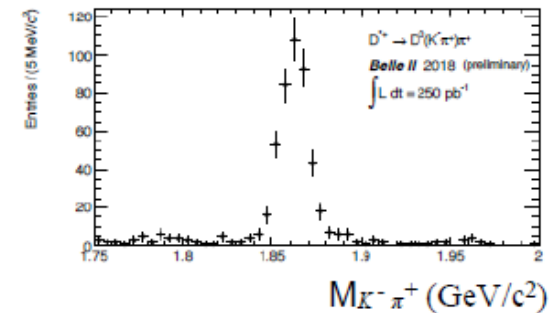
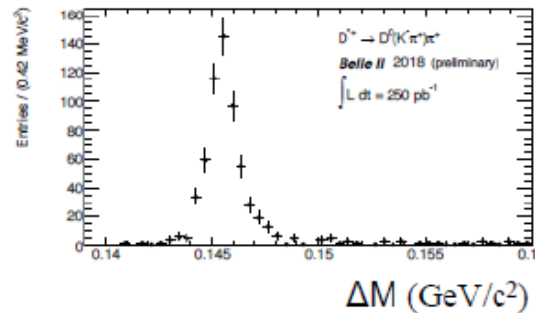
Flavour not just a  $B$  factory

@ $\sqrt{s} = 10.58$  GeV:  $\sigma(c\bar{c}) = 1.18\sigma(B\bar{B})$

All the attributes of  $B$  physics  
experiment – hermeticity, PID,  
vertexing, low momentum track and  
photon reconstruction – good for  
charm!



$$D^{*+} \rightarrow D^0 \pi^+, D^0 \rightarrow K^- \pi^+$$

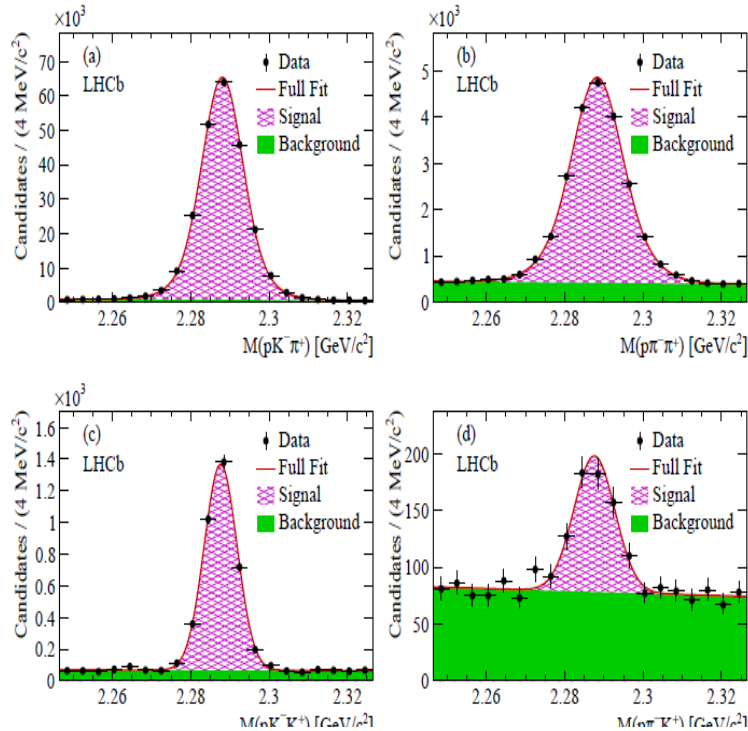


Tag	Millions of events in 50 ab <sup>-1</sup>	Current BESIII
$D^0$	38	2.8
$D^+$	3.5	1.7
$D_s^+$	5.2	0.4

# LHCb国际竞争 [举例]

LHCb, JHEP 1803 (2018) 043

$\Lambda_b^0 \rightarrow \Lambda_c^+(phh')\mu^-\bar{\nu}_\mu$  selection



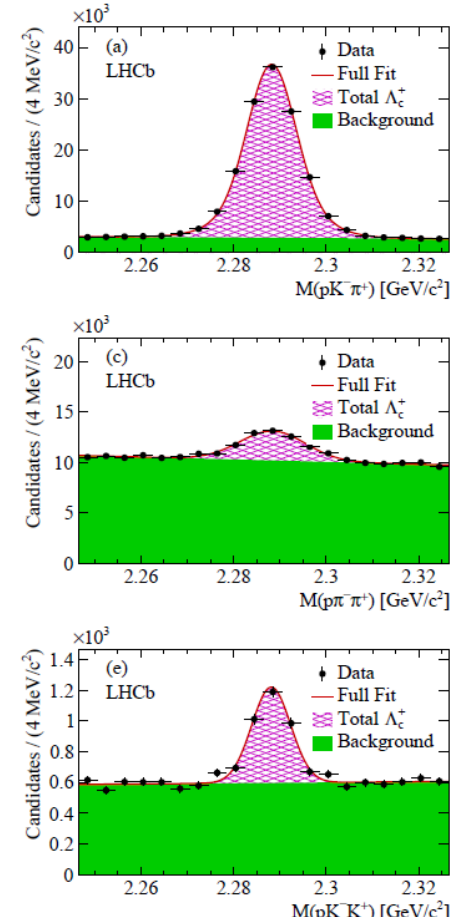
$$\frac{\mathcal{B}(\Lambda_c^+ \rightarrow p\pi^-\pi^+)}{\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+)} = (7.44 \pm 0.08 \pm 0.18) \%,$$

$$\frac{\mathcal{B}(\Lambda_c^+ \rightarrow pK^-K^+)}{\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+)} = (1.70 \pm 0.03 \pm 0.03) \%,$$

$$\frac{\mathcal{B}(\Lambda_c^+ \rightarrow p\pi^-K^+)}{\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\pi^+)} = (0.165 \pm 0.015 \pm 0.005) \%,$$

1 fb<sup>-1</sup> data @ 7 TeV

Prompt  $\Lambda_c^+ \rightarrow phh'$  selection



$$\mathcal{B}(\Lambda_c^+ \rightarrow p\pi^-\pi^+) = (4.72 \pm 0.05 \pm 0.11 \pm 0.25) \times 10^{-3},$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow pK^-K^+) = (1.08 \pm 0.02 \pm 0.02 \pm 0.06) \times 10^{-3},$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow p\pi^-K^+) = (1.04 \pm 0.09 \pm 0.03 \pm 0.05) \times 10^{-4},$$

# BESIII粲物理研究总结

## ■ $D^{0(+)}$ 研究取得一些重要物理成果

-- $D^+$ 衰变常数 $f_{D^+}$

--形状因子 $f^{D \rightarrow K(\pi)}_+(q^2)$

--CKM矩阵元 $|V_{cs(d)}|$

-- $D^0\bar{D}^0$ 混合参数 $y_{CP}, \delta_{K\pi}$

-- $D^0 \rightarrow K_S \pi^+ \pi^-$ 强相差初步结果

→精密检验格点QCD计算  
和CKM矩阵幺正性、探讨  
 $D^0\bar{D}^0$ 混合、约束 $\gamma/\phi_3$ 测量

## ■ $\Lambda_c^+$ 衰变的系统研究结束了其发现近40年来无近阈数据绝对测量的历史

■ 2016年，在4.178 GeV采集了 $3.2 \text{ fb}^{-1}$   $D_s^+$ 数据。已取得 $D_s^+$ 衰变常数 $f_{D_s^+}$ 、CKM矩阵元 $|V_{cs}|$ 等初步结果

■ 更多物理结果将在未来1-2年完成

**谢谢!**



# BESI/II上 $D_{(s)}^+ \rightarrow l^+ \nu$ 的寻找

22.3 pb<sup>-1</sup> at 4.03 GeV

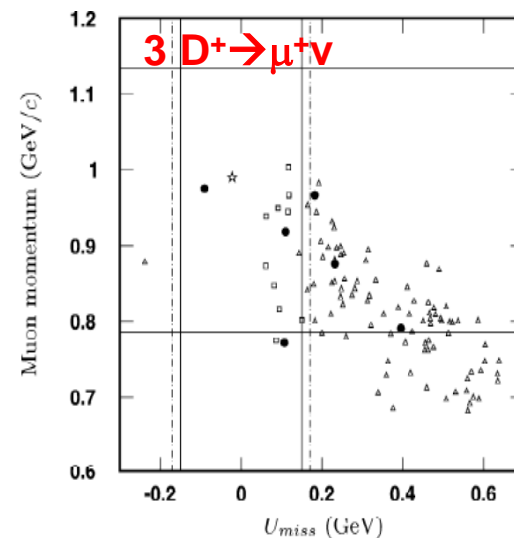
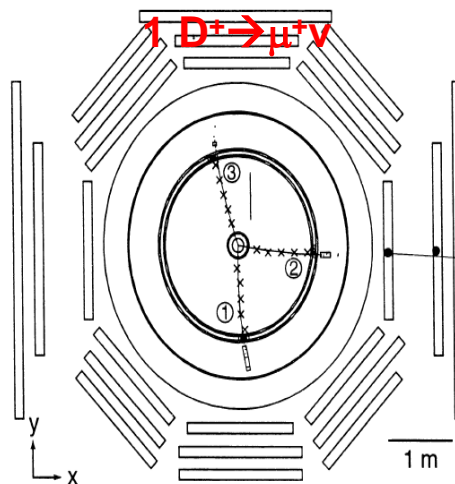
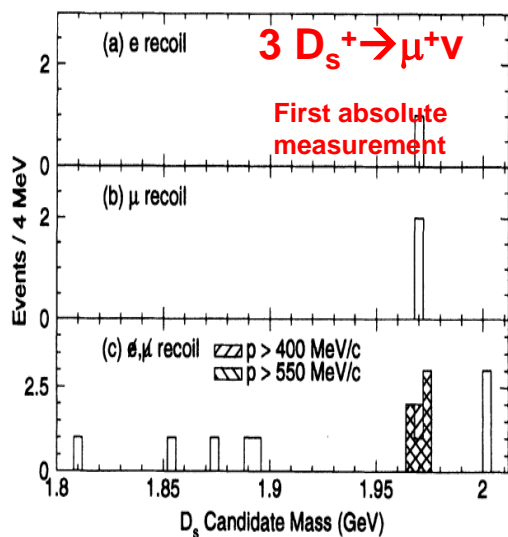
22.3 pb<sup>-1</sup> at 4.03 GeV

33 pb<sup>-1</sup> around  $\psi(3770)$

PRL74(1995)4599

PLB429(1998)188

PLB610(2005)183



$$f_{D_s^+} = (430^{+150+40}_{-130-40}) \text{ MeV}$$

$$f_{D^+} = (300^{+180+80}_{-150-40}) \text{ MeV}$$

$$f_{D^+} = (371^{+129}_{-119} \pm 25) \text{ MeV}$$

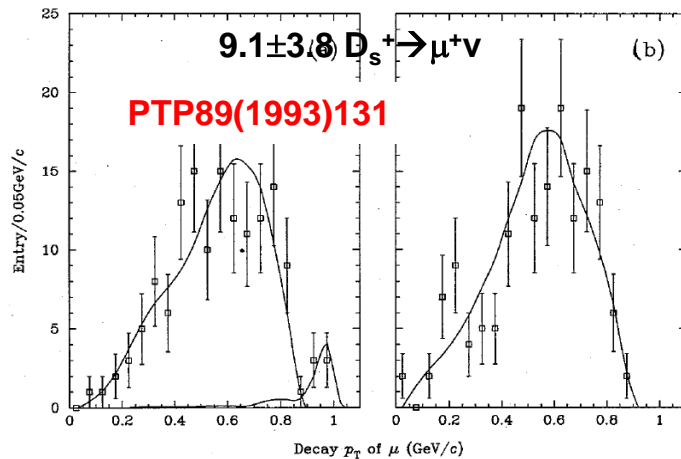
BESI

BESI

BESII

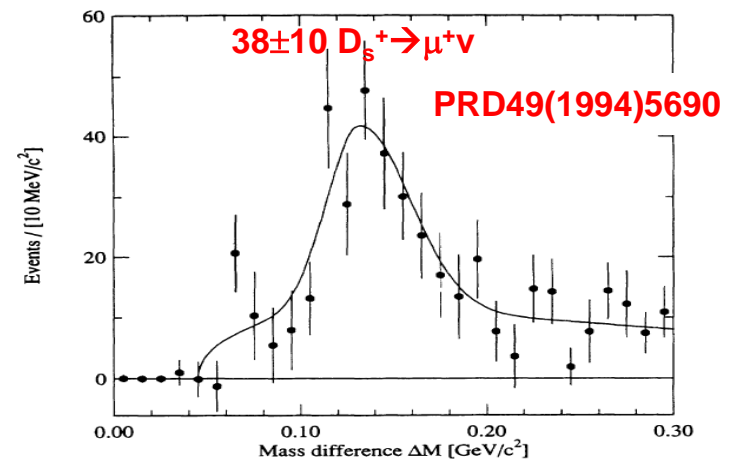
# 早期关于 $f_{D_{s^+}}$ 的测量

## ■ WA75, Fixed target experiment



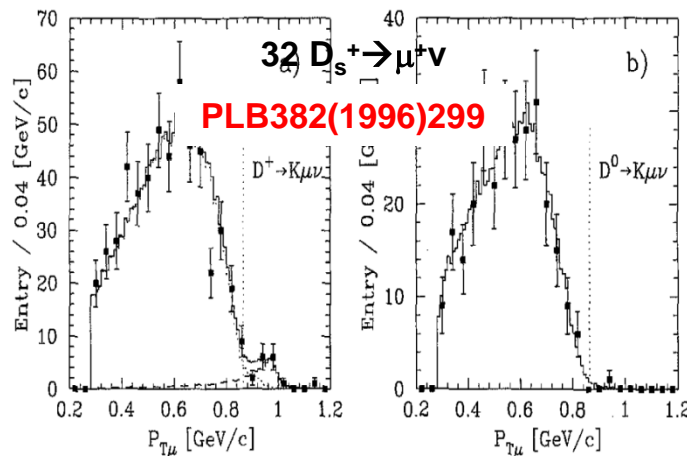
$$f_{D_{s^+}} = 232 \pm 45 \pm 20 \pm 48 \text{ MeV}$$

## ■ CLEOII, 2.13 fb<sup>-1</sup> at 10.6 GeV



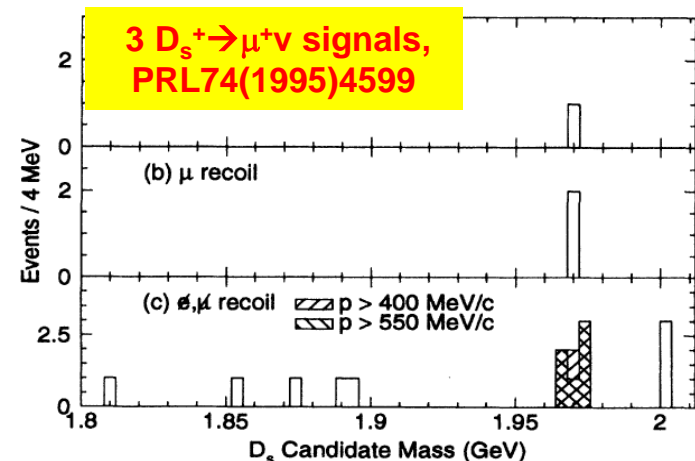
$$f_{D_{s^+}} = 344 \pm 37 \pm 52 \pm 42 \text{ MeV}$$

## ■ E653, Fermilab fixed target experiment



$$f_{D_{s^+}} = 194 \pm 35 \pm 20 \pm 14 \text{ MeV}$$

## ■ BESII, 22.3 pb<sup>-1</sup> at 4.03 GeV

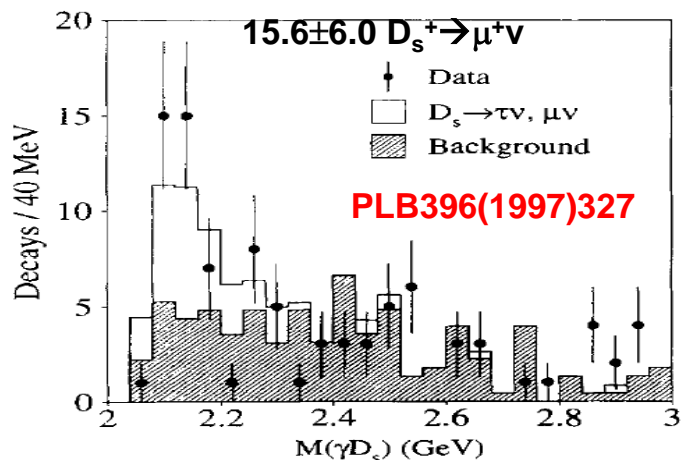


$$f_{D_{s^+}} = (430^{+150+40}_{-130-40}) \text{ MeV}$$

First absolute measurement

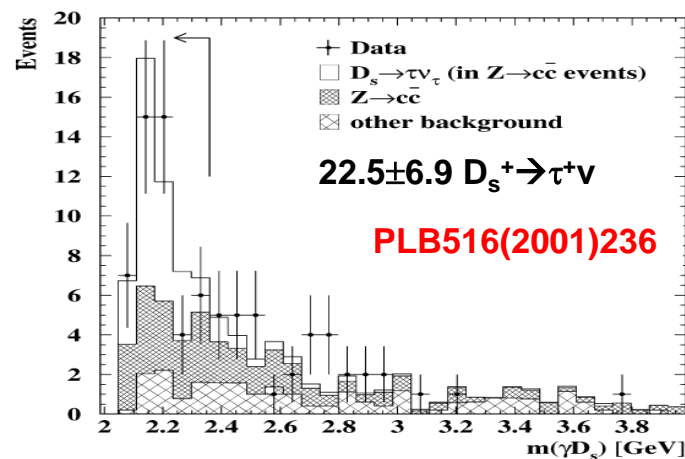
# 早期关于 $f_{D_{s^+}}$ 的测量

- L3,  $Z \rightarrow q\bar{q}$ ,  $49.6 \text{ pb}^{-1}$  at 91.2 GeV



$$f_{D_{s^+}} = 309 \pm 58 \pm 33 \pm 38 \text{ MeV}$$

- OPAL,  $3.9 \times 10^6 e^+e^- \rightarrow q\bar{q}$



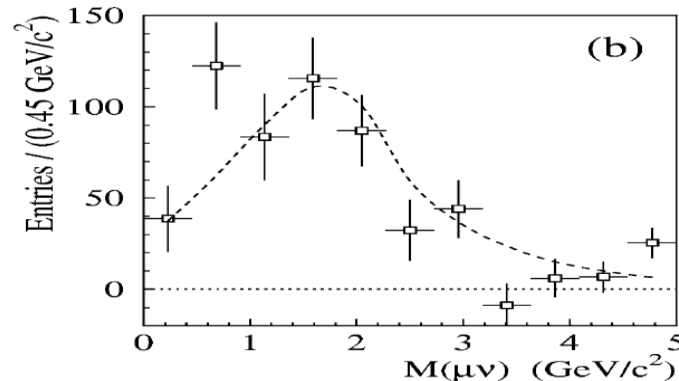
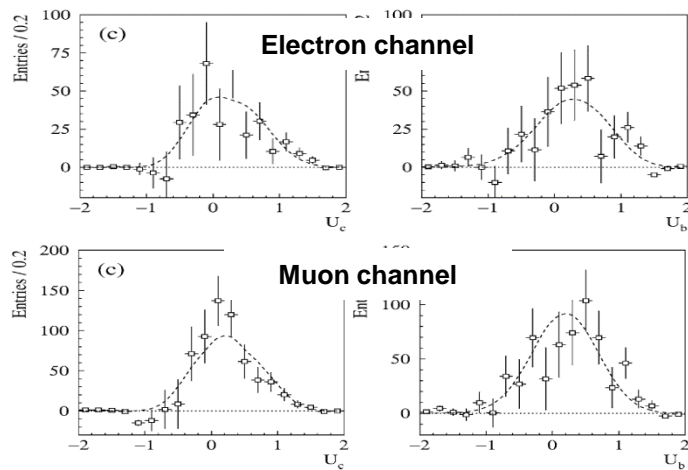
$$f_{D_{s^+}} = 286 \pm 44 \pm 41 \text{ MeV}$$

- ALPHA,  $3.97 \times 10^6 Z$  hadronic decay

$$306 \pm 62 D_s^+ \rightarrow \tau^+ \nu$$

$$\text{PLB528(2002)1}$$

$$575 \pm 84 D_s^+ \rightarrow \mu^+ \nu$$



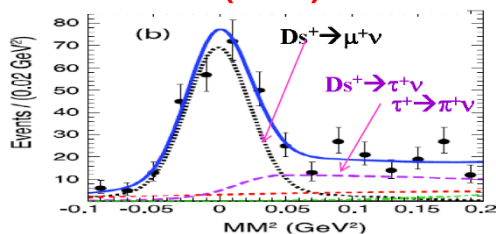
$$f_{D_{s^+}} = 285 \pm 19 \pm 40 \text{ MeV}$$

# 已有 $D_s^+ \rightarrow l^+ \nu$ 实验测量

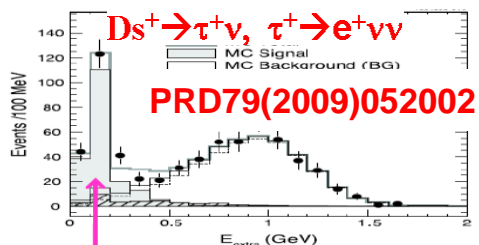
In the past 30 years,  $D_s^+ \rightarrow l^+ \nu$  has been studied by WA75, CLEOII, E653, BESII, L3, OPAL, ALPHA, **CLEO-c, BELLE, Babar**

■  $D_s^+ D_s^-$ , 600 pb<sup>-1</sup>  
@ 4.17 GeV [697  $l^+ \nu$ ]

PRD79(2009)052001

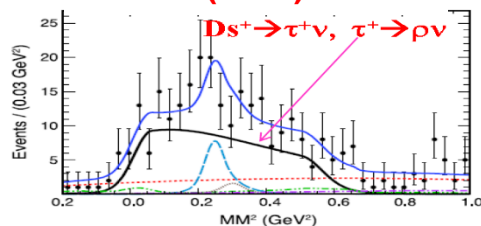


$f_{D_s^+} = 263.3 \pm 8.2 \pm 1.9$  MeV



Signal for  $D_s^+ \rightarrow \tau^+ \nu$   
 $f_{D_s^+} = 252.2 \pm 11.1 \pm 5.2$  MeV

PRD80(2009)112004

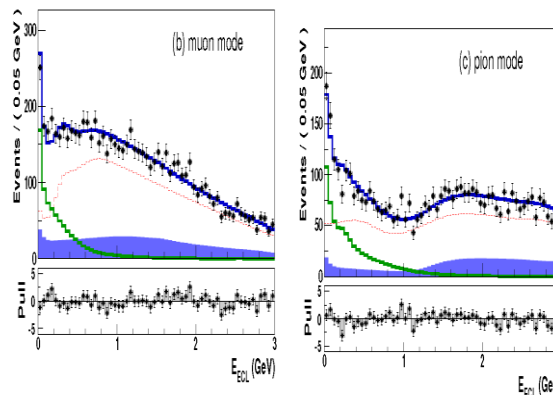
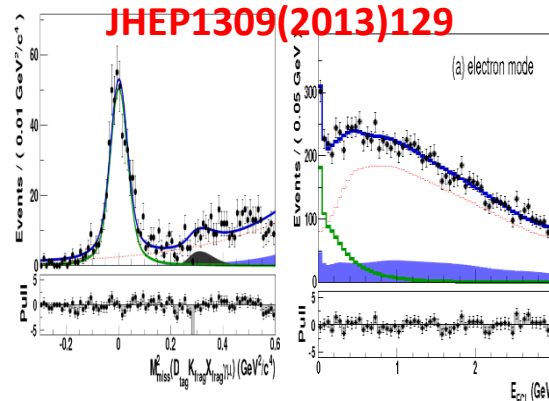


$f_{D_s^+} = 257.8 \pm 13.3 \pm 5.2$  MeV

■ Belle, 913 fb<sup>-1</sup> at  
10.58 GeV [2698  $l^+ \nu$ ]

$$e^+ e^- \rightarrow DKXD_s^{*-}$$

JHEP1309(2013)129

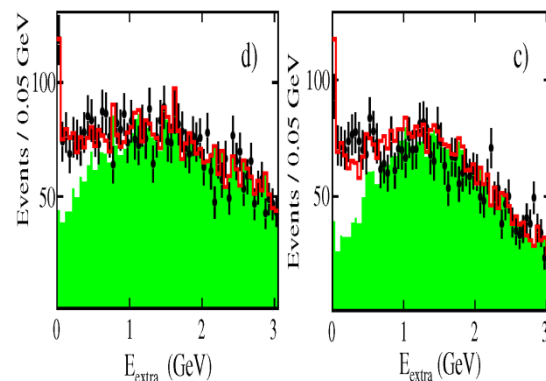
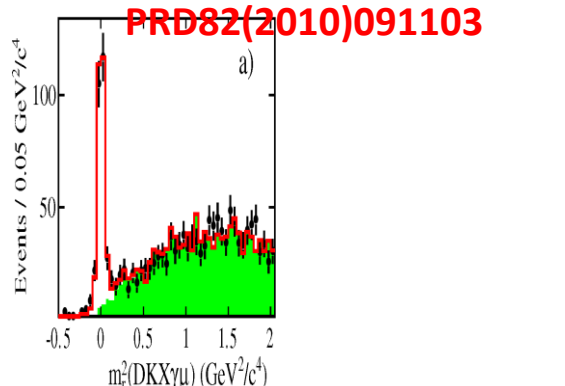


$f_{D_s^+} = 255.5 \pm 4.2 \pm 5.1$  MeV

■ Babar, 521 fb<sup>-1</sup> at  
10.58 GeV [1023  $l^+ \nu$ ]

$$e^+ e^- \rightarrow DKXD_s^{*-}$$

PRD82(2010)091103



$f_{D_s^+} = 258.6 \pm 6.4 \pm 7.5$  MeV <sup>70</sup>

# $D^+ \rightarrow K_L^0 e^+ \nu$ 分支比的首次测量

PRD92(2015)112008

➤ Regardless of long flight distance,  $K_L^0$  interact with EMC and deposit part of energy, thus giving position information

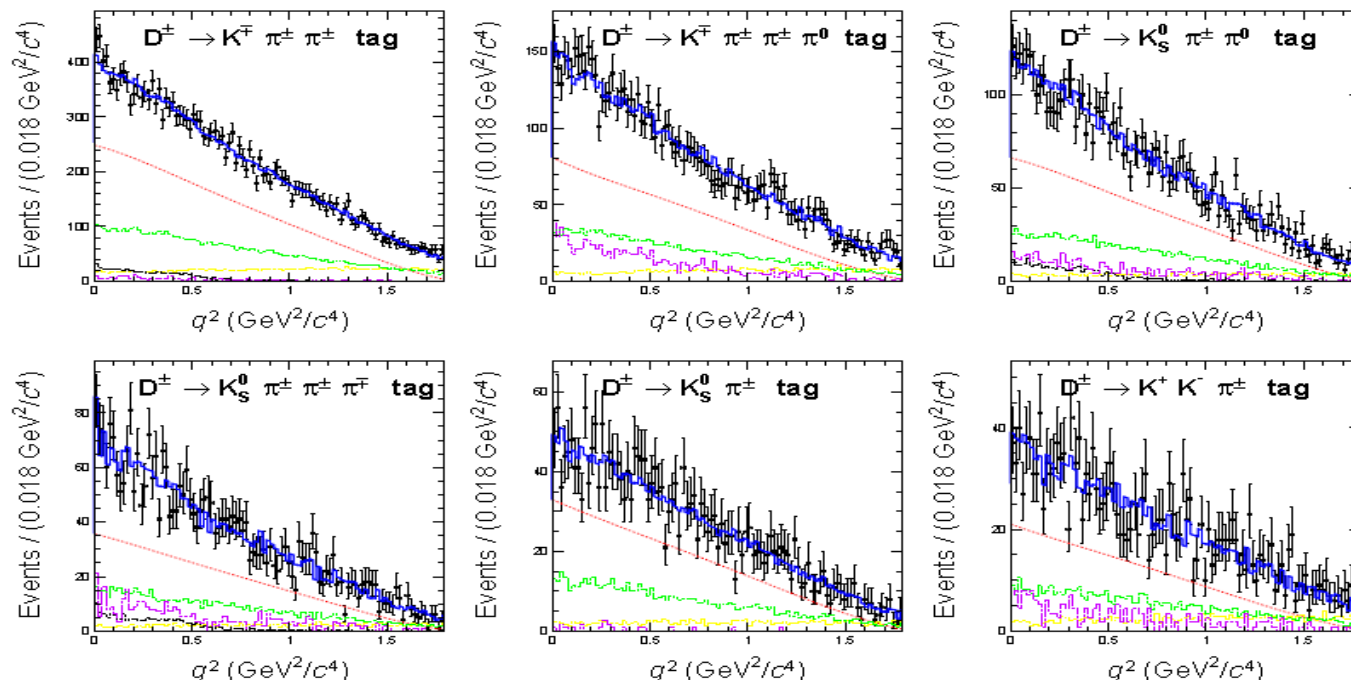
➤ After reconstructing all other particles,  $K_L^0$  can be inferred with position information and constrain  $U_{\text{miss}} \rightarrow 0$

$$B(D^+ \rightarrow K_L^0 e^+ \nu) = (4.482 \pm 0.027 \pm 0.103)\%$$

$$A_{CP} \equiv \frac{B(D^+ \rightarrow K_L^0 e^+ \nu_e) - B(D^- \rightarrow K_L^0 e^- \bar{\nu}_e)}{B(D^+ \rightarrow K_L^0 e^+ \nu_e) + B(D^- \rightarrow K_L^0 e^- \bar{\nu}_e)}$$

$$A_{CP}^{D^+ \rightarrow K_L e^+ \nu} = (-0.6 \pm 0.6 \pm 1.5)\%$$

Simultaneous fit to event density  $I(q^2)$  with 2-par. series Form Factor



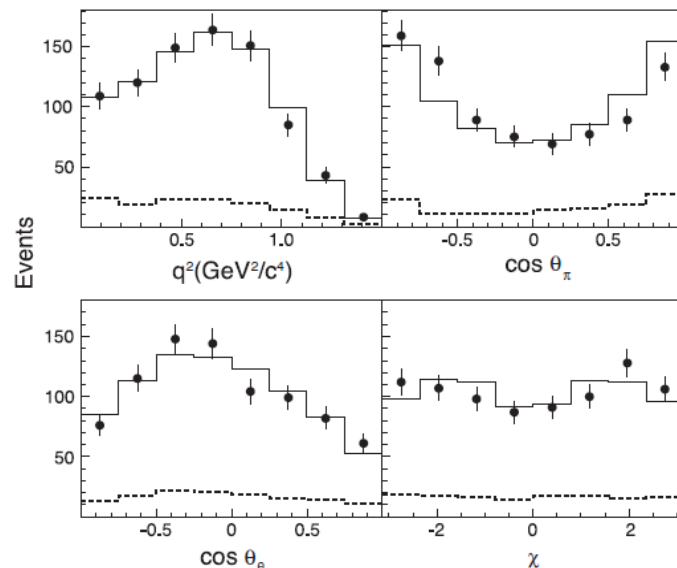
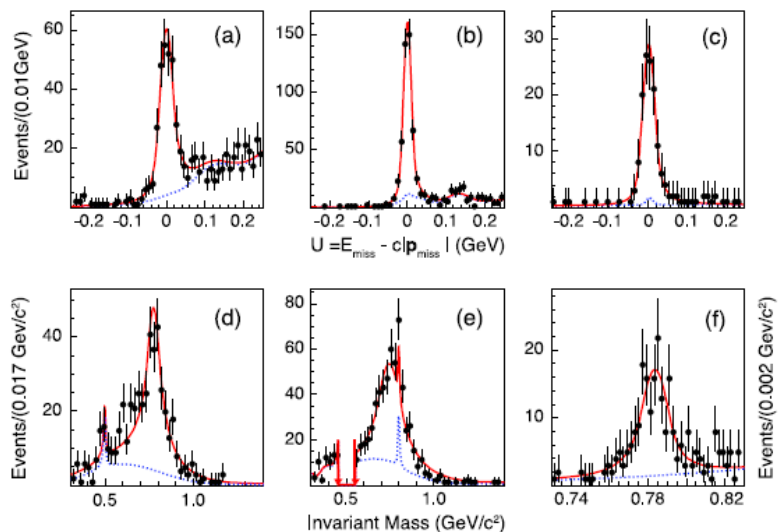
$D^+ \rightarrow K_L^0 e^+ \nu$  is measured for the first time

$$f_{+}^{K}(0)|V_{cs}| = 0.728 \pm 0.006 \pm 0.011$$

$$r_1 = a_1/a_0 = -1.91 \pm 0.33 \pm 0.24$$

# $D^+(0) \rightarrow \rho^0(-) e^+ \nu$ 振幅分析研究

CLEO, PRL110,131802 (2008)



Decay Mode	$\epsilon$ (%)	$N_{\text{tag,SL}}$	$\mathcal{B}_{\text{SL}}$	$\mathcal{B}_{\text{SL}} \text{ (prev)}$	$\mathcal{B}_{\text{SL}} \text{ (QCD SR)}$	$\mathcal{B}_{\text{SL}} \text{ (ISGW2)}$	$\mathcal{B}_{\text{SL}} \text{ (FK)}$
$D^0 \rightarrow \rho^- e^+ \nu_e$	$26.03 \pm 0.02$	$304.6 \pm 20.9$	$1.77 \pm 0.12 \pm 0.10$	$1.94 \pm 0.39 \pm 0.13$	$0.5 \pm 0.1$	1.0	2.0
$D^+ \rightarrow \rho^0 e^+ \nu_e$	$42.84 \pm 0.03$	$447.4 \pm 24.5$	$2.17 \pm 0.12^{+0.12}_{-0.22}$	$2.1 \pm 0.4 \pm 0.1$	...	1.3	2.5
$D^+ \rightarrow \omega e^+ \nu_e$	$14.67 \pm 0.03$	$128.5 \pm 12.6$	$1.82 \pm 0.18 \pm 0.07$	$1.6^{+0.7}_{-0.6} \pm 0.1$	...	1.3	2.5

$$\frac{\Gamma(D^0 \rightarrow \rho^- e^+ \nu_e)}{2\Gamma(D^+ \rightarrow \rho^0 e^+ \nu_e)} = 1.03 \pm 0.09^{+0.08}_{-0.02}$$

$$r_V = V(0)/A_1(0) = 1.48 \pm 0.15 \pm 0.05$$

$$r_2 = A_2(0)/A_1(0) = 0.83 \pm 0.11 \pm 0.04$$

BESIII相关工作正在开展

# 粲介子半轻衰变中同位旋是否守恒？

The 'long-standing puzzle' of whether the Isospin conservation holds in the exclusive semileptonic D decays

半轻子衰变的研究

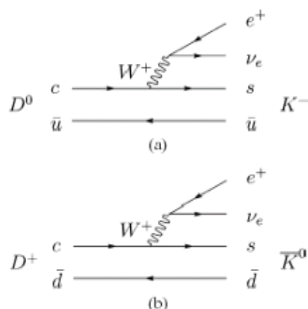
$$D^0 \rightarrow K^- e^+ \nu, \quad D^+ \rightarrow \bar{K}^0 e^+ \nu$$

## Motivation

Isospin conservation implies

$$\Gamma(D^0 \rightarrow K^- e^+ \nu_e) / \Gamma(D^+ \rightarrow \bar{K}^0 e^+ \nu_e) = 1$$

$$\Gamma(D^0 \rightarrow K^- e^+ \nu_e) / \Gamma(D^+ \rightarrow \bar{K}^0 e^+ \nu_e) = 1.4 \pm 0.2$$



	BES	MARK III	PDG02
$\frac{\Gamma(D^0 \rightarrow K^- e^+ \nu_e)}{\Gamma(D^+ \rightarrow \bar{K}^0 e^+ \nu_e)}$	$1.08 \pm 0.22 \pm 0.07$	$1.44 \pm 0.62$	$1.4 \pm 0.2$

Moriond EW04 (2004 年 3 月)  
ICHEP'04

Obtained based on the branching fractions quoted from PDG02

**BES-II 实验结果支持“D介子半轻子衰变过程中同位旋守恒”。**解决了粲介子物理领域内过去二十年中存在的一个“Puzzle”。

Paper published in  
PLB 608 (2005) 24

PLB644 (2007) 20

Measurement of the ratio of the partial widths

μ道联合电子道

	BES	MARK III	PDG02
$\frac{\Gamma(D^0 \rightarrow K^- l^+ \nu_e)}{\Gamma(D^+ \rightarrow \bar{K}^0 l^+ \nu_e)}$	$1.00 \pm 0.17 \pm 0.06$	$1.44 \pm 0.62$	$1.4 \pm 0.2$

Obtained based on the branching fractions quoted from PDG02

**BES-II 实验结果支持“D介子半轻子衰变过程中同位旋守恒”。 Solved the long-standing puzzle in D decays !** I. Shipsey, ICHEP'04

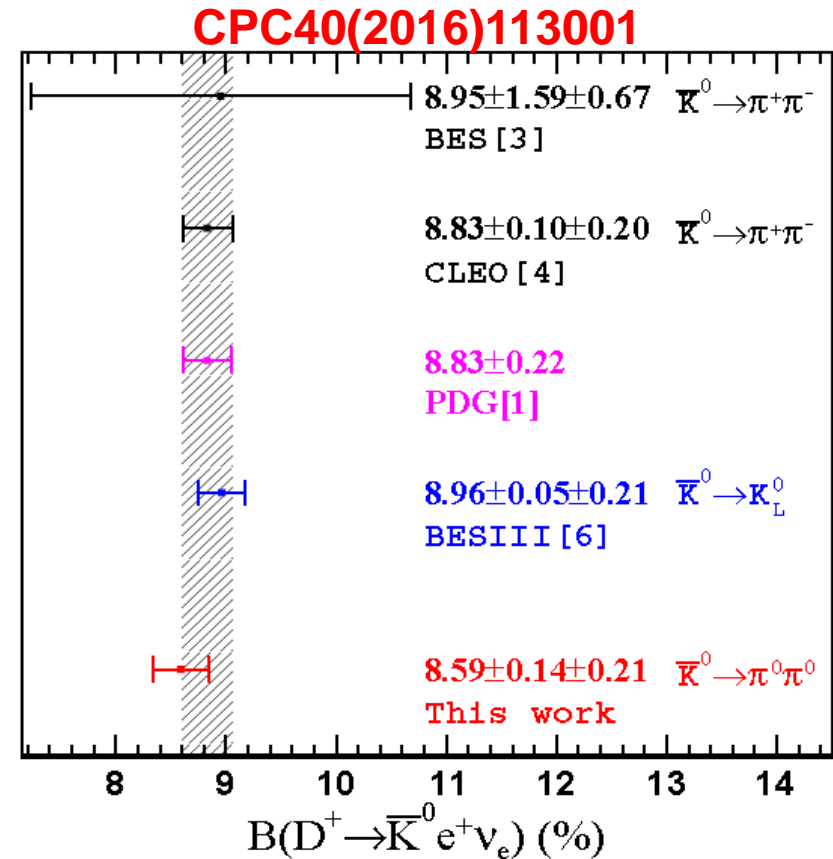
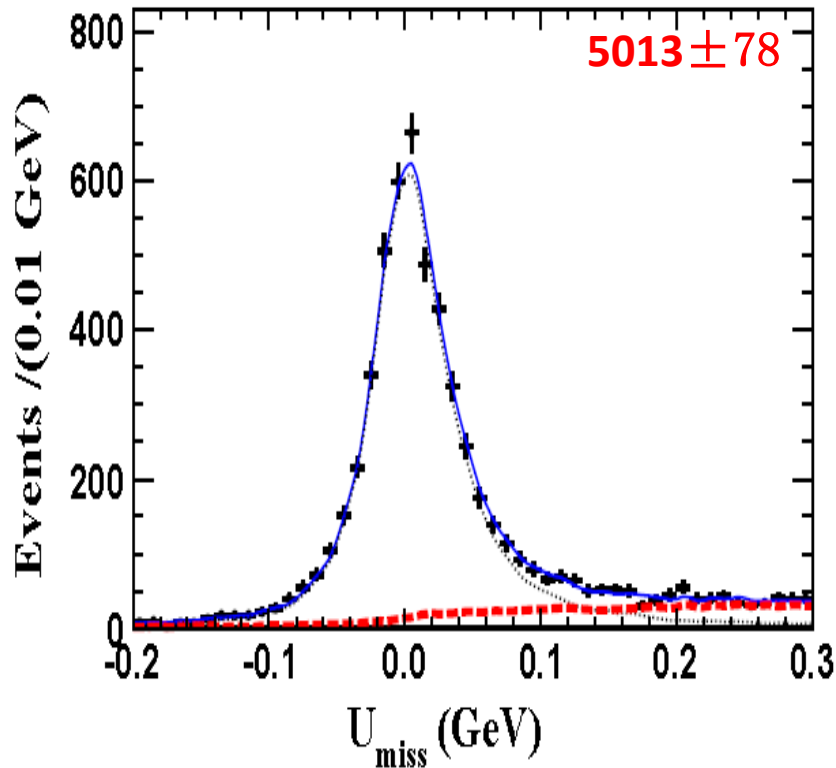
23

**CLEO-c confirmed the BES-II result**

$$\frac{\Gamma(D^0 \rightarrow K^- e^+ \nu_e)}{\Gamma(D^+ \rightarrow \bar{K}^0 e^+ \nu_e)} = 1.00 \pm 0.05 \pm 0.04$$



# 首次使用 $\bar{K}^0 \rightarrow \pi^0 \pi^0$ 测量 $D^+ \rightarrow \bar{K}^0 e^+ \nu$ 分支比



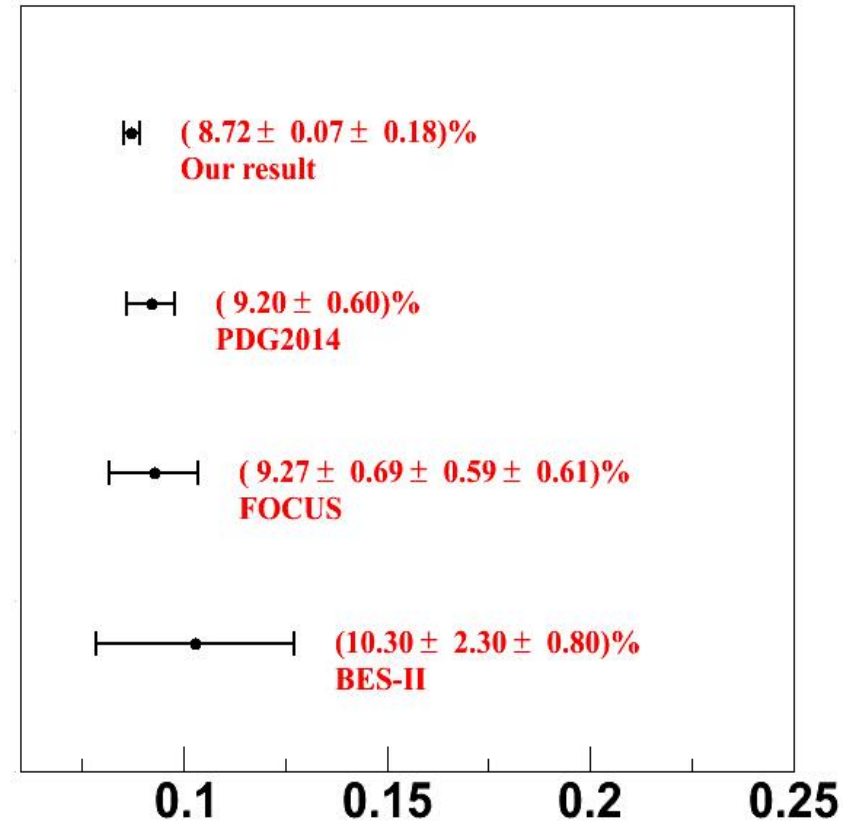
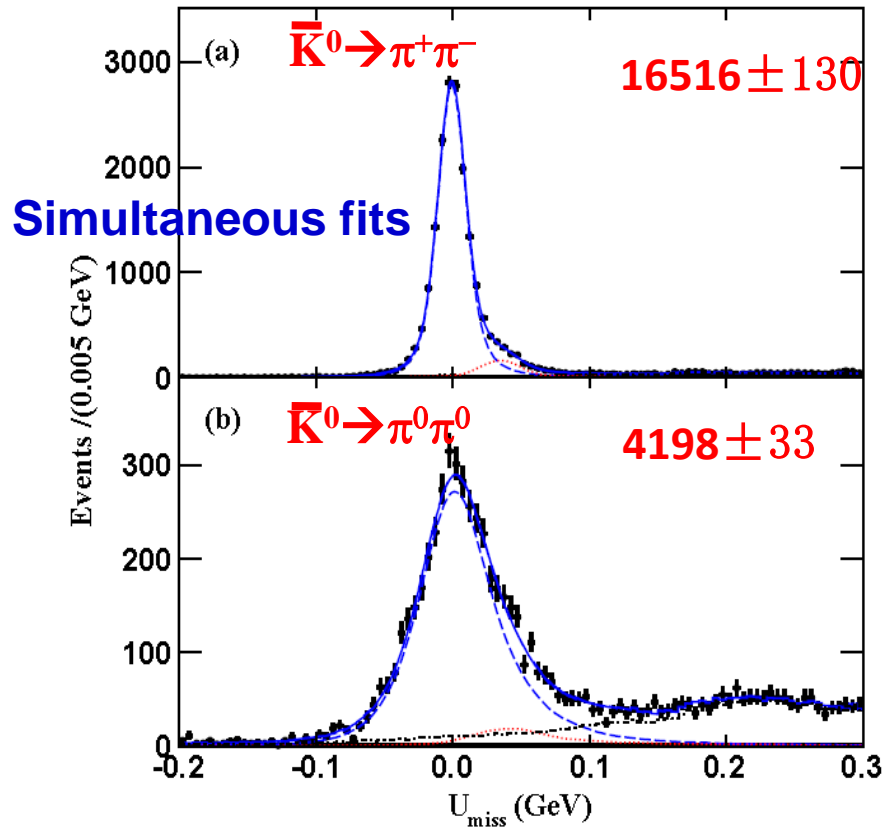
Taking  $\tau_{D^+}$ ,  $\tau_{D^0}$ ,  $B[D^0 \rightarrow K^- e^+ \nu]$  and  $B[D^+ \rightarrow \bar{K}^0 e^+ \nu]$  from the PDG as input

$$\frac{\Gamma[D^0 \rightarrow K^- e^+ \nu]}{\bar{\Gamma}[D^+ \rightarrow \bar{K}^0 e^+ \nu]} = 0.969 \pm 0.025$$

Agrees with isospin conservation within  $1.2\sigma$

# $D^+ \rightarrow \bar{K}^0 \mu^+ \nu$ 分支比的改进测量

EPJC76(2016)369



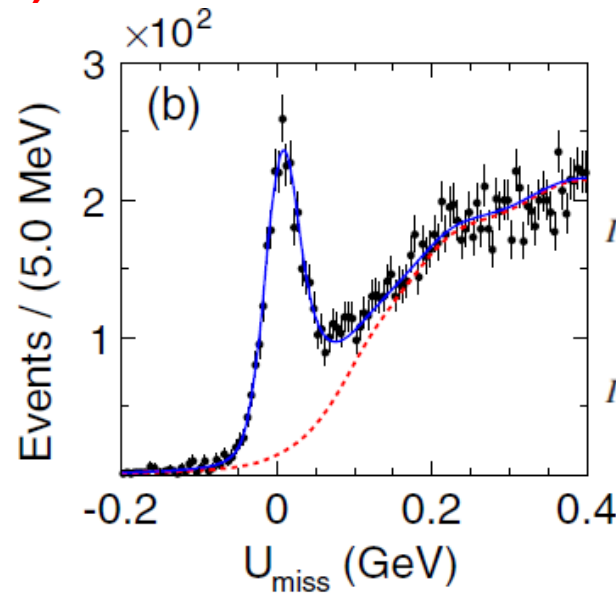
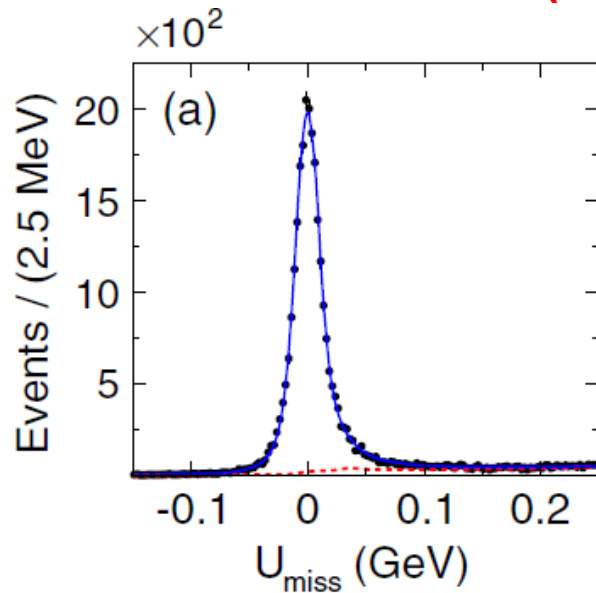
Taking  $B[D^0 \rightarrow K^- \mu^+ \nu]$   
and  $B[D^+ \rightarrow \bar{K}^0 e^+ \nu]$   
from the PDG as input

$$\frac{\Gamma[D^0 \rightarrow K^- \mu^+ \nu]}{\bar{\Gamma}[D^+ \rightarrow \bar{K}^0 \mu^+ \nu]} = 0.963 \pm 0.044$$

Support isospin conservation in  
these two decays within errors

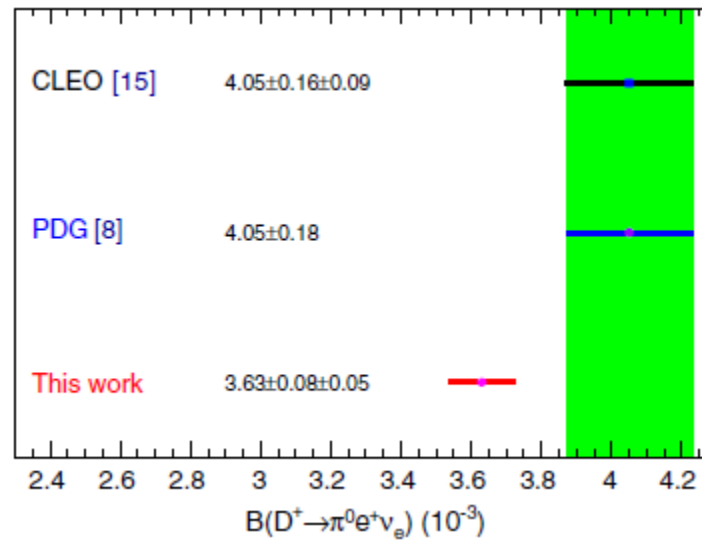
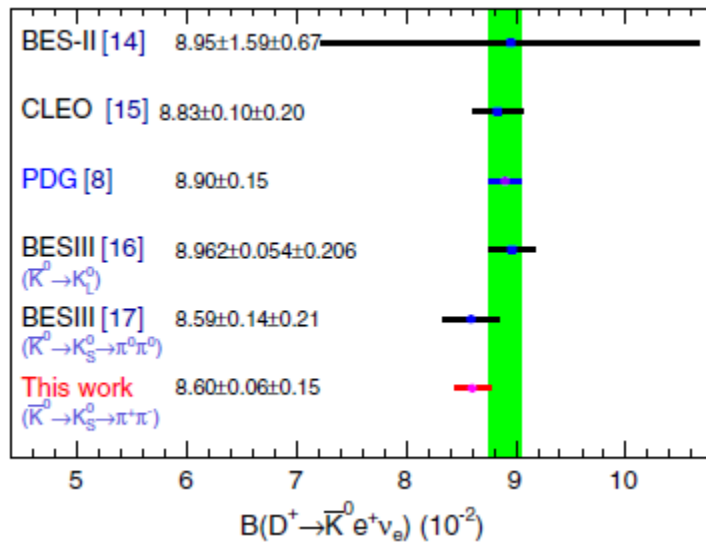
# 检验同位旋是否守恒

PRD96(2017)012002



$$I_K \equiv \frac{\Gamma(D^0 \rightarrow K^- e^+ \nu_e)}{\Gamma(D^+ \rightarrow \bar{K}^0 e^+ \nu_e)} = 1.03 \pm 0.01 \pm 0.02$$

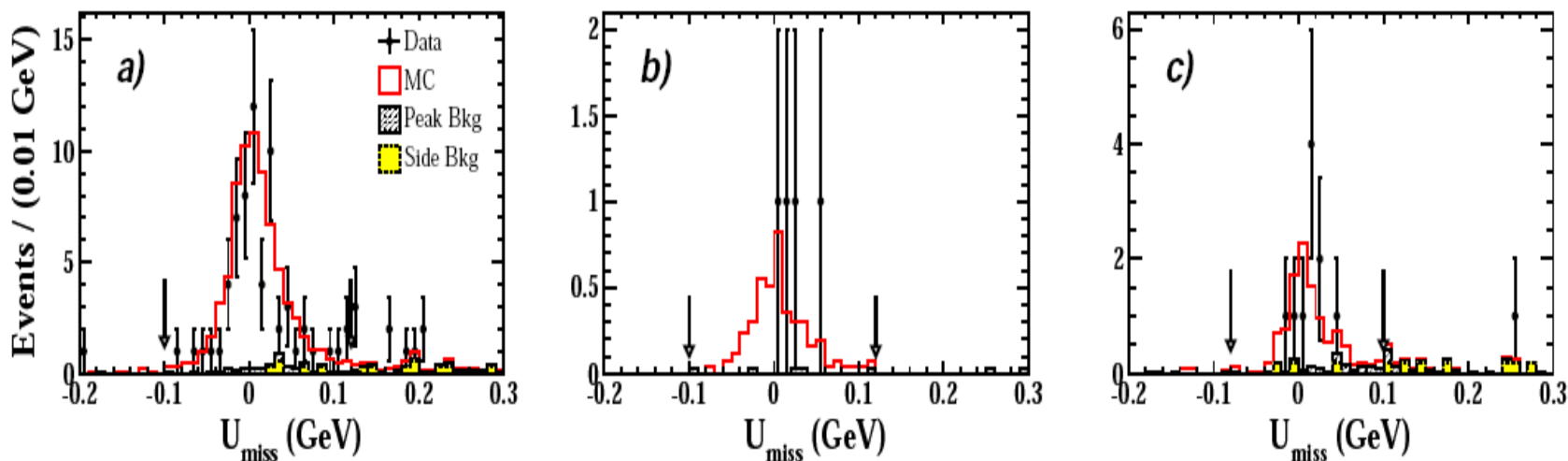
$$I_\pi \equiv \frac{\Gamma(D^0 \rightarrow \pi^- e^+ \nu_e)}{2\Gamma(D^+ \rightarrow \pi^0 e^+ \nu_e)} = 1.03 \pm 0.03 \pm 0.02$$



# $D_s^+ \rightarrow \eta^{(\prime)} e^+ \nu$ 分支比测量

- Benefit the understanding of the source of difference of inclusive decay rates of  $D^{0(+)}$  and  $D_s^+$
- Complementary information to understand  $\eta$ - $\eta'$  mixing

482 pb<sup>-1</sup> data @ 4.009 GeV, PRD94(2016)112003

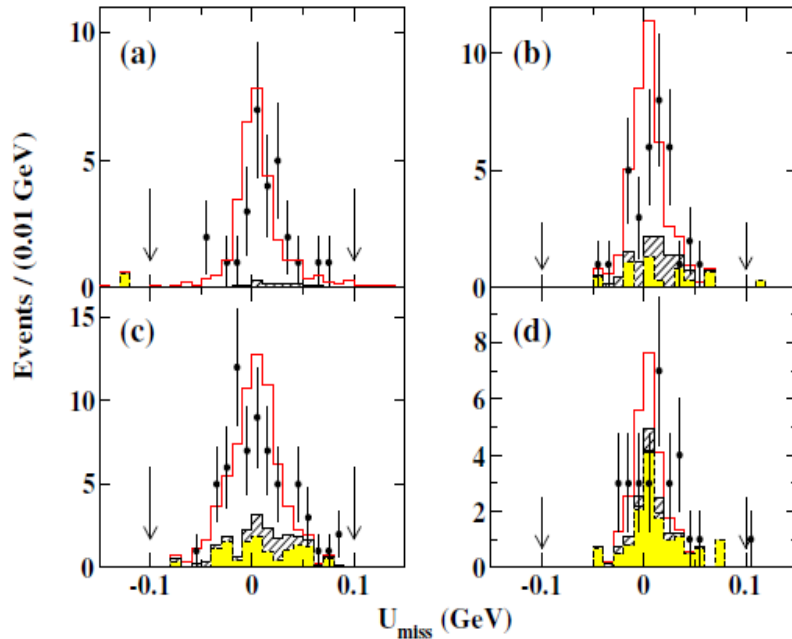


	BESIII	CLEOII 95	CLEOc09	CLEOc15	PDG [4]
$B(D_s^+ \rightarrow \eta e^+ \nu_e)[\%]$	$2.30 \pm 0.31 \pm 0.08$	—	$2.48 \pm 0.29 \pm 0.13$	$2.28 \pm 0.14 \pm 0.20$	$2.67 \pm 0.29$
$B(D_s^+ \rightarrow \eta' e^+ \nu_e)[\%]$	$0.93 \pm 0.30 \pm 0.05$	—	$0.91 \pm 0.33 \pm 0.05$	$0.68 \pm 0.15 \pm 0.06$	$0.99 \pm 0.23$
$\frac{B(D_s^+ \rightarrow \eta' e^+ \nu_e)}{B(D_s^+ \rightarrow \eta e^+ \nu_e)}$	$0.40 \pm 0.14 \pm 0.02$	$0.35 \pm 0.09 \pm 0.07$	—	—	—

# $D_s^+ \rightarrow \phi \mu^+ \nu, \eta^{(\prime)} \mu^+ \nu$ 分支比的首次测量

PRD97(2018)012006

482 pb<sup>-1</sup> data @ 4.009 GeV



- BFs of semi-muonic  $D_s^+$  decays are measured for the first time
- Benefit testing of lepton flavor universality and measuring the  $\eta$ - $\eta'$  mixing angle

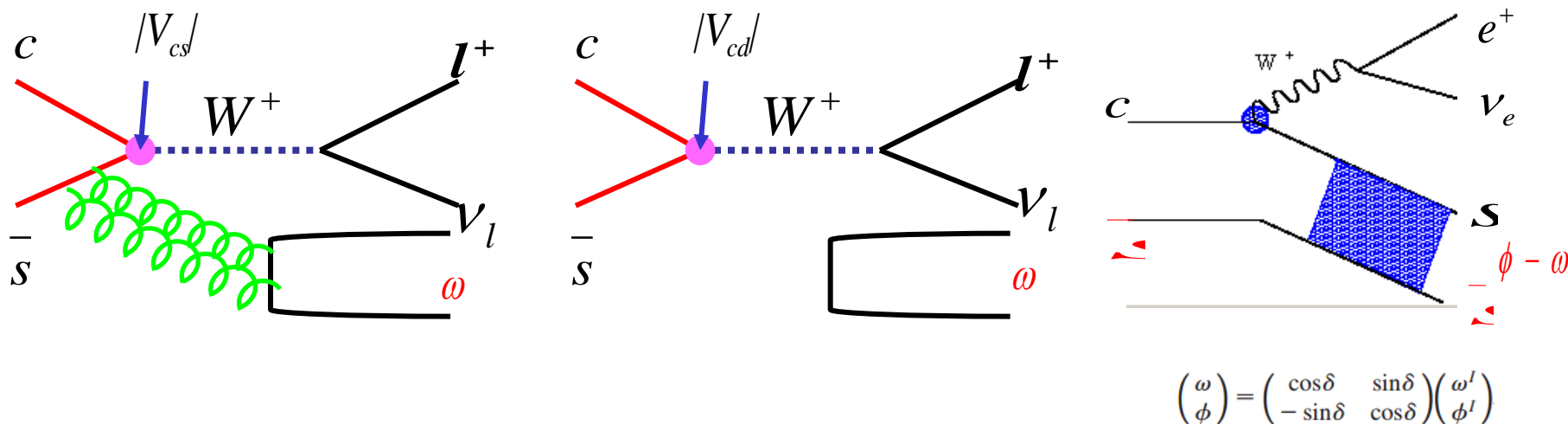
$$\frac{\Gamma[D_s^+ \rightarrow \phi \mu^+ \nu]}{\Gamma[D_s^+ \rightarrow \phi e^+ \nu]} = 0.86 \pm 0.29$$

$$\frac{\Gamma[D_s^+ \rightarrow \eta \mu^+ \nu]}{\Gamma[D_s^+ \rightarrow \eta e^+ \nu]} = 1.05 \pm 0.24$$

$$\frac{\Gamma[D_s^+ \rightarrow \eta' \mu^+ \nu]}{\Gamma[D_s^+ \rightarrow \eta' e^+ \nu]} = 1.14 \pm 0.68$$

$\mu^+$ mode	$\mathcal{B}_{\text{BESIII}} (\%)$	$\mathcal{B}_{\text{PDG}} (\%)$	$e^+$ mode	$\mathcal{B}_{\text{BESIII}} (\%)$	$\mathcal{B}_{\text{PDG}} (\%)$
$D_s^+ \rightarrow \phi \mu^+ \nu_\mu$	$1.94 \pm 0.53 \pm 0.09$	...	$D_s^+ \rightarrow \phi e^+ \nu_e$	$2.26 \pm 0.45 \pm 0.09$	$2.39 \pm 0.23$
$D_s^+ \rightarrow \eta \mu^+ \nu_\mu$	$2.42 \pm 0.46 \pm 0.11$	...	$D_s^+ \rightarrow \eta e^+ \nu_e$	$2.30 \pm 0.31 \pm 0.08$ [8]	$2.28 \pm 0.24$
$D_s^+ \rightarrow \eta' \mu^+ \nu_\mu$	$1.06 \pm 0.54 \pm 0.07$	...	$D_s^+ \rightarrow \eta' e^+ \nu_e$	$0.93 \pm 0.30 \pm 0.05$ [8]	$0.68 \pm 0.16$

# $D_s^+ \rightarrow \omega e^+ \nu$ 的寻找



$D_s^+$  四夸克态图象

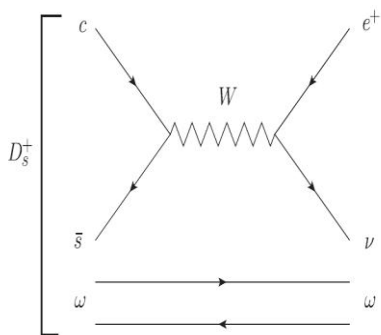
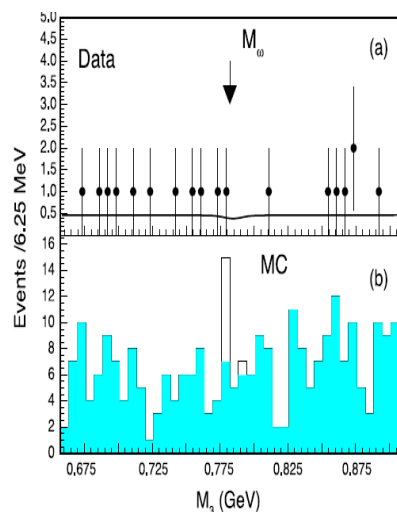


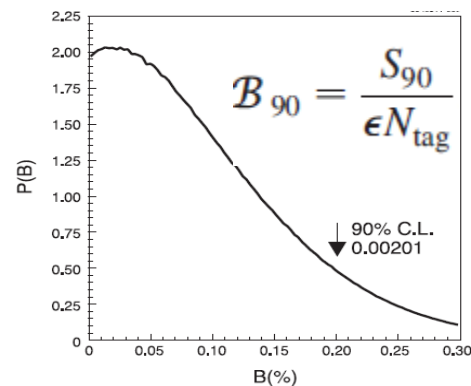
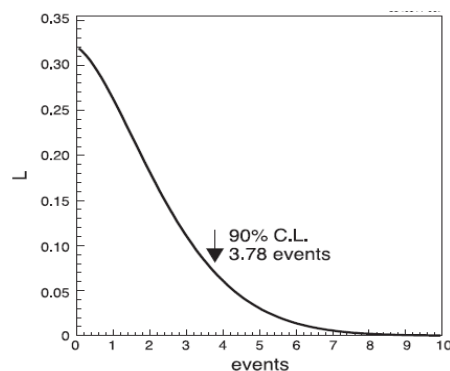
FIG. 1. Feynman diagram representing the four-quark semi-leptonic decay  $D_s^+ \rightarrow \omega e^+ \nu$ .

CLEO, PRD84, 012005



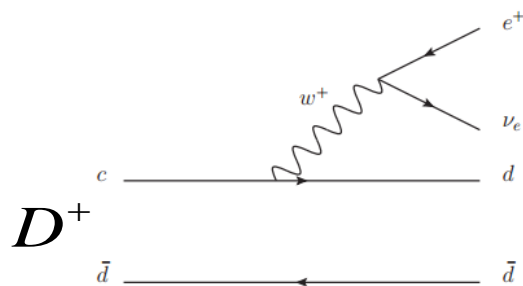
PRD79,074006:  $< 2 \times 10^{-4}$

$$R = (4.1 - 8.2)(\delta/3.34^\circ)^2 \times 10^{-3}$$



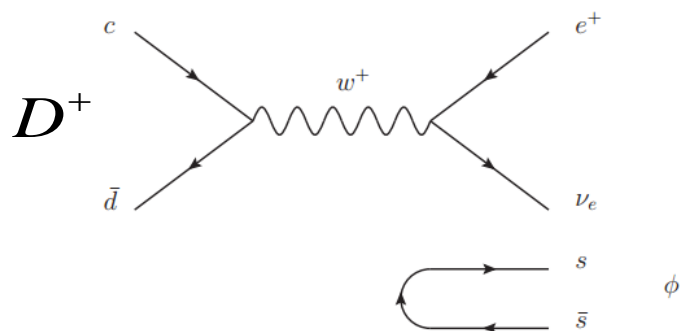
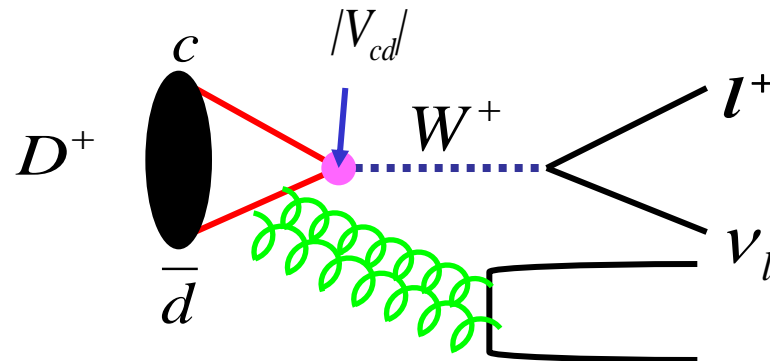
Search@BESIII is ongoing

# $D^+ \rightarrow \phi e^+ \nu$ 的寻找

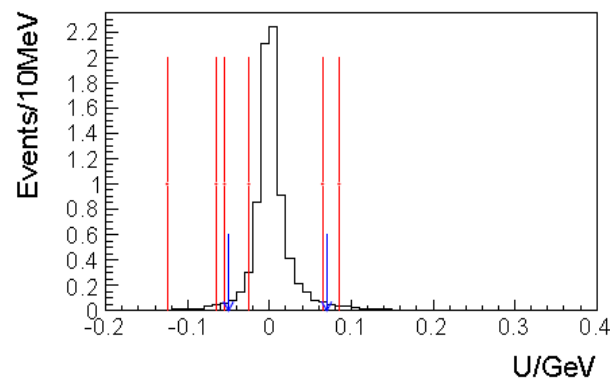


$$\omega \rightarrow \phi$$

$$\begin{pmatrix} \omega \\ \phi \end{pmatrix} = \begin{pmatrix} \cos\delta & \sin\delta \\ -\sin\delta & \cos\delta \end{pmatrix} \begin{pmatrix} \omega^I \\ \phi^I \end{pmatrix}$$



PRD92(2016)071101(RC)



$$B[D^+ \rightarrow \phi e^+ \nu] < 1.3 \times 10^{-5} \text{ at 90\% C.L.}$$



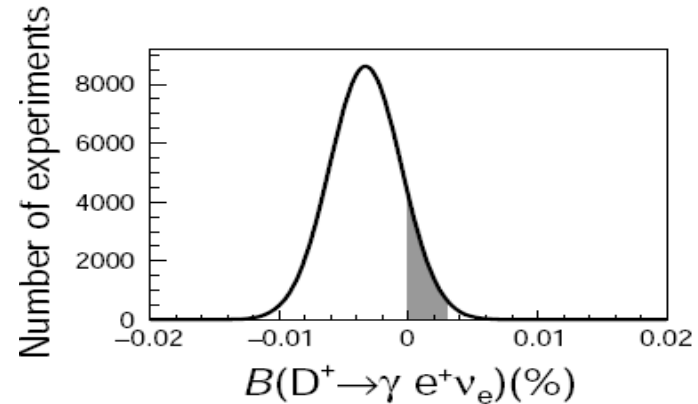
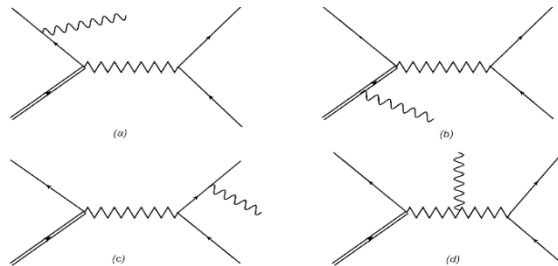
# $D_{(s)}^+$ 介子辐射半轻衰变

- no helicity suppression in contrast to pure leptonic decay, and simpler non-perturbative QCD calculation without final-state hadron

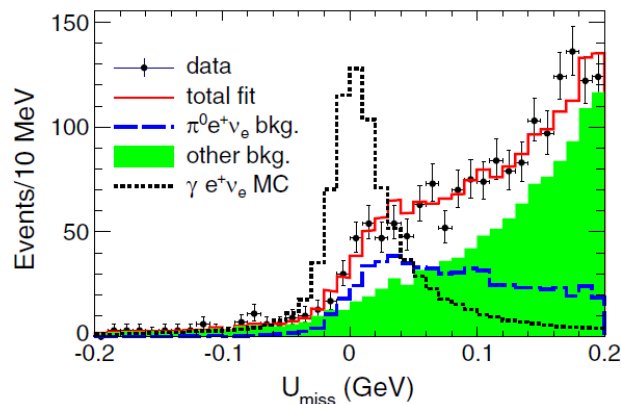
models	pQCD <sup>1</sup>	light front quark <sup>2</sup> & NR constituent quark model <sup>3</sup>	VMD <sup>4</sup>	factorization <sup>5</sup>
$\mathcal{B}_{theo.}$	$10^{-4}$	$10^{-6}$	$10^{-5}$ (enhanced by LD)	$10^{-5}$

[1][PRD 51, 111 (1995)] [2]MPLA 15, 2087 (2000); [3]PLB 562, 75 (2003);  
[4]MPLA 27, 1250120 (2012);[5]Nucl. Phys. B 889, 778 (2014); 914, 301 (2017)

## Tree level amplitudes



## PRD95(2017)071102(RC)



$$B[D^+ \rightarrow \gamma e^+ \nu] |_{E_\gamma > 10 \text{ MeV}} < 3.0 \times 10^{-4} \text{ @90\% C.L.}$$

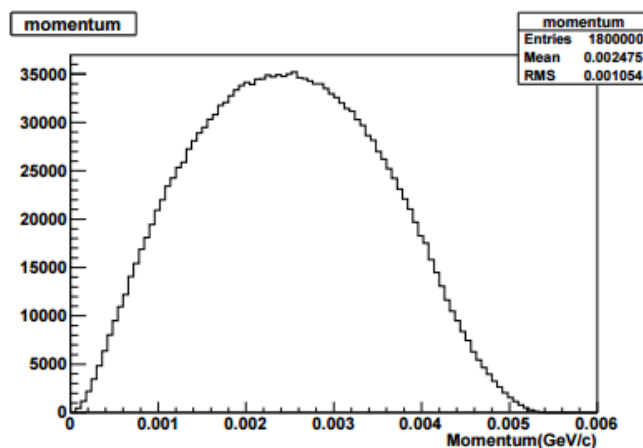
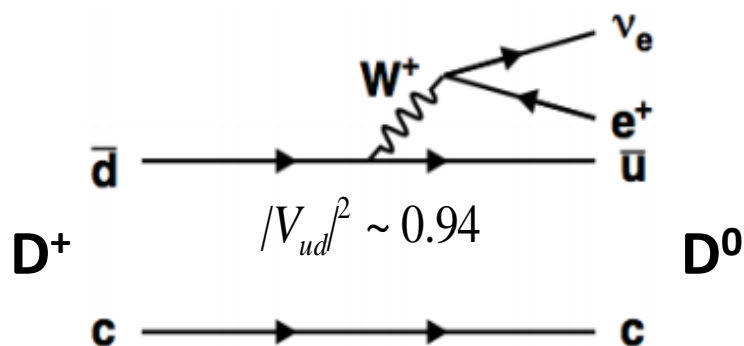
Search for  $D_s^+ \rightarrow \gamma e^+ \nu$   
@BESIII is ongoing

# $D_{(s)}^+ \rightarrow D^0 e^+ \nu$ 的寻找

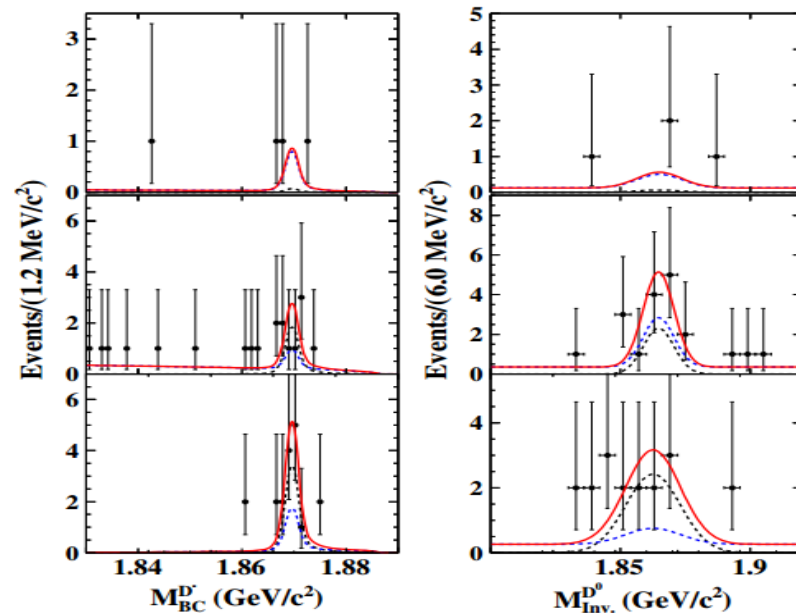
与其他半轻衰变  $c \rightarrow d/s l^+ \nu$  不同

此衰变通过  $d/s \rightarrow u l^+ \nu$

Applying the SU(3) symmetry for the light quarks, this rare decay branching fraction can be predicted by theoretical calculation and its theoretical value is  $2.78 \times 10^{-13}$  [EPJC, 59:841-845(2009)].



PRD96(2017)092002



$B[D^+ \rightarrow D^0 e^+ \nu] < 1 \times 10^{-4}$  @90% C.L.

# $D^0\bar{D}^0$ 混合和CP破坏

- Open-flavor neutral meson transforms to its anti-meson and vice versa:

$$K^0 \Leftrightarrow \bar{K}^0, B_d^0 \Leftrightarrow \bar{B}_d^0, B_s^0 \Leftrightarrow \bar{B}_s^0, D^0 \Leftrightarrow \bar{D}^0$$

- Flavor eigenstate ( $|D^0\rangle, |\bar{D}^0\rangle$ )  $\neq$  mass eigenstate  $|D_{1,2}\rangle$  with  $M_{1,2}$  and  $\Gamma_{1,2}$

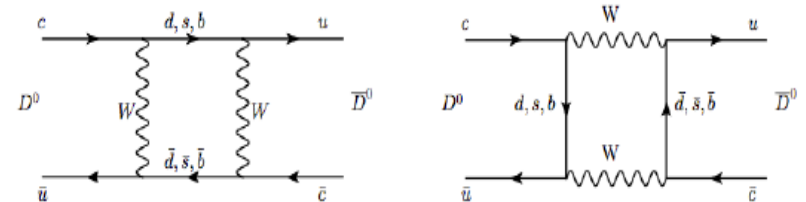
$$|D_{1,2}\rangle \equiv p|D^0\rangle \pm q|\bar{D}^0\rangle \quad (\text{CPT: } p^2 + q^2 = 1)$$

- Mixing parameters definition:

$$\boxed{\mathbf{x} \equiv \frac{M_1 - M_2}{\Gamma}, \quad \mathbf{y} \equiv \frac{\Gamma_1 - \Gamma_2}{2\Gamma}, \quad \Gamma \equiv \frac{\Gamma_1 + \Gamma_2}{2}}$$

- under phase convention  
 $CP|D^0\rangle = |\bar{D}^0\rangle, CP|\bar{D}^0\rangle = |D^0\rangle,$
- with CP conservation ( $q = p = 1/\sqrt{2}$ ):  
 $|D_{1,2}\rangle = |D_{+,-}\rangle$  (CP eigenstates)

- Unique: only the up-type meson for mixing
- Standard Model predicts:  $\sim \mathcal{O}(1\%)$



(1) short distance ( $< 0.1\%$  by CKM and GIM)



(2) long distance ( $\sim 1\%$ )

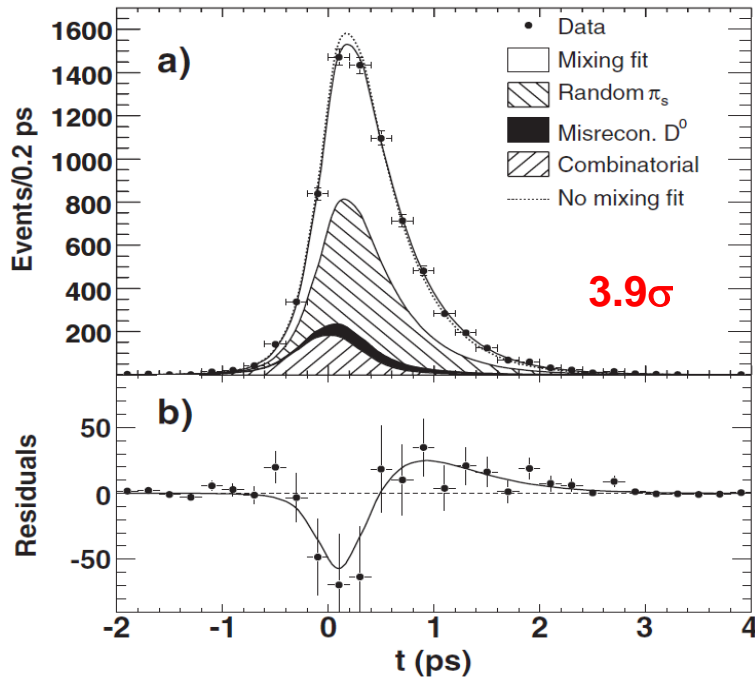
- Precise measurement of  $x, y$ : effectively limit New Physics(NP) modes;
- search for NP, eg:  $|x| \gg |y|$

# D<sup>0</sup> $\bar{D}^0$ 混合的迹象

■ Babar, 384 fb<sup>-1</sup>@10.58 GeV

PRL98(2007)211802

$$\frac{T_{WS}(t)}{e^{-\Gamma t}} \propto R_D + \sqrt{R_D} y' \Gamma t + \frac{x'^2 + y'^2}{4} (\Gamma t)^2$$



$$R_D = (0.303 \pm 0.016(\text{stat}) \pm 0.010(\text{syst}))\%$$

$$x'^2 = (-0.22 \pm 0.30(\text{stat}) \pm 0.21(\text{syst})) \times 10^{-3}$$

$$y' = (9.7 \pm 4.4(\text{stat}) \pm 3.1(\text{syst})) \times 10^{-3}$$

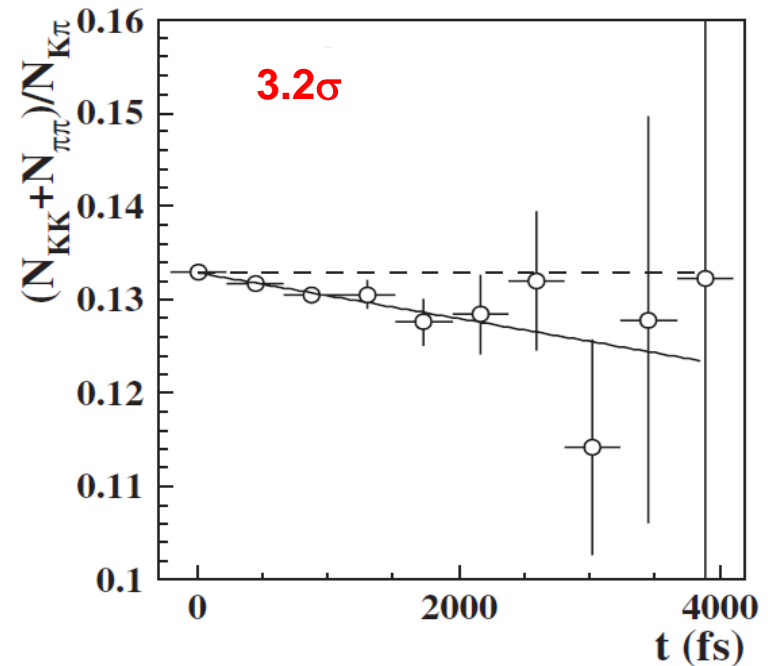
( $x'^2$ ,  $y'$ ) with correlation -0.95

■ BELLE, 540 fb<sup>-1</sup>@10.58 GeV

PRL98(2007)211803

$$y_{CP} = \frac{\tau(K^- \pi^+)}{\tau(K^+ K^-)} - 1$$

$$A_\Gamma = \frac{\tau(\bar{D}^0 \rightarrow K^- K^+) - \tau(D^0 \rightarrow K^+ K^-)}{\tau(\bar{D}^0 \rightarrow K^- K^+) + \tau(D^0 \rightarrow K^+ K^-)}$$



$$A_\Gamma = [0.01 \pm 0.30(\text{stat}) \pm 0.15(\text{syst})]\%$$

$$y_{CP} = [1.31 \pm 0.32(\text{stat}) \pm 0.25(\text{syst})]\%$$

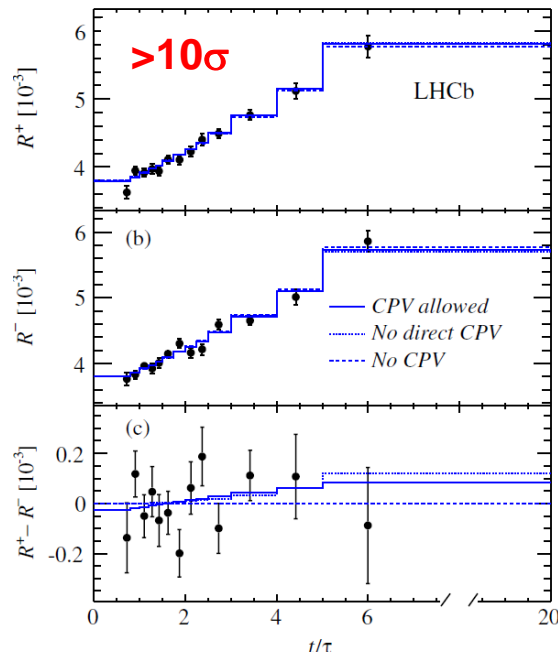
# D<sup>0</sup> $\bar{D}^0$ 混合的确认

■ LHCb, 3 fb<sup>-1</sup> p $\bar{p}$  at 7/8 TeV

PRL110(2013)101802 (1fb<sup>-1</sup>)

PRL111(2013)251801

$$R(t) \approx R_D + \sqrt{R_D} y' \frac{t}{\tau} + \frac{x'^2 + y'^2}{4} \left(\frac{t}{\tau}\right)^2$$



$$x'^2 = (5.5 \pm 4.9) \times 10^{-5},$$

$$y' = (4.8 \pm 1.0) \times 10^{-3}$$

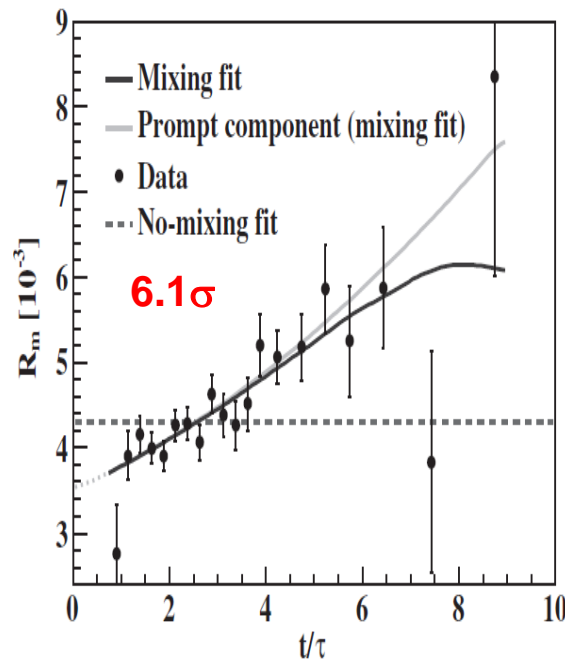
$$R_D = (3.568 \pm 0.066) \times 10^{-3}$$

■ CDFII, 9.6 fb<sup>-1</sup> p $\bar{p}$  at 1.96 TeV

PRL100(2008)121802(1.5 fb<sup>-1</sup>)

PRL111(2013)231802

$$R(t/\tau) = R_D + \sqrt{R_D} y' (t/\tau) + \frac{x'^2 + y'^2}{4} (t/\tau)^2.$$



$$x'^2 = (0.08 \pm 0.18) \times 10^{-3}$$

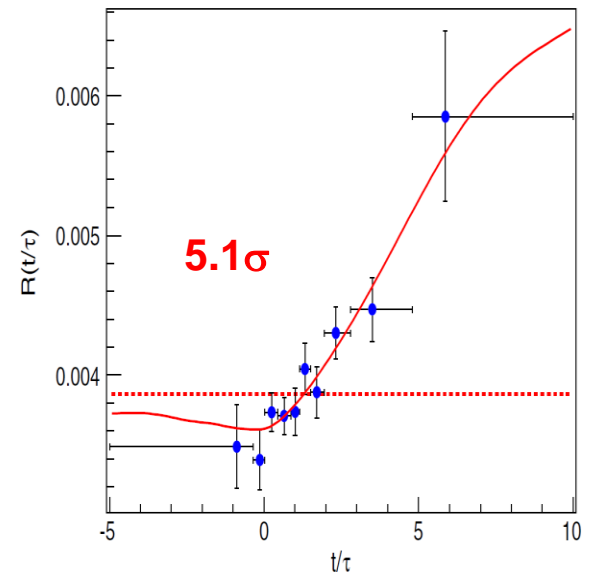
$$y' = (4.3 \pm 4.3) \times 10^{-3},$$

$$R_D = (3.51 \pm 0.35) \times 10^{-3}$$

■ Belle, 976 fb<sup>-1</sup> at 10.58 GeV

PRL112(2014)111801

$$R(\tilde{t}/\tau) = \frac{\Gamma_{\text{WS}}(\tilde{t}/\tau)}{\Gamma_{\text{RS}}(\tilde{t}/\tau)} \approx R_D + \sqrt{R_D} y' \frac{\tilde{t}}{\tau} + \frac{x'^2 + y'^2}{4} \left(\frac{\tilde{t}}{\tau}\right)^2$$



$$x'^2 = (0.09 \pm 0.22) \times 10^{-3}$$

$$y' = (4.6 \pm 3.4) \times 10^{-3}$$

$$R_D = (3.53 \pm 0.13) \times 10^{-3}$$

# D<sup>0</sup> $\bar{D}^0$ 混合和CP破坏参数

Decay Mode	Observables	Relationship
$D^0 \rightarrow K^+ K^- / \pi^+ \pi^-$	$y_{CP}$ $A_\Gamma$	$2y_{CP} = ( q/p  +  p/q ) y \cos \phi - ( q/p  -  p/q ) x \sin \phi$ $2A_\Gamma = ( q/p  -  p/q ) y \cos \phi - ( q/p  +  p/q ) x \sin \phi$
$D^0 \rightarrow K_S^0 \pi^+ \pi^-$	$x$ $y$ $ q/p $ $\phi$	
$D^0 \rightarrow K^+ \ell^- \nu$	$R_M$	$R_M = (x^2 + y^2)/2$
$D^0 \rightarrow K^+ \pi^- \pi^0$ (Dalitz plot analysis)	$x''$ $y''$	$x'' = x \cos \delta_{K\pi\pi} + y \sin \delta_{K\pi\pi}$ $y'' = y \cos \delta_{K\pi\pi} - x \sin \delta_{K\pi\pi}$
“Double-tagged” branching fractions measured in $\psi(3770) \rightarrow DD$ decays	$R_M$ $y$ $R_D$ $\sqrt{R_D} \cos \delta$	$R_M = (x^2 + y^2)/2$
$D^0 \rightarrow K^+ \pi^-$	$x'^2, y'$ $x'^{2+}, x'^{2-}$ $y'^+, y'^-$	$x' = x \cos \delta + y \sin \delta$ $y' = y \cos \delta - x \sin \delta$ $A_M \equiv ( q/p ^4 - 1)/( q/p ^4 + 1)$ $x'^{\pm} = [(1 \pm A_M)/(1 \mp A_M)]^{1/4} \times (x' \cos \phi \pm y' \sin \phi)$ $y'^{\pm} = [(1 \pm A_M)/(1 \mp A_M)]^{1/4} \times (y' \cos \phi \mp x' \sin \phi)$
$D^0 \rightarrow K^+ \pi^- / K^- \pi^+$ (time-integrated)	$\frac{\Gamma(D^0 \rightarrow K^+ \pi^-) + \Gamma(\bar{D}^0 \rightarrow K^- \pi^+)}{\Gamma(D^0 \rightarrow K^- \pi^+) + \Gamma(\bar{D}^0 \rightarrow K^+ \pi^-)}$ $\frac{\Gamma(D^0 \rightarrow K^+ \pi^-) - \Gamma(\bar{D}^0 \rightarrow K^- \pi^+)}{\Gamma(D^0 \rightarrow K^+ \pi^-) + \Gamma(\bar{D}^0 \rightarrow K^- \pi^+)}$	$R_D$ $A_D$
$D^0 \rightarrow K^+ K^- / \pi^+ \pi^-$ (time-integrated)	$\frac{\Gamma(D^0 \rightarrow K^+ K^-) - \Gamma(\bar{D}^0 \rightarrow K^+ K^-)}{\Gamma(D^0 \rightarrow K^+ K^-) + \Gamma(\bar{D}^0 \rightarrow K^+ K^-)}$ $\frac{\Gamma(D^0 \rightarrow \pi^+ \pi^-) - \Gamma(\bar{D}^0 \rightarrow \pi^+ \pi^-)}{\Gamma(D^0 \rightarrow \pi^+ \pi^-) + \Gamma(\bar{D}^0 \rightarrow \pi^+ \pi^-)}$	$A_K + \frac{\langle t \rangle}{\tau_D} \mathcal{A}_{CP}^{\text{indirect}} \quad (\mathcal{A}_{CP}^{\text{indirect}} \approx -A_\Gamma)$ $A_\pi + \frac{\langle t \rangle}{\tau_D} \mathcal{A}_{CP}^{\text{indirect}} \quad (\mathcal{A}_{CP}^{\text{indirect}} \approx -A_\Gamma)$

混合参数:x,y

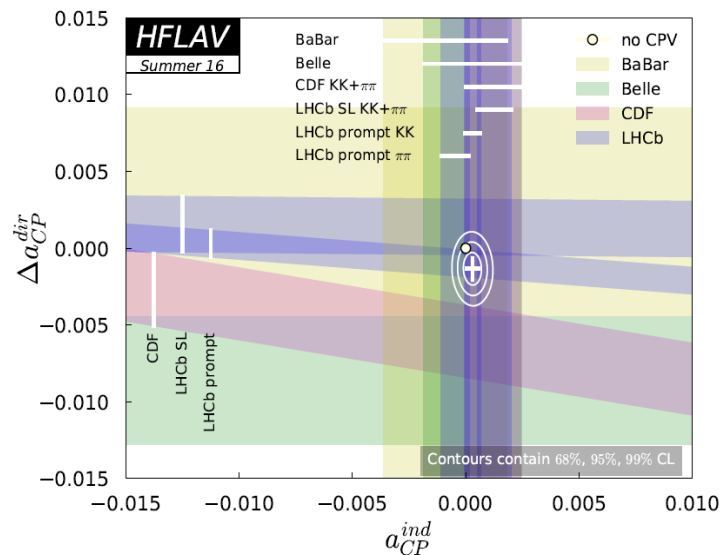
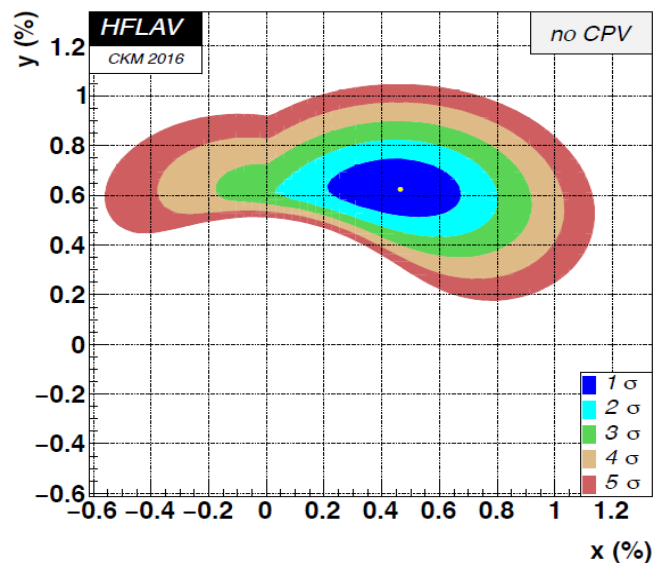
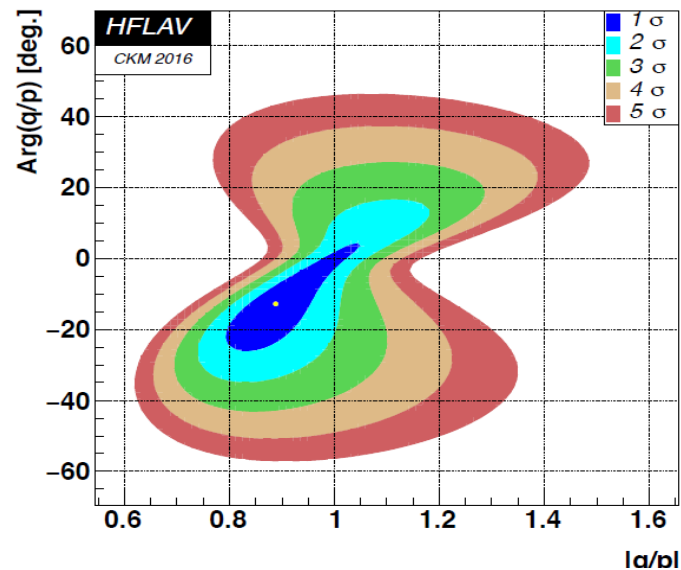
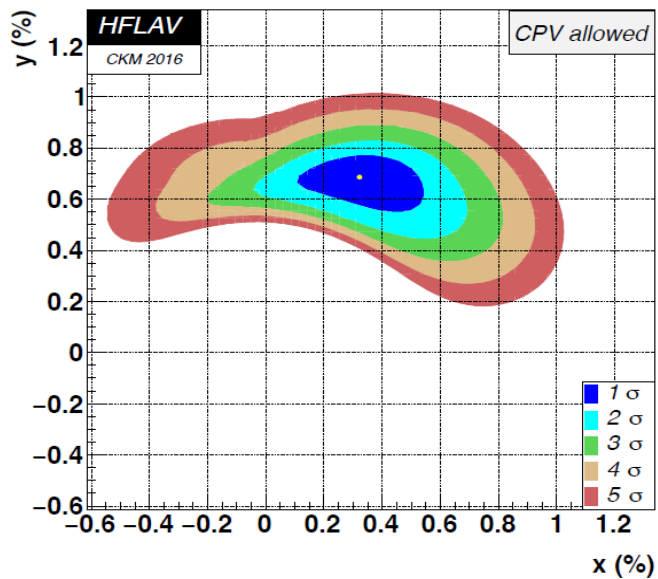
间接CPV参数:|q/p|,φ

直接CPV参数:A<sub>D</sub>,A<sub>K</sub>,A<sub>π</sub>

R<sub>D</sub>

强相差参数:δ<sub>Kπ</sub>, δ<sub>Kππ0</sub>

# $D^0\bar{D}^0$ 混合和CP破坏主要参数平均



$D^0\bar{D}^0$  mixing is observed, no direct CPV is found